Fairfield Public Schools

Math Curriculum K-6



Contributors:

Nicole Carnovale – Kindergarten Laura Barra – Grade 1 Andrea Goldsmith – Grade 2 Jen Sarna – Grade 3 Giana D'Arco – Grade 4 Joleen Dickson – Grade 5 Megan Dewland – Grade 6 James Verrengia – Math Coach, Grades 3-6 Jennifer Valenti – Math Coach, Grades K-2

Board Approved: August 15, 2024

Fairfield Mathematics

Contents

- 1. Instructional Materials p. 2
- 2. Supplemental Resources p. 2
- 3. Kindergarten p. 3-22
- 4. First Grade p. 23-42
- 5. Second Grade p. 43-61
- 6. Third Grade p. 62-78
- 7. Fourth Grade p. 79-96
- 8. Fifth Grade p. 97-114
- 9. Sixth Grade p. 115-131

Instructional Materials

Math Expressions © HMH Publishing Company 2018

Big Ideas: Modeling Real Life © **Big Ideas Learning LLC, 2022**

Supplemental Resources

- Illustrative Mathematics <u>https://www.illustrativemathematics.org/</u>
- Khan Academy https://www.khanacademy.org/
- Math for Elementary School Teachers <u>http://www.mathforelementaryteachers.org/</u>video clips that contain explanations of arithmetic topics including: Place Value/Arithmetic Models/Arithmetic Algorithms, Mental Math, Primes/Divisibility, Fraction Arithmetic, and Word Problems/Model Drawing.
- National Council of Teachers of Mathematics <u>http://www.nctm.org/</u>
- National Library of Virtual Manipulatives <u>http://nlvm.usu.edu/</u>
- NCTM Illuminations Resources for Teaching Math <u>http://illuminations.nctm.org/</u>
- Open Up Resources https://openupresources.org/

Kindergarten

Interdisciplinary Connections

Mathematics is a unified body of knowledge whose concepts build upon each other. Connecting mathematical concepts includes linking ideas to related ideas learned previously.

Major emphasis should be given to ideas and concepts across mathematical content areas that help students see that mathematics is a web of closely connected ideas. Students need to connect their mathematical learning to appropriate real-world contexts. They need to create interest and maintain the interest after the novelty of the work has worn off.

Mathematics is the language of science and is greatly utilized in industry and business. It gives us the power to solve difficult real-world problems, but also helps us to understand how the universe operates.

Every mathematics teacher needs to make students unafraid of the subject by convincing the students of the usefulness of learning mathematics in their daily lives and for higher studies. The world today, which leans more and more heavily on Science and Technology, demands more from mathematics. Tomorrow's world will, no doubt, make still greater demands from mathematics.

Interdisciplinary Connections for Kindergarten

Literature:

 \sim The Greedy Triangle, By Meghan Everette

- Introduce the lesson by reading The Greedy Triangle
- Follow the lesson in the Interdisciplinary Supplemental Section.

~ Ten Little Monkeys: Jumping on the Bed by Annie Kubler

- Introduce the lesson by reading Ten Little Monkeys: Jumping on the Bed.
- Follow the lesson in the Interdisciplinary Supplemental Section.

~ Ten Fat Turkeys

• Subtraction book used in November

~Dr. Seuss Math

• Follow the worksheets in the Interdisciplinary Supplemental Section

(NJSLSA.R1. Read closely to determine what the text says explicitly and to make logical inferences and relevant connections from it; cite specific textual evidence when writing or speaking to support conclusions drawn from the text.

RL.K.1. With prompting and support, ask and answer questions about key details in a text (e.g., who, what, where, when, why, how).)

Climate Change for Kindergarten

With the adoption of the 2020 New Jersey Student Learning Standards (NJSLS), New Jersey became the first state in the nation to include climate change across content areas. The goal of inclusion of climate change education implementation is to foster generations of New Jersey students that can analyze, question, interpret, to think independently, and bring critical deduction to fulfill, and to lead in jobs created by burgeoning industries of the future green economy.

- K.DL.A.1 Classify objects into given categories; count the numbers of objects in each category and sort the categories by count.
 - Students will be given pictures of objects and sort them into categories: Trash, Reuse and Recycle. They will then count the number of cards in each group.
- K.OA.A.2 Solve addition and subtraction word problems, and add and subtract within 10, e.g., by using objects or drawings to represent the problem.
 - Students will go outside and count the number of trees on the playground. They will represent the number of trees using counters, dots and the number.
 - Students can count trees in the front of the school, then the back of the school. They can count the total objects together to find the total trees on the school campus. Students who are able to can add the numbers together.

New Jersey Student Learning Standards (NJSLS)

In Kindergarten, instructional time should focus on two critical areas: (1) representing and comparing whole numbers, initially with sets of objects; (2) describing shapes and space. More learning time in Kindergarten should be devoted to number than to other topics.

(1) Students use numbers, including written numerals, to represent quantities and to solve quantitative problems, such as counting objects in a set; counting out a given number of objects; comparing sets or numerals; and modeling simple joining and separating situations with sets of objects, or eventually with equations such as 5 + 2 = 7 and 7 - 2 = 5. (Kindergarten students should see addition and subtraction equations, and student writing of equations in kindergarten is encouraged, but it is not required.) Students choose, combine, and apply effective strategies for answering quantitative questions, including quickly recognizing the cardinalities of small sets of objects, counting and producing sets of given sizes, counting the number of objects in combined sets, or counting the number of objects that remain in a set after some are taken away.

(2) Students describe their physical world using geometric ideas (e.g., shape, orientation, spatial relations) and vocabulary. They identify, name, and describe basic two-dimensional shapes, such as squares, triangles, circles, rectangles, and hexagons, presented in a variety of ways (e.g., with different sizes and orientations), as well as three-dimensional shapes such as cubes, cones, cylinders, and spheres. They use basic shapes and spatial reasoning to model objects in their environment and to construct more complex shapes.

Counting and Cardinality A. Know number names and the count sequence.

K.CC.A.1 Count to 100 by ones and by tens.

Math Talk

extension)

Workbook Pages ("Check for Understanding"

K.CC.A.2 Count forward beginning from a given number within the known sequence (instead of having to begin at 1).

K.CC.A.3 Write numbers from 0 to 20. Represent a number of objects with a written numeral 0-20 (with 0 representing a count of no objects).

Understandings	Essential Questions		
Students will understand			
• Counting involves one-to-one correspondence.	• Why do we need to count?		
• One can count by different amounts (ones, tens,	• How do we count?		
etc.).			
Knowledge	Skills		
Students will know	Students will be able to		
Multiples of ten	• Count to 100 by ones		
How to count	• Count to 100 by tens		
• How to write the numerals 0 – 9	• Count forward beginning from a given number within the		
Count a number of objects	known sequence		
	• Write numbers from 0-20		
	• Represent a number of objects with a written numeral 0-20		
	(with 0 representing a count of no objects)		
Standards for N	Standards for Mathematical Practice		
MP2. Reason abstractly and quantitatively. MP7. Look for and make use of structure. MP8. Look for and express regularity in repeated reasoning.			
Resources			
 Math Expressions, 2018: Lessons 1.7, 1.12, 1.13, 1.14, 1.16, 1.17, 2.1, 2.2, 2.5, 2.6, 2.7, 2.8, 2.9, 2.10, 2.11, 2.12, 2.14, 2.15, 2.16, 2.18, 2.19, 3.1, 3/2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.11, 3.12, 3.13, 3.14, 3.18, 3.19, 4.3, 4.8, 4.10, 4.12, 4.13, 4.15, 4.16, 4.17, 4.18, 4.20, 5.2, 5.3, 5.4, 5.5, 5.7, 5.8, 5.10, 5.11, 5.13, 5.14, 5.16, 5.17, 5.20, 5.23 			
Assessment			
Formative Assessment	Summative Assessment		
Do Now	• Unit Tests		
Homework	 Benchmarks (beginning, middle, end of year) 		
Puzzled Penguin			

Counting and Cardinality B. Count to tell the number of objects

K.CC.B.4 Understand the relationship between numbers and quantities to 10; connect counting to cardinality. a. When counting objects, say the number names in the standard order, pairing each object with one and only one number name and each number name with one and only one object. b. Understand that the last number name said tells the number of objects counted. The number of objects is the same regardless of their arrangement or the order in which they were counted. c. Understand that each successive number name refers to a quantity that is one larger. K.CC.B.5 Count to answer "how many?" questions about as many as 10 things arranged in a line, a rectangular array, or a circle, or as many as 5 things in a scattered configuration; given a number from 1-10, count out that many objects Understandings **Essential Questions** Students will understand... there is a relationship between the numbers and quantities. How do we count? • when counting, each object has one and only one number name and each number • name is paired with one and only one object (one-to-one correspondence). when counting, the last number name said tells the number of objects counted. • the number of objects is the same regardless of the order in which they were counted. • each successive number name refers to a quantity that is one larger. Knowledge Skills Students will know . . . Students will be able to . . . the connection between • count objects while saying the number names in the standard order. counting and cardinality. state the total number of objects in a group. • one-to-one • count as many as 20 things arranged in a line, a rectangular array, or a circle, when correspondence. asked "how many...?". count as many as 10 things in a scattered configuration, when asked "how many...?". • count out the correct number of objects when given a number from 1-20. **Standards for Mathematical Practice** MP2. Reason abstractly and quantitatively. MP7. Look for and make use of structure. MP8. Look for and express regularity in repeated reasoning. Resources Math Expressions, 2018: Lessons 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 1.11, 1.12, 1.13, 1.14, 1.15, 1.16, 1.17, 2.1, 2.2, 2.3, • 2.4, 2.5, 2.7, 2.8, 2.9, 2.10, 2.11, 2.12, 2.14, 2.15, 2.16, 2.18, 2.19, 2.20, 3.1, 3.2, 3.5, 3.7, 3.8, 3.10, 3.11, 3.12, 3.13, 3.14, 3.15, 3.18, 3.19, 3.20, 3.21, 4.1, 4.3, 4.5, 4.6, 4.7, 4.8, 4.12, 4.15, 4.16, 4.20, 5.1, 5.2, 5.3, 5.4, 5.7, 5.9, 5.14, 5.15, 5.16, 5.17, 5.19, 5.20, 5.23 Assessment Formative Assessment Summative Assessment • Do Now • Unit Tests Benchmarks (beginning, middle, end of year) Homework • **Puzzled** Penguin • Math Talk • Workbook Pages ("Check for Understanding"

extension)

Counting and Cardinality C. Compare numbers

K.CC.C.6 Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group, e.g., by using matching and counting strategies (include groups with up to ten objects).

K.CC.C.7 Compare two numbers between 1 and 10 presented as written numerals.

Understandings	Essential Questions
 Students will understand "greater than" means the amount is more; "less than" means the amount is less. a numeral stands for number of concrete objects. 	• How do we compare two numbers?
Knowledge	Skills
 Students will know matching strategies to identify the number of objects in a group of up to 10 objects. counting strategies to identify the number of objects in a group of up to 10 objects. 	 Students will be able to identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group. compare two numbers between 1 and 10 presented as written numerals.
Standards for Mathematical Practice	

MP2. Reason abstractly and quantitatively.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Lessons 1.9, 1.11, 1.12, 1.13, 1.15, 1.16, 1.17, 2.9, 3.10, 3.12, 3.14, 4.6, 4.10, 5.10, 5.16, 5.17, 5.20

Assessment	
Formative Assessment	Summative Assessment
Do Now	Unit Tests
Homework	• Benchmarks (beginning, middle, end of year)
Puzzled Penguin	
Math Talk	
Workbook Pages ("Check for Understanding"	
extension)	

Operations and Algebraic Thinking A. Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

K.OA.A.1 Represent addition and subtraction up to 10 with objects, fingers, mental images, drawings, sounds (e.g., claps), acting out situations, verbal explanations, expressions, or equations.

K.OA.A.2 Solve addition and subtraction word problems, and add and subtract within 10, e.g., by using objects or drawings to represent the problem. **2**

K.OA.A.3 Decompose numbers less than or equal to 10 into pairs in more than one way, e.g., by using objects or drawings, and record each decomposition by a drawing or equation (e.g., 5 = 2 + 3 and 5 = 4 + 1).

K.OA.A.4 For any number from 1 to 9, find the number that makes 10 when added to the given number, e.g., by using objects or drawings, and record the answer with a drawing or equation.

Understandings	Essential Questions
 Students will understand numbers can be decomposed. making a sum of 10 will be important to make work easier. objects, mental images, drawings, sounds, acting out situations, verbal explanations, expressions, or equations can help one understand problems and find solutions. 	 Why do we need to add and subtract? What happens when we put groups together or add to a group? What happens when we take apart groups or take away from a group?
Knowledge	Skills
 Students will know addition and subtraction can be represented in multiple ways. numbers can be decomposed. 	 Students will be able to represent addition and subtraction with objects, mental images, drawings, sounds, acting out situations, verbal explanations, expressions, or equations. solve addition and subtraction word problems. add and subtract within 10. decompose numbers less than or equal to 10 into pairs in more than one way by using objects or drawings. record decompositions of numbers by a drawing or equation (5 = 4 + 1). find the number that makes 10 when added to a given number, for any number 1-9, by using objects or drawings and record the answer with a drawing or an equation. fluently add and subtract within 5.

K.OA.A.5 Demonstrate accuracy and efficiency for addition and subtraction within 5.

Standards for Mathematical Practice

MP1. Make sense of problems and persevere in solving them.

MP2. Reason abstractly and quantitatively.

MP4. Model with mathematics.

MP5. Use appropriate tools strategically.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

Math Expressions, 2018: Lessons 1.6, 1.7, 1.8, 1.14, 1.21, 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.9, 2.10, 2.11, 2.12, 2.14, 2.15, 2.16, 2.19, 2.20, 3.1, 3.3, 3.4, 3.5, 3.6, 3.7, 3.11, 3.12, 3.14, 3.15, 3.16, 3.17, 3.18, 3.19, 3.20, 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.8, 4.10, 4.11, 4.12, 4.13, 4.15, 4.16, 4.17, 4.18, 4.19, 4.20, 5.1, 5.2, 5.3, 5.4, 5.5, 5.6, 5.7, 5.8, 5.9, 5.10, 5.11, 5.12, 5.13, 5.14, 5.15, 5.16, 5.18, 5.19

Assessment	
Formative Assessment	Summative Assessment
Do Now	Unit Tests
Homework	• Benchmarks (beginning, middle, end of year)
Puzzled Penguin	
Math Talk	
• Workbook Pages ("Check for Understanding"	
extension)	

Numbers and Operation in Base 10 A. Work with numbers 11-19 to gain foundations for place value.

K.NBT.A.1 Compose and decompose numbers from 11 to 19 into ten ones and some further ones, e.g., by using objects or drawings, and record each composition or decomposition by a drawing or equation (e.g., 18 = 10 + 8); understand that these numbers are composed of ten ones and one, two, three, four, five, six, seven, eight, or nine ones.

Understandings	Essential Questions
 Students will understand teen numbers (11-19) are composed of ten ones and one, two, three, four, five, six, seven, eight, or nine ones. 	• Why do we compose and decompose numbers?
Knowledge	Skills
 Students will know composing and decomposing numbers into tens and ones will help solve problems 	 Students will be able to compose and decompose numbers from 11-19 into ten ones and some further ones, by using objects or drawings. record compositions and decompositions with drawings or equations.
Standards for Mathematical Practice	

MP1. Make sense of problems and persevere in solving them.

MP2. Reason abstractly and quantitatively.

MP4. Model with mathematics.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

Math Expressions, 2018: Lessons 3.2, 3.3, 3.5, 3.6, 3.8, 3.13, 3.15, 3.16, 3.17, 3.18, 3.19, 3.20, 4.3, 4.5, 4.7, 4.12, 4.16, 4.18, 4.20, 5.1, 5.3, 5.4, 5.5, 5.6, 5.7, 5.9, 5.10, 5.15, 5.17, 5.18, 5.19, 5.20, 5.23

Assessment	
Formative Assessment	Summative Assessment
Do Now	Unit Tests
Homework	• Benchmarks (beginning, middle, end of year)
Puzzled Penguin	
Math Talk	
Workbook Pages ("Check for Understanding"	
extension)	

Measurement A. Describe and compare measurable attributes.

K.M.A.1 Describe measurable attributes of objects, such as length or weight. Describe several measurable attributes of a single object.

K.M.A.2 Directly compare two objects with a measurable attribute in common, to see which object has "more of"/"less of" the attribute, and describe the difference. For example, directly compare the heights of two children and describe one child as taller/shorter.

Understandings	Essential Questions
 Students will understand measurable attributes are a way to compare objects. an object may have multiple measurable attributes. multiple objects may have the same measurable attribute. 	Why do we need to measure objects?What attributes are measurable?How do we compare objects?
Knowledge	Skills
the potential attributes are measurable.words that compare attributes.	 Students will be able to describe measurable attributes of objects, such as length or weight. describe several measurable attributes of a single object. directly compare two objects with a measurable attribute in common to determine which has "more of"/"less of" the attribute, e.g. heights of two children. describe the difference between two objects with the common attribute that was compared, one child is taller/shorter than the other child.
Standards for M	athematical Practice
MP6. Attend to precision. MP7. Look for and make use of structure.	
Math Expressions, 2018: Lessons 5.21, 5.22, 5.23	
	essment
 Formative Assessment Do Now Homework Puzzled Penguin Math Talk Workbook Pages ("Check for Understanding" 	 Summative Assessment Unit Tests Benchmarks (beginning, middle, end of year)

extension)

Measurement B. Work with money.

K.M.B.3 Understand that certain objects are coins and dollar bills, and that coins and dollar bills represent money. Identify the values of all U.S. coins and the one-dollar bill.

Understandings	Essential Questions	
 Students will understand different coins have unique values. the relative sizes of the coins are not related to the relative values of the coins (i.e., a penny is larger than a dime but it is not worth more than a dime.) some coins can be exchanged for other coins, e.g., 5 pennies can be exchanged for 1 nickel. the value of some coins and bills can be represented by a combination of other coins. money amounts can be counted and compared. coins can be identified by their color, size, and edge. 	 Why do we need money? How do we count money? 	
Knowledge	Skills	
 Students will know pennies are copper and nickels, dimes, and quarters are silver. a nickel is bigger than a dime but smaller than a quarter. pennies and nickels have a smooth edge while dimes and quarters have an edge with ridges. 	 Students will be able to identify a penny, nickel, dime, and quarter. sort coins. identify the value of a penny, nickel, dime, and quarter. skip count to count one type of coin, e.g., 10, 20, 30 for dimes. 	
MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reas MP4. Model with mathematics.	oning of others.	
Re	sources	
• Done in morning routines.		
Assessment		
 Formative Assessment Do Now Homework Puzzled Penguin Math Talk Workbook Pages ("Check for Understanding" extension) 	 Summative Assessment Unit Tests Benchmarks (beginning, middle, end of year) 	

Data Literacy

A. Classify objects and count the number of objects in each category.

K.DL.A.1 Classify objects into given categories; count the numbers of objects in each category and sort the categories by count. (Clarification: *Limit category counts to be less than or equal to 10.)*

Understandings	Essential Questions
 Students will understand classifying objects helps to count total numbers. objects can be described by their attributes. objects can be sorted by their attributes. 	Why do we need to classify objects?How does sorting help us to count?
Knowledge	Skills
 Students will know attributes that can be used to sort or classify objects. 	 Students will be able to classify objects into given categories. count the number of objects in a category (counts less than or equal to 10). sort the categories by count.
Standards for Mathematical Practice	
MP2. Reason abstractly and quantitatively.	

MP7. Look for and make use of structure.

Resources

• Math Expressions, 2018: Lessons 1.10, 2.13, 2.17, 2.20, 3.10, 3.12, 3.21, 4.1, 4.9, 4.22

Assessment

1 LSSUSSMENT	
Formative Assessment	Summative Assessment
Do Now	Unit Tests
Homework	• Benchmarks (beginning, middle, end of year)
Puzzled Penguin	
Math Talk	
Workbook Pages ("Check for Understanding"	
extension)	

Geometry A. Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cylinders, and spheres).

K.G.A.1 Describe objects in the environment using names of shapes, and describe the relative positions of these objects using terms such as *above, below, beside, in front of, behind, and next to*.

K.G.A.2 Correctly name shapes regardless of their orientations or overall size.

K.G.A.3 Identify shapes as two-dimensional (lying in a plane, "flat") or three-dimensional ("solid").

Understandings	Essential Questions
 Students will understand shapes have positions in the world relative to other things. characteristics of shapes give it a name. 	 What characteristics of a shape help us to name it? How does knowing the name of shapes help us? Why do we need to know positions of shapes?
Knowledge	Skills
 Students will know the characteristics of a square, circle, triangle, rectangle, hexagon, cube, cylinder, and sphere. the meaning of the words above, below, beside, in front of, behind, and next to. 	 Students will be able to Describe objects in the environment using names of shapes. Describe the relative positions of these objects using terms such as <i>above, below, beside, in front of, behind, and next to.</i>

Standards for Mathematical Practice

MP7. Look for and make use of structure.

Resources

• Math Expressions, 2018: Lessons 1.8, 1.10, 1.18, 2.13, 2.17, 2.20, 3.10, 3.12, 3.21, 4.9, 4.14, 4.21, 4.22

Assessment		
Formative Assessment	Summative Assessment	
• Do Now	Unit Tests	
Homework	• Benchmarks (beginning, middle, end of year)	
Puzzled Penguin		
Math Talk		
• Workbook Pages ("Check for Understanding"		
extension)		

Geometry

B. Analyze, compare, create, and compose shapes.

K.G.B.4 Analyze and compare two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g., number of sides and vertices/"corners") and other attributes (e.g., having sides of equal length).

K.G.B.5 Model shapes in the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes. **2**

K.G.B.6 Compose simple shapes to form larger shapes. For example, "*Can you join these two triangles with full sides touching to make a rectangle?*"

Understandings	Essential Questions
 Students will understand shapes in the world can be built with components such as sticks and clay balls. shapes in the world can be drawn. shapes can be formed by composing other shapes. 	Why do we need to identify shapes?Why would we compose shapes?
Knowledge	Skills
 Students will know the characteristics of a square, circle, triangle, rectangle, hexagon, cube, cylinder, and sphere. components/representations that can be used to model shapes in the world. 	 Students will be able to analyze two- and three-dimensional shapes, using informal language. compare two- and three-dimensional shapes, using informal language. model shapes in the world by building shapes from components and drawing shapes.

Standards for Mathematical Practice

MP1. Make sense of problems and persevere in solving them.

MP4. Model with mathematics.

MP7. Look for and make use of structure.

Resources

• Math Expressions, 2018: Lessons 1.8, 1.10, 1.18, 2.13, 2.17, 3.9, 3.21, 4.9, 4.14, 4.21, 4.22

Assessment		
Formative Assessment	Summative Assessment	
Do Now	• Unit Tests	
Homework	• Benchmarks (beginning, middle, end of year)	
Puzzled Penguin		
Math Talk		
• Workbook Pages ("Check for Understanding"		
extension)		

Additional Lesson for Kindergarten: Measurement

This money cluster was moved to the Measurement domain

Although not required in the standards, students need to be exposed to additional topics in order to prepare for what is required in future grades. These topics in Kindergarten include **MONEY**, time, and patterns.

Understandings	Essential Questions
Students will understand	
• different coins have unique values.	• Why do we need money?
• the relative sizes of the coins are not related to the relative values of the coins (i.e., a penny is larger than a dime but it is not worth more than a dime.)	• How do we count money?
• some coins can be exchanged for other coins, e.g., 5 pennies can be exchanged for 1 nickel.	
• the value of some coins and bills can be represented by a combination of other coins.	
• money amounts can be counted and compared.	
• coins can be identified by their color, size, and	
edge.	
Knowledge	Skills
Students will know	Students will be able to
• pennies are copper and nickels, dimes, and	• identify a penny, nickel, dime, and quarter.
quarters are silver.	• sort coins.
• a nickel is bigger than a dime but smaller	• identify the value of a penny, nickel, dime, and
than a quarter.	quarter.
• pennies and nickels have a smooth edge while dimes and quarters have an edge with ridges.	• skip count to count one type of coin, e.g., 10, 20, 30 for dimes.
Resources	
• Done in morning routines.	

Additional Lesson for Kindergarten: Measurement

Although not required in the standards, students need to be exposed to additional topics in order to prepare for what is required in future grades. These topics in Kindergarten include money, **TIME**, and patterns.

Understandings	Essential Questions	
 Students will understand some activities take more time than others to complete. a day has three parts that we discuss: morning, afternoon, and evening. when time passes, the hour hand and the minute hand move at different rates. the hour hand represents the approximate time of the day, the minute hand gives a more exact time. 	 Why do we need clocks? What are the different types of clocks? How do we tell time? 	
events happen in order- we use terms such as first, next, and last. Knowledge	Skills	
 Students will know there are two cycles to the passage of time, 12:00 through 11:59, during the 24 hours of a day. the hour hand must be pointing at the number exactly for it to be "o'clock." 	 Students will be able to identify the part of day, morning, afternoon, evening. recognize the numbers 1-12 on the face of a clock. tell time to the hour WITH THE HOUR HAND ONLY. 	
Resources		
Done in morning routines.		

Additional Lesson for Kindergarten: Algebraic Thinking

Although not required in the standards, students need to be exposed to additional topics in order to prepare for what is required in future grades. These topics in Kindergarten include money, time, and **PATTERNS**.

Understandings	Essential Questions
Students will understand	
• the same set of objects can be used to create	• Why do we need to identify patterns?
different patterns.	• How do we recognize a pattern?
• some patterns are made up of units that repeat.	
• some patterns can be identified by type, e.g.,	
ABABAB.	
• many things can be used to create patterns, e.g.,	
shapes, colors, sounds, letters, and objects.	
Knowledge	Skills
Students will know	Students will be able to
• some common patterns types, e.g.	• recognize patterns.
ABABAB; clap, clap, stomp, clap, clap,	• create patterns.
stomp	• extend a given pattern.
Re	esources
Dong in morning routings	
Done in morning routines.	

Career Readiness, Life Literacies, and Key Skills

Career Readiness, Life Literacies, and Key Skills

Rapid advancements in technology and subsequent changes in the economy have created opportunities for individuals to compete and connect on a global scale. In this increasingly diverse and complex world, the successful entrepreneur or employee must not only possess the requisite education for specific industry pathways but also employability skills necessary to collaborate with others and manage Resources effectively in order to establish and maintain stability and independence. This document outlines concepts and skills necessary for New Jersey's students to thrive in an ever-changing world. Intended for integration throughout all K–12 academic and technical content areas, the New Jersey Student Learning Standards- Career Readiness, Life Literacies, and Key Skills (NJSLS-CLKS) provides the framework for students to learn the concepts, skills, and practices essential to the successful navigation of career exploration and preparation, personal finances and digital literacy.

Mission

Career readiness, life literacies, and key skills education provides students with the necessary skills to make informed career and financial decisions, engage as responsible community members in a digital society, and to successfully meet the challenges and opportunities in an interconnected global economy.

Vision

An education in career readiness, life literacies, and key skills fosters a population that:

•Continually self-reflects and seeks to improve the essential life and career practices that lead to success;

•Uses effective communication and collaboration skills and Resources to interact with a global society;

•Possesses financial literacy and responsibility at home and in the broader community;

•Plans, executes, and alters career goals in response to changing societal and economic conditions; and •Seeks to attain skill and content mastery to achieve success in a chosen career path.

Career Readiness, Life Literacies, and Key Skills

- 9.1.2. FI.1: Differentiate the various forms of money and how they are used (e.g., coins, bills, checks, debit and credit cards).
- 9.1.2.FP.2: Differentiate between financial wants and needs.
- **9.1.2.FP.3:** Identify the factors that influence people to spend or save (e.g., commercials, family, culture, society).
- 9.1.2.PB.2: Explain why an individual would choose to save money.
- **9.4.2.CI.1**: Demonstrate openness to new ideas and perspectives (e.g., 1.1.2.CR1a, 2.1.2.EH.1, 6.1.2.CivicsCM.2).
- 9.4.2.CI.2: Demonstrate originality and inventiveness in work (e.g., 1.3A.2CR1a).
- **9.4.2.CT.1:** Gather information about an issue, such as climate change, and collaboratively brainstorm ways to solve the problem (e.g., K-2-ETS1-1, 6.3.2.GeoGI.2).
- 9.4.2.CT.2: Identify possible approaches and Resources to execute a plan (e.g., 1.2.2.CR1b, 8.2.2.ED.3).
- 9.4.2.CT.3: Use a variety of types of thinking to solve problems (e.g., inductive, deductive).
- **9.4.2.DC.3:** Explain how to be safe online and follow safe practices when using the internet (e.g., 8.1.2.NI.3, 8.1.2.NI.4).
- 9.4.2.DC.6: Identify respectful and responsible ways to communicate in digital environments.
- 9.4.2.IML.2: Represent data in a visual format to tell a story about the data (e.g., 2.MD.D.10)

Computer Science and Design Thinking

Computer Science and Design Thinking

New approaches necessary for solving the critical challenges that we face as a society will require harnessing the power of technology and computing. Rapidly changing technologies and the proliferation of digital information have permeated and radically transformed learning, working, and everyday life. To be well-educated, global-minded individuals in a computing-intensive world, students must have a clear understanding of the concepts and practices of computer science. As education systems adapt to a vision of students who are not just computer users but also computationally literate creators who are proficient in the concepts and practices of computer science and design thinking, engaging students in computational thinking and human-centered approaches to design through the study of computer science and technology serves to prepare students to ethically produce and critically consume technology.

Mission

Computer science and design thinking education prepares students to succeed in today's knowledge-based economy by providing equitable and expanded access to high-quality, standards-based computer science and technological design education.

Vision

All students have equitable access to a rigorous computer science and design thinking education. Students will benefit from opportunities to engage in high-quality technology programs that foster their ability to: • develop and apply computational and design thinking to address real-world problems and design creative solutions;

• engage as collaborators, innovators, and entrepreneurs on a clear pathway to success through postsecondary education and careers;

• navigate the dynamic digital landscape to become healthy, productive, 21st century global-minded individuals; and

• participate in an inclusive and diverse computing culture that appreciates and incorporates perspectives from people of different genders, ethnicities, and abilities.

COMPUTER SCIENCE AND DESIGN THINKING

- **8.1.2.CS.1:** Select and operate computing devices that perform a variety of tasks accurately and quickly based on user needs and preferences.
- **8.1.2.AP.1:** Model daily processes by creating and following algorithms to complete tasks.
- **8.1.2.AP.4:** Break down a task into a sequence of steps.
- **8.1.2.AP.5:** Describe a program's sequence of events, goals, and expected outcomes.
- **8.1.2.AP.6:** Debug errors in an algorithm or program that includes sequences and simple loops.
- **8.1.2.DA.1:** Collect and present data, including climate change, in various visual formats.
- **8.1.2.DA.3:** Identify and describe patterns in data visualizations.
- **8.1.2.DA.4:** Make predictions based on data using charts or graphs.
- **8.2.2.ED.1:** Communicate the function of a product or device.
- **8.2.2.ITH.4:** Identify how various tools reduce work and improve daily tasks.
- **8.2.2.NT.2:** Brainstorm how to build a product, improve a designed product, fix a product that has stopped working, or solve a simple problem.

Differentiation Strategies

Students with Disabilities/ Students at Risk of School Failure

(For students with disabilities, appropriate accommodations, instructional adaptations, and/or modifications should be determined by the IEP or 504 team)

Modifications for Classroom

- Pair visual prompts with verbal presentations
- Ask students to restate information, directions, and assignments.
- Give repetition and practice exercises
- Model skills/techniques to be mastered
- Give extended time to complete class work
- Provide copy of class notes
- Determine if preferential seating would be beneficial
- Provide access to a computer
- Provide copies of textbooks for home
- Provide access to books on tape/CD/digital media, as available and appropriate
- Assign a peer helper in the class setting
- Provide oral reminders and check student work during independent work time
- Assist student with long- and short-term planning of assignments
- Encourage student to proofread assignments and tests
- Provide regular parent/school communication

Modifications for Homework and Assignments

- Provide extended time to complete assignments
- Break down assignments
- Provide the student with clearly stated (written) expectations and grading criteria for assignments
- Implement RAFT activities as they pertain to the types/modes of communication (role, audience, format, topic)

Modifications for Assessments

- Provide extended time on classroom tests and quizzes
- Provide alternate setting as needed
- Restate, reread, and clarify directions/questions
- Distribute study guide for classroom tests
- Establish procedures for accommodations /modifications for assessments

Differentiation Strategies

Gifted and Talented

(content, process, product and learning environment)

- Allow students to pursue independent projects based on their individual interests
- Provide enrichment activities that include more advanced material
- Allow team-teaching opportunities and collaboration
- Set individual goals
- Conduct research and provide presentation of appropriate topics
- Design surveys to generate and analyze data to be used in discussion.
- Use Higher-Level Questioning Techniques
- Provide assessments at a higher level of thinking

English Language Learners

Modifications for Classroom

- Pair visual prompts with verbal presentations
- Provide repetition and practice
- Model skills/techniques to be mastered

Modifications for Homework/Assignments

- Provide Native Language Translation (peer, online assistive technology, translation device, bilingual dictionary)
- Provide extended time for assignment completion as needed
- Highlight key vocabulary
- Use graphic organizers

First Grade

Interdisciplinary Connections

Mathematics is a unified body of knowledge whose concepts build upon each other. Connecting mathematical concepts includes linking ideas to related ideas learned previously.

Major emphasis should be given to ideas and concepts across mathematical content areas that help students see that mathematics is a web of closely connected ideas. Students need to connect their mathematical learning to appropriate real-world contexts. They need to create interest and maintain the interest after the novelty of the work has worn off.

Mathematics is the language of science and is greatly utilized in industry and business. It gives us the power to solve difficult real-world problems, but also helps us to understand how the universe operates.

Every mathematics teacher needs to make students unafraid of the subject by convincing the students of the usefulness of learning mathematics in their daily lives and for higher studies. The world today, which leans more and more heavily on Science and Technology, demands more from mathematics. Tomorrow's world will, no doubt, make still greater demands from mathematics.

Interdisciplinary Connections for Grade 1

"Pumpkin Math"

~Introduce with How Many Seeds in a Pumpkin (skills covered- skip counting, addition, estimating) -

- ~Pumpkin Packet
 - Record Estimate & Actual
 - Weight
 - Inches around
 - Number of Seeds
 - Sink or Float
 - Describing Words (adjectives)
 - Illustration

"10 Fat Turkeys"

~Introduce with 10 Fat Turkeys (skills covered- counting forward & backward, complements of 10)

~Record Complements of 10 on individual feathers (reference illustrations- How many turkeys are on the fence? (6) How many are off? (4) What do you know about 6 and 4? (=10)

~Create "This turkey is a 10!" project with feathers and other copy patterns

"Seeing Double"

~Read Two of Everything

~Comprehension Questions

- What was special about the pot that Mr. Haktak found? (everything he put in was doubled)
- What happened when Mr. Haktak fell into the pot? (2 Mr. Haktak's came out)
- What happened when Mr. & Mrs. Haktak put 5 coins in? (10 came out)
- After understanding is confirmed, write equations to show what happened in the text (1+1=2, 5+5=10)

~Introduce "doubling machine" (mirror) and model & play "Seeing Double" activity

~After students have rolled die and held that number of items in the mirror the see it doubled, they can write one equation and create a drawing representation on the "Doubling Pot" activity sheet.

~Present work & display class book

"Lifetime: The Amazing Numbers in Animal Lives"

 \sim The story is set up in a style where every page states something along the lines of, "In one lifetime caribou grow and shed 10 sets of antlers."

~Note that each illustration matches the numbers stated in the text.

(NJSLSA.R1. Read closely to determine what the text says explicitly and to make logical inferences and relevant connections from it; cite specific textual evidence when writing or speaking to support conclusions drawn from the text.

RL.1.1. Ask and answer questions about key details in a text.)

Climate Change for Grade 1

With the adoption of the 2020 New Jersey Student Learning Standards (NJSLS), New Jersey became the first state in the nation to include climate change across content areas. The goal of inclusion of climate change education implementation is to foster generations of New Jersey students that can analyze, question, interpret, to think independently, and bring critical deduction to fulfill, and to lead in jobs created by burgeoning industries of the future green economy.

- 1.OA.A.1 Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.
 - Students will play a card game in which they will read energy usage situations and either receive a lightbulb or lose a lightbulb. At the end of 4 rounds, the student with the most lightbulbs wins.
- 1.DL.A.1 Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.
 - Students will sort objects into different categories (Recycle, Compost, Trash). They will then graph their results and answer questions about their data.

New Jersey Student Learning Standards (NJSLS)

In Grade 1, instructional time should focus on four critical areas: (1) developing understanding of addition, subtraction, and strategies for addition and subtraction within 20; (2) developing understanding of whole number relationships and place value, including grouping in tens and ones; (3) developing understanding of linear measurement and measuring lengths as iterating length units; and (4) reasoning about attributes of, and composing and decomposing geometric shapes.

(1) Students develop strategies for adding and subtracting whole numbers based on their prior work with small numbers. They use a variety of models, including discrete objects and length-based models (e.g., cubes connected to form lengths), to model add-to, take-from, put-together, take apart, and compare situations to develop meaning for the operations of addition and subtraction, and to develop strategies to solve arithmetic problems with these operations. Students understand connections between counting and addition and subtraction (e.g., adding two is the same as counting on two). They use properties of addition to add whole numbers and to create and use increasingly sophisticated strategies based on these properties (e.g., "making tens") to solve addition and subtraction go the relationship between addition and subtraction.

(2) Students develop, discuss, and use efficient, accurate, and generalizable methods to add within 100 and subtract multiples of 10. They compare whole numbers (at least to 100) to develop understanding of and solve problems involving their relative sizes. They think of whole numbers between 10 and 100 in terms of tens and ones (especially recognizing the numbers 11 to 19 as composed of a ten and some ones). Through activities that build number sense, they understand the order of the counting numbers and their relative magnitudes.

(3) Students develop an understanding of the meaning and processes of measurement, including underlying concepts such as iterating (the mental activity of building up the length of an object 1 with equal-sized units) and the transitivity principle for indirect measurement. *

(4) Students compose and decompose plane or solid figures (e.g., put two triangles together to make a quadrilateral) and build understanding of part-whole relationships as well as the properties of the original and composite shapes. As they combine shapes, they recognize them from different perspectives and orientations, describe their geometric attributes, and determine how they are alike and different, to develop the background for measurement and for initial understandings of properties such as congruence and symmetry.

*Students should apply the principle of transitivity of measurement to make indirect comparisons, but they need not use this technical term.

Operations and Algebraic Thinking A. Represent and solve problems involving addition and subtraction.

1.OA.A.1 Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

1.OA.A.2 Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

problem. 🜌			
	nderstandings		Essential Questions
 Students will understand addition involves adding to and putting together. subtraction involves taking from, taking apart, and comparing. missing numbers in a math sentence can be found using addition and subtraction. a symbol can represent an unknown. 			 How can one find the total of parts? How can one find the missing part of a whole?
	quations can be used to solve	problems.	
Knowledge		S	kills
 Students will know the meaning of addition. the meaning of subtraction. there are multiple interpretations of addition and subtraction. 	 Students will be able to add on to a group in order to find a total amount. solve problems as part-part-whole problems when joining or putting them together. use subtraction to determine how many more are in one group than another (comparing). solve word problems that call for the addition of three whole numbers whose sum is less than 20. use objects and drawings to represent problems. use equations with a symbol for the unknown number to represent the problem. 		
	Standards for Matl	nematical	Practice
MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP5. Use appropriate tools strategically. MP8. Look for and express regularity in repeated reasoning.			
Life of Look for and express	Resou	•	
Kesources • Math Expressions, 2018: Lessons 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 2.1, 2.2, 2.3, 2.4, 2.10, 2.11, 2.12, 2.13, 2.14, 2.15, 2.16, 3.2, 3.4, 3.5, 3.6, 3.7, 3.8, 3.9, 3,10, 3.11, 3.12, 4.5, 5.1, 5.2, 5.3, 5.4, 5.5, 5.6, 5.11, 6.1, 6.2, 6.3, 6.4, 6.5, 6.6, 6.7, 6.8, 6.9			
Assessment			
Formative Assessment Do Now Homework Puzzled Penguin Math Talk			Assessment t Tests chmarks (beginning, middle, end of year)

Operations and Algebraic Thinking

B. Understand and apply properties of operations and the relationship between addition and subtraction.

1.OA.B.3 Apply properties of operations as strategies to add and subtract. *Examples:* If 8 + 3 = 11 is known, then 3 + 8 = 11 is also known. (Commutative property of addition.) To add 2 + 6 + 4, the second two numbers can be added to make a ten, so 2 + 6 + 4 = 2 + 10 = 12. (Associative property of addition.) (Students need not use formal terms for these properties.)

1.OA.B.4 Understand subtraction as an unknown-addend problem. For example, subtract 10 - 8 by finding the number that makes 10 when added to 8. Add and subtract within 20.

Understandings	Essential Questions
 Students will understand properties of operations are used as strategies for solving addition and subtraction problems. knowing how addition and subtraction are related helps us to solve math problems. 	 What is the relationship between addition and subtraction? How can properties of operations help to solve addition and subtraction problems?
Knowledge	Skills
Students will know	Students will be able to
• the properties of operations (but will not use formal terms for these properties.)	 apply the properties of operations to solve problems involving addition and subtraction. solve a subtraction problem by making it an unknown- addend problem.
Standards for Mathematical Practice	

MP2. Reason abstractly and quantitatively.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Lessons 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.7, 3.6, 3.7, 3.8, 3.9, 3.10, 3.12, 4.5, 5.1, 5.2, 5.5, 5.6

Assessment	
Formative Assessment	Summative Assessment
• Do Now	Unit Tests
Homework	• Benchmarks (beginning, middle, end of year)
Puzzled Penguin	
Math Talk	

Operations and Algebraic Thinking C. Add and subtract within 20.

1.OA.C.5 Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

1.OA.C.6 Add and subtract within 20, demonstrating **accuracy and fluency** for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14); decomposing a number leading to a ten (e.g., 13 - 4 = 13 - 3 - 1 = 10 - 1 = 9); using the relationship between addition and subtraction (e.g., knowing that 8 + 4 = 12, one knows 12 - 8 = 4); and creating equivalent but easier or known sums (e.g., adding 6 + 7 by creating the known equivalent 6 + 6 + 1 = 12 + 1 = 13).

+6+1=12+1=13).		
Understandings	Essential Questions	
Students will understand		
• there are multiple strategies to add and subtract.	• How is counting related to addition and subtraction?	
• counting is related to addition and subtraction.	• How can a problem be simplified?	
• how many or how much there is of something	• What strategies are available to determine how much	
increases with addition and decreases with	or how many we have?	
subtraction.		
Knowledge	Skills	
Students will know	Students will be able to	
• numbers that make 10 will help solve problems.	• add within 20.	
• numbers can be decomposed into simpler	• subtract within 20.	
terms.	• fluently add within 10.	
• counting on strategies.	• fluently subtract within 10.	
• "making 10" strategies.	• count on to add.	
• "decomposing 10" strategies.	• decompose a number leading to 10.	
• the inverse relationship between addition and		
subtraction.		
• solutions can be found by forming equivalent		
but easier or known sums.		
Standards for Mathematical Practice		
MP2. Reason abstractly and quantitatively.		
MP7. Look for and make use of structure.		
MP8. Look for and express regularity in repeated reas	oning.	
Resources		
• Math Expressions, 2018: Lessons 1.1, 1.2, 1.3, 1.4	4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.1, 2.2, 2.3, 2.5, 2.6, 2.7, 2.8, 2.9,	
2.10, 2.11, 2.12, 2.14, 2.15, 2.16, 3.1, 3.3, 3.4, 3.5	5, 3.6, 3.7, 3.10, 3.11, 3.12, 4.1, 4.4, 4.5, 4.6, 4.7, 4.10,	
4.11, 4.15, 4.16, 5.1, 5.2, 5.3, 5.4, 5.5, 5.10, 5.11,		
, , , , , , , , , , , , , , , , , , , ,		
Ass	essment	
Formative Assessment	Summative Assessment	
• Do Now	• Unit Tests	
• Homework	• Benchmarks (beginning, middle, end of year)	
Puzzled Penguin		

• Math Talk

Operations and Algebraic Thinking D. Work with addition and subtraction equations.

1.OA.D.7 Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? 6 = 6, 7 = 8 - 1, 5 + 2 = 2 + 5, 4 + 1 = 5 + 2.

1.OA.D.8 Determine the unknown whole number in an addition or subtraction equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations 8 + ? = 11, 5 = -3, 6 + 6 = -3.

Understandings	Essential Questions
 Students will understand the equal sign represents two sides that are balanced and have equivalent expressions on each side. an equation is true if the representation on the left side of the equal sign is equivalent to the representation on the right side of the equal sign; otherwise it is false. if an unknown number must be found, it must make the equation true. 	 How can one determine if an equation is true or false? When the unknown number is found for an equation, how can one tell if it is correct?
Knowledge	Skills
Students will know	Students will be able to
 an equation is true only if the left and right sides of an equal sign have equivalent expressions. that an unknown represents a number that will make an equation true. 	 determine if an equation is true or false. determine the value of an unknown which will make the equation true. relate three numbers to each other through the use of an equation.

Standards for Mathematical Practice

MP2. Reason abstractly and quantitatively.

MP3. Construct viable arguments and critique the reasoning of others.

MP6. Attend to precision.

MP7. Look for and make use of structure.

Resources

Math Expressions, 2018: Lessons 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8, 2.9, 2.10, 2.11, 2.12, 2.13, 2.16, 3.3, 3.4, 3.6, 3.7, 3.9, 3.11, 3.12, 4.4, 4.5, 4.10, 4.11, 5.1, 5.2, 5.3, 5.4, 5.5

Assessment		
Formative Assessment	Summative Assessment	
Do Now	Unit Tests	
Homework	• Benchmarks (beginning, middle, end of year)	
Puzzled Penguin		
Math Talk		

Number and Operations in Base Ten A. Extend the counting sequence.

1.NBT.A.1 Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral.

Understandings	Essential Questions
Students will understand • counting involves patterns.	 How does where the digits are located affect how one reads the number? How do counting patterns help one to count?
Knowledge	Skills
 Students will know counting patterns. how to read a number in the hundreds, tens, and ones place (for example, in 88 the 8 in the tens place is read as eighty whereas the 8 in the ones place is read as eight.) 	 Students will be able to count to 120, starting at any number less than 120. read numerals from 0 to 120. write numerals from 0 to 120. represent a number of objects with a written numeral, up to 120.
Standards for Mathematical Practice	
MP2. Reason abstractly and quantitatively.	

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Lessons 4.1, 4.2, 4.7, 4.8, 4.9, 4.10, 4.11, 4.15, 4.16, 4.18, 5.7, 5.8, 5.9

Assessment	
Formative Assessment • Do Now • Homework • Puzzled Penguin • Math Talk	 Summative Assessment Unit Tests Benchmarks (beginning, middle, end of year)

Number and Operations in Base Ten B. Understand place value.

1.NBT.B.2 Understand that the two digits of a two-digit number represent amounts of tens and ones. Understand the following as special cases:

a. 10 can be thought of as a bundle of ten ones — called a "ten."

b. The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight, or nine ones.

c. The numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones).

1.NBT.B.3 Compare two two-digit numbers based on meanings of the tens and ones digits, recording the results of comparisons with the symbols >, =, and <.

Understandings	Essential Questions
 Students will understand the location of digits in a number determines the value of the number. to compare two numbers, one must compare the digits 	• Why is place value important?
Knowledge	Skills
 Students will know the representation of 1 – 9 as ones; 11 – 19 as a composition of one ten plus ones. the two digits in a two-digit number represent the amount of tens and ones. the numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones). 	 Students will be able to identify ten as ten ones bundled. identify tens and ones in a two-digit number. compare two digit numbers using <, =, and >.

Standards for Mathematical Practice

MP2. Reason abstractly and quantitatively.

MP6. Attend to precision.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: 4.1, 4.2, 4.3, 4.4, 4.5, 4.7, 4.8, 4.9, 4.10, 4.11, 4.12, 4.13, 4.14, 4.16, 4.17, 4.18, 5.7, 5.8, 5.9, 5.10

Assessment	
Formative Assessment	Summative Assessment
Do Now	• Unit Tests
Homework	• Benchmarks (beginning, middle, end of year)
Puzzled Penguin	
Math Talk	

Number and Operations in Base Ten C. Use place value understanding and properties of operations to add and subtract.

1.NBT.C.4 Add within 100, including adding a two-digit number and a one-digit number, and adding a two-digit number and a multiple of 10, using concrete models (e.g., base-ten blocks) or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used. Understand that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten.

1.NBT.C.5 Given a two-digit number, mentally find 10 more or 10 less than the number, without having to count; explain the reasoning used.

1.NBT.C.6 Subtract multiples of 10 in the range 10-90 from multiples of 10 in the range 10-90 (positive or zero differences), using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

	Understandings		Essential Questions
 properties of operation and subtraction can h when adding two-dig ones; and sometimes 	 wings, strategies based on plac ons, and/or the relationship bet elp one solve problems. it numbers, one adds tens and it is necessary to compose a te ltiples of 10 from multiples of	e value, answers veen addition problem ens, ones and n.	bes place value help one find the s to addition and subtraction
Knowledge		Skills	
 Students will know properties of operations to add and subtract. the values of digits in a two-digit number. 	 Students will be able to add a two-digit number and a one-digit number, with a sum within 100. add a two-digit number and a multiple of ten, with a sum within 100. given a two-digit number, mentally find 10 more or 10 less than the number, without having to count. subtract multiples of 10 in the range 10 – 90, from multiples of 10 in the range 10 – 90 (positive or 0 differences). relate a strategy to a written method. explain the reasoning used for a given strategy. 		
	Standards for M	athematical Practice	
MP2. Reason abstractly a MP3. Construct viable ar reasoning of others. MP4. Model with mathem	guments and critique the	MP5. Use appropriate tools MP7. Look for and make us MP8. Look for and express	
Resources			
 Math Expressions, 2018: 4.1, 4.9, 4.10, 4.11, 4.13, 4.14, 4.15, 4.16, 4.17, 4,18, 5.8, 5.9, 5.10, 5.11, 8.1, 8.2, 8.3, 8.4, 8.5, 8.6 			
Assessment			
Formative Assessment • Do Now • Homework • Puzzled Penguin • Math Talk		Summative Assessment Unit Tests Benchmarks (beg 	inning, middle, end of year)

Measurement A. Measure lengths indirectly and by iterating length units.

1.M.A.1 Order three objects by length; compare the lengths of two objects indirectly by using a third object.

1.M.A.2 Express the length of an object as a whole number of length units, by laying multiple copies of a shorter object (the length unit) end to end; understand that the length measurement of an object is the number of same-size length units that span it with no gaps or overlaps. Limit to contexts where the object being measured is spanned by a whole number of length units with no gaps or overlaps.

Understandings	Essential Questions	
 Students will understand lengths of objects can be compared to lengths of other objects. measurement is an iteration of same-size units. 	How do we measure the length of an object?How do we compare the lengths of two objects?	
Knowledge	Skills	
 Students will know the units used to measure an object should not overlap. the units used to measure an object should not have gaps between them. the length measurement of an object is the number of same-size length units that span it with no gaps or overlaps. 	 Students will be able to order three objects by length. compare the lengths of two objects indirectly by using a third object. express the length of an object as a whole number of length units. 	
Standards for N	Aathematical Practice	
MP6. Attend to precision. MP7. Look for and make use of structure.		
Resources		
• Math Expressions, 2018: Lessons 7.12, 7.13, 7.14		
Assessment		
Formative Assessment	Summative Assessment	
• Do Now	• Unit Tests	
Homework	• Benchmarks (beginning, middle, end of year)	

Puzzled Penguin Math Talk

•

Measurement B. Tell and Write Time

1.M.B.3 Tell and write time in hours and half-hours using analog and digital clocks.

Understandings	Essential Questions
 Students will understand when time passes, the hour hand and the minute hand move at different rates. 	 How do the positions of the hands on an analog clock indicate the time? How do the numbers on a digital clock indicate the time?
Knowledge	Skills
 Students will know on an analog clock, the difference between the hour hand and the minute hand. on an analog clock, on the hour, the hour hand is pointing exactly to the number that represents the hour; on the half-hour, the hour hand is pointing exactly half-way between two numbers. on a digital clock, the digits to the left of the colon represent the hour and the digits to the right of the colon represent the minutes. MP6. Attend to precision. MP7. Look for and make use of structure.	 Students will be able to tell and write time in hours using an analog clock. tell and write time in half-hours using an analog clock. tell and write time in half-hours using a digital clock. tell and write time in half-hours using a digital clock.
Resources	
 Math Expressions, 2018: Lessons 7.1, 7.2, 7.3, 7.4, 7.5, 7.14 	
	sessment
Formative Assessment Do Now Homework Puzzled Penguin Math Talk	 Summative Assessment Unit Tests Benchmarks (beginning, middle, end of year)

Measurement C. Work with Money

1.M.C.4 Know the comparative values of coins and all dollar bills (e.g., a dime is of greater value than a nickel). Use appropriate notation (e.g., 69¢, \$10).

1.M.C.5 Use dollars in the solutions of problems up to \$20. Find equivalent monetary values (e.g., a nickel is equivalent in value to five pennies). Show monetary values in multiple ways. For example, show 25ϕ as two dimes and one nickel, and as five nickels. Show \$20 as two tens and as 20 ones.

Understandings	Essential Questions
Students will understand	
 different coins have unique values. 	• Why do we need money?
 the relative sizes of the coins are not related to 	Why do we need money?How do we count money?
the relative values of the coins (i.e., a penny is	· now do we count money.
larger than a dime but it is not worth more than	
a dime.)	
• some coins can be exchanged for other coins,	
e.g., 5 pennies can be exchanged for 1 nickel.	
• the value of some coins and bills can be	
represented by a combination of other coins.	
• money amounts can be counted and compared.	
• coins can be identified by their color, size, and	
edge.	
Knowledge	Skills
Students will know	Students will be able to
• pennies are copper and nickels, dimes, and	• identify a penny, nickel, dime, quarter, and dollar bill.
quarters are silver.	• sort coins.
• a nickel is bigger than a dime but smaller than a questor	• identify the value of a penny, nickel, dime, quarter and dollar bill.
quarter.pennies and nickels have a smooth edge while	
dimes and quarters have a shooth edge while	skip count to count money.compare value of set of coins or money amounts.
	Image: The set of cons of money amounts. Interactical Practice
Standards for N	Tathematical Practice
MP2. Reason abstractly and quantitatively.	
MP3. Construct viable arguments and critique the rea	asoning of others.
MP4. Model with mathematics.	
Resources	
Done in morning routine	
Assessment	
Formative Assessment	Summative Assessment
• Do Now	Unit Tests
Homework	• Benchmarks (beginning, middle, end of year)
Puzzled Penguin	
Math Talk	

Data Literacy A. Represent and interpret data

1.DL.A.1 Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.

Understandings	Essential Questions
Students will understandthere are many ways to analyze data.	• How can representing data help us to interpret it and draw conclusions?
Knowledge	Skills
 Students will know the total number of data points will be represented in two or more categories. 	 Students will be able to organize data with up to three categories. represent data with up to three categories. interpret data with up to three categories. compare the number of data points in two categories.
Standards for Mathematical Practice	
MP2. Reason abstractly and quantitatively.MP3. Construct viable arguments and critique the reasoning of others.MP4. Model with mathematics.MP5. Use appropriate tools strategically.MP6. Attend to precision.	
Resources	
• Math Expressions, 2018: Lessons 6.1, 6.2, 6.3, 6.4, 6.5, 6.9	
Assessment	
Formative Assessment Do Now Homework Purzlad Panguin 	Summative Assessment Unit Tests Benchmarks (beginning, middle, end of year)

- Puzzled Penguin
- Math Talk
Geometry A. Reason with shapes and their attributes

1.G.A.1 Distinguish between defining attributes (e.g., triangles are closed and three-sided) versus nondefining attributes (e.g., color, orientation, overall size); build and draw shapes to possess defining attributes.

1.G.A.2 Compose two-dimensional shapes (rectangles, squares, trapezoids, triangles, half-circles, and quartercircles) or three-dimensional shapes (cubes, right rectangular prisms, right circular cones, and right circular cylinders) to create a composite shape, and compose new shapes from the composite shape.

1.G.A.3 Partition circles and rectangles into two and four equal shares, describe the shares using the words *halves*, *fourths*, and *quarters*, and use the phrases *half of*, *fourth of*, and *quarter of*. Describe the whole as two of, or four of the shares. Understand for these examples that decomposing into more equal shares creates smaller shares.

of the shares. Understand for these examples that decomposing into			
Understandings		Essential Questions	
Understandings Students will understand attributes may or may not define a shape. new shapes can be made from two or more other shapes. compositions must be within the same dimension. shares of a whole must always be equal. decomposing into more equal shares creates smaller shares. Knowledge Students will know shapes are characterized by their defining attributes (number of sides, size of angles, etc.). non-defining attributes (color, overall size, orientation, etc.) give additional information but		hares. defining a es to posse sional sha rter-circles insional sha ight circul two and fe into two ar	ess defining attributes. pes (rectangles, squares, trapezoids, triangles, s) to create a composite shape. apes (cubes, right rectangular prisms, right ar cylinders)* to create a composite shape. our equal shares. nd four equal shares.
do not characterize the shape.	 appropriately use the words halves, fourths and quarters and the phrases <i>half of, fourth of,</i> and <i>quarter of.</i> describe the whole as two of, or four of the shares. 		
*Students do not need to learn formal names.			
	Standards for Math	nematica	al Practice
MP2. Reason abstractly and qua MP3. Construct viable argument MP4. Model with mathematics. MP6. Attend to precision. MP7. Look for and make use of	ts and critique the reasoning	ng of other	s.
	Resou	rces	
• Math Expressions, 2018: Le			.14
Assessment			
• Do Now • U		ve Assessment nit Tests enchmarks (beginning, middle, end of year)	

Additional Lesson for Grade 1 ***This money cluster was moved to the Measurement domain***

Although not required in the standards, students need to be exposed to additional topics in order to prepare for what is required in future grades. In Grade 1 this includes money.

Understandings	Essential Questions	
 Students will understand different coins have unique values. the relative sizes of the coins are not related to the relative values of the coins (i.e., a penny is larger than a dime but it is not worth more than a dime.) some coins can be exchanged for other coins, e.g., 5 pennies can be exchanged for 1 nickel. the value of some coins and bills can be represented by a combination of other coins. money amounts can be counted and compared. coins can be identified by their color, size, and edge. 	 Why do we need money? How do we count money? 	
 Knowledge Students will know pennies are copper and nickels, dimes, and quarters are silver. a nickel is bigger than a dime but smaller than a quarter. pennies and nickels have a smooth edge while dimes and quarters have an edge with ridges 	Skills Students will be able to identify a penny, nickel, dime, quarter, and dollar bill. sort coins. identify the value of a penny, nickel, dime, quarter and dollar bill. skip count to count money. compare value of set of coins or money amounts.	
Resources		
• Done in morning routine		

Career Readiness, Life Literacies, and Key Skills

Career Readiness, Life Literacies, and Key Skills

Rapid advancements in technology and subsequent changes in the economy have created opportunities for individuals to compete and connect on a global scale. In this increasingly diverse and complex world, the successful entrepreneur or employee must not only possess the requisite education for specific industry pathways but also employability skills necessary to collaborate with others and manage Resources effectively in order to establish and maintain stability and independence. This document outlines concepts and skills necessary for New Jersey's students to thrive in an ever-changing world. Intended for integration throughout all K–12 academic and technical content areas, the New Jersey Student Learning Standards- Career Readiness, Life Literacies, and Key Skills (NJSLS-CLKS) provides the framework for students to learn the concepts, skills, and practices essential to the successful navigation of career exploration and preparation, personal finances and digital literacy.

Mission

Career readiness, life literacies, and key skills education provides students with the necessary skills to make informed career and financial decisions, engage as responsible community members in a digital society, and to successfully meet the challenges and opportunities in an interconnected global economy.

Vision

An education in career readiness, life literacies, and key skills fosters a population that:

•Continually self-reflects and seeks to improve the essential life and career practices that lead to success;

•Uses effective communication and collaboration skills and Resources to interact with a global society;

•Possesses financial literacy and responsibility at home and in the broader community;

•Plans, executes, and alters career goals in response to changing societal and economic conditions; and •Seeks to attain skill and content mastery to achieve success in a chosen career path.

Career Readiness, Life Literacies, and Key Skills

- 9.1.2. FI.1: Differentiate the various forms of money and how they are used (e.g., coins, bills, checks, debit and credit cards).
- 9.1.2.FP.2: Differentiate between financial wants and needs.
- **9.1.2.FP.3:** Identify the factors that influence people to spend or save (e.g., commercials, family, culture, society).
- 9.1.2.PB.2: Explain why an individual would choose to save money.
- **9.4.2.CI.1**: Demonstrate openness to new ideas and perspectives (e.g., 1.1.2.CR1a, 2.1.2.EH.1, 6.1.2.CivicsCM.2).
- 9.4.2.CI.2: Demonstrate originality and inventiveness in work (e.g., 1.3A.2CR1a).
- **9.4.2.CT.1:** Gather information about an issue, such as climate change, and collaboratively brainstorm ways to solve the problem (e.g., K-2-ETS1-1, 6.3.2.GeoGI.2).
- 9.4.2.CT.2: Identify possible approaches and Resources to execute a plan (e.g., 1.2.2.CR1b, 8.2.2.ED.3).
- 9.4.2.CT.3: Use a variety of types of thinking to solve problems (e.g., inductive, deductive).
- **9.4.2.DC.3:** Explain how to be safe online and follow safe practices when using the internet (e.g., 8.1.2.NI.3, 8.1.2.NI.4).
- 9.4.2.DC.6: Identify respectful and responsible ways to communicate in digital environments.
- 9.4.2.IML.2: Represent data in a visual format to tell a story about the data (e.g., 2.MD.D.10)

Computer Science and Design Thinking

Computer Science and Design Thinking

New approaches necessary for solving the critical challenges that we face as a society will require harnessing the power of technology and computing. Rapidly changing technologies and the proliferation of digital information have permeated and radically transformed learning, working, and everyday life. To be well-educated, global-minded individuals in a computing-intensive world, students must have a clear understanding of the concepts and practices of computer science. As education systems adapt to a vision of students who are not just computer users but also computationally literate creators who are proficient in the concepts and practices of computer science and design thinking, engaging students in computational thinking and human-centered approaches to design through the study of computer science and technology serves to prepare students to ethically produce and critically consume technology.

Mission

Computer science and design thinking education prepares students to succeed in today's knowledge-based economy by providing equitable and expanded access to high-quality, standards-based computer science and technological design education.

Vision

All students have equitable access to a rigorous computer science and design thinking education. Students will benefit from opportunities to engage in high-quality technology programs that foster their ability to:

- develop and apply computational and design thinking to address real-world problems and design creative solutions;
- engage as collaborators, innovators, and entrepreneurs on a clear pathway to success through postsecondary education and careers;
- navigate the dynamic digital landscape to become healthy, productive, 21st century global-minded individuals; and

• participate in an inclusive and diverse computing culture that appreciates and incorporates perspectives from people of different genders, ethnicities, and abilities.

COMPUTER SCIENCE AND DESIGN THINKING

- **8.1.2.CS.1:** Select and operate computing devices that perform a variety of tasks accurately and quickly based on user needs and preferences.
- **8.1.2.AP.1:** Model daily processes by creating and following algorithms to complete tasks.
- **8.1.2.AP.4:** Break down a task into a sequence of steps.
- **8.1.2.AP.5:** Describe a program's sequence of events, goals, and expected outcomes.
- **8.1.2.AP.6:** Debug errors in an algorithm or program that includes sequences and simple loops.
- **8.1.2.DA.1:** Collect and present data, including climate change, in various visual formats.
- **8.1.2.DA.3:** Identify and describe patterns in data visualizations.
- **8.1.2.DA.4:** Make predictions based on data using charts or graphs.
- **8.2.2.ED.1:** Communicate the function of a product or device.
- **8.2.2.ITH.4:** Identify how various tools reduce work and improve daily tasks.
- **8.2.2.NT.2:** Brainstorm how to build a product, improve a designed product, fix a product that has stopped working, or solve a simple problem.

Differentiation Strategies

Students with Disabilities/ Students at Risk of School Failure

(For students with disabilities, appropriate accommodations, instructional adaptations, and/or modifications should be determined by the IEP or 504 team)

Modifications for Classroom

- Pair visual prompts with verbal presentations
- Ask students to restate information, directions, and assignments.
- Give repetition and practice exercises
- Model skills/techniques to be mastered
- Give extended time to complete class work
- Provide copy of class notes
- Determine if preferential seating would be beneficial
- Provide access to a computer
- Provide copies of textbooks for home
- Provide access to books on tape/CD/digital media, as available and appropriate
- Assign a peer helper in the class setting
- Provide oral reminders and check student work during independent work time
- Assist student with long- and short-term planning of assignments
- Encourage student to proofread assignments and tests
- Provide regular parent/school communication

Modifications for Homework and Assignments

- Provide extended time to complete assignments
- Break down assignments
- Provide the student with clearly stated (written) expectations and grading criteria for assignments
- Implement RAFT activities as they pertain to the types/modes of communication (role, audience, format, topic)

Modifications for Assessments

- Provide extended time on classroom tests and quizzes
- Provide alternate setting as needed
- Restate, reread, and clarify directions/questions
- Distribute study guide for classroom tests
- Establish procedures for accommodations /modifications for assessments

Differentiation Strategies

Gifted and Talented

(content, process, product and learning environment)

- Allow students to pursue independent projects based on their individual interests
- Provide enrichment activities that include more advanced material
- Allow team-teaching opportunities and collaboration
- Set individual goals
- Conduct research and provide presentation of appropriate topics
- Design surveys to generate and analyze data to be used in discussion.
- Use Higher-Level Questioning Techniques
- Provide assessments at a higher level of thinking

English Language Learners

Modifications for Classroom

- Pair visual prompts with verbal presentations
- Provide repetition and practice
- Model skills/techniques to be mastered

Modifications for Homework/Assignments

- Provide Native Language Translation (peer, online assistive technology, translation device, bilingual dictionary)
- Provide extended time for assignment completion as needed
- Highlight key vocabulary
- Use graphic organizers

Second Grade

Interdisciplinary Connections

Mathematics is a unified body of knowledge whose concepts build upon each other. Connecting mathematical concepts includes linking ideas to related ideas learned previously.

Major emphasis should be given to ideas and concepts across mathematical content areas that help students see that mathematics is a web of closely connected ideas. Students need to connect their mathematical learning to appropriate real-world contexts. They need to create interest and maintain the interest after the novelty of the work has worn off.

Mathematics is the language of science and is greatly utilized in industry and business. It gives us the power to solve difficult real-world problems, but also helps us to understand how the universe operates.

Every mathematics teacher needs to make students unafraid of the subject by convincing the students of the usefulness of learning mathematics in their daily lives and for higher studies. The world today, which leans more and more heavily on Science and Technology, demands more from mathematics. Tomorrow's world will, no doubt, make still greater demands from mathematics.

Interdisciplinary Connections for Grade 2

Literature:

~Even Steven Odd Todd by Kathryn Cristaldi

~*How Big is a Foot* by Rolf Myller

Math Expressions Math Readers:

- Unit 1 Game Time!
- Unit 2 *The Number Machine*
- Unit 3 Taking Shape
- Unit 4 Comic Books for Sale
- Unit 5 Wow! Fluffo Sure Can Eat
- Unit 6 The If Game
- Unit 7 The Pizza Puzzle

(NJSLSA.R1. Read closely to determine what the text says explicitly and to make logical inferences and relevant connections from it; cite specific textual evidence when writing or speaking to support conclusions drawn from the text.

RL.2.1. Ask and answer such questions as who, what, where, when, why, and how to demonstrate understanding of key details in a text.)

Social Studies Themed Projects Infusing Math:

Fact Family Pumpkins Turkey Name Collection Box Flower Pot Telling Time Spring Umbrella Fact Fluency

(6.1.2.HistoryCC.3: Make inferences about how past events, individuals, and innovations affect our current lives.

6.1.2.Geo.HE.1: Explain how seasonal weather changes, climate, and other environmental characteristics affect people's lives in a place or region.)

Climate Change for Grade 2

With the adoption of the 2020 New Jersey Student Learning Standards (NJSLS), New Jersey became the first state in the nation to include climate change across content areas. The goal of inclusion of climate change education implementation is to foster generations of New Jersey students that can analyze, question, interpret, to think independently, and bring critical deduction to fulfill, and to lead in jobs created by burgeoning industries of the future green economy.

- 2.OA.A.1 Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
 - o Students will solve a series of word problems involving the environment.
- 2.DL.B.4 Draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. Solve simple put together, take-apart, and compare problems using information presented in a bar graph.
 - Students will read a variety of situations in terms of waste collection. Students will graph the data provided and answer questions about the information.

New Jersey Student Learning Standards (NJSLS)

In Grade 2, instructional time should focus on four critical areas: (1) extending understanding of base ten notation; (2) building fluency with addition and subtraction; (3) using standard units of measure; and (4) describing and analyzing shapes.

(1) Students extend their understanding of the base-ten system. This includes ideas of counting in fives, tens, and multiples of hundreds, tens, and ones, as well as number relationships involving these units, including comparing. Students understand multi-digit numbers (up to 1000) written in base-ten notation, recognizing that the digits in each place represent amounts of thousands, hundreds, tens, or ones (e.g., 853 is 8 hundreds + 5 tens + 3 ones).

(2) Students use their understanding of addition to develop fluency with addition and subtraction within 100. They solve problems within 1000 by applying their understanding of models for addition and subtraction, and they develop, discuss, and use efficient, accurate, and generalizable methods to compute sums and differences of whole numbers in base-ten notation, using their understanding of place value and the properties of operations. They select and accurately apply methods that are appropriate for the context and the numbers involved to mentally calculate sums and differences for numbers with only tens or only hundreds.

(3) Students recognize the need for standard units of measure (centimeter and inch) and they use rulers and other measurement tools with the understanding that linear measure involves an iteration of units. They recognize that the smaller the unit, the more iterations they need to cover a given length.

(4) Students describe and analyze shapes by examining their sides and angles. Students investigate, describe, and reason about decomposing and combining shapes to make other shapes. Through building, drawing, and analyzing two- and three-dimensional shapes, students develop a foundation for understanding area, volume, congruence, similarity, and symmetry in later grades.

Operations and Algebraic Thinking A. Represent and solve problems involving addition and subtraction.

2.OA.A.1 Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

using drawings and equations with a symbol for the us	hknown number to represent the problem.	
Understandings	Essential Questions	
 Students will understand addition involves adding to and putting together. subtraction involves taking from, taking apart, and missing numbers in a math sentence can be found and subtraction. a symbol can represent an unknown. the unknown may be located in any position in the objects, drawings, and equations can be used to see 	using addition a whole?	
Knowledge	Skills	
 Students will know the meaning of addition. the meaning of subtraction. there are multiple interpretations of addition and subtraction. some problems take more than one step to solve. 	 Students will be able to use addition and subtraction within 100 to solve word problems that involve one-and twostep problems. use objects and drawings to represent problems. use equations with a symbol for the unknown number to represent the problem. 	
Standards for M	athematical Practice	
 MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP5. Use appropriate tools strategically. MP8. Look for and express regularity in repeated reasoning. 		
	Sources	
 Math Expressions, 2018: Lessons 1.1, 1.2, 1.4, 1.10, 1.11, 1.12, 1.13, 1.14, 1.15, 1.16, 1.17, 1.18, 1.19, 1.20, 1.21, 2.1, 2.2, 2.7, 2.15, 4.3, 4.4, 4.5, 4.12, 4.13, 4.14, 4.16, 4.17, 4.18, 4.19, 4.20, 4.21, 4.22, 4.23, 5.1, 5.4, 5.5, 5.6, 5.7, 5.9, 5.10, 6.8, 6.9, 6.14, 6.15, 7.3, 7.4, 7.5 		
Assessment		
Formative Assessment Minute Math Fluency Checks Do Now Homework Puzzled Penguin Math Talk Exit Slips IXL and other online tools 	 Summative Assessment Unit Tests Quick Quizzes Benchmarks (beginning, middle, end of year) 	

Operations and Algebraic Thinking B. Add and subtract within 20.

2.OA.B.2 With accuracy and efficiency add and subtract within 20 using mental strategies. By end of Grade 2, know from memory all sums of two one-digit numbers.

Understandings	Essential Questions	
Students will understandthere are multiple strategies to add and subtract	• How can a problem be simplified?	
	 What strategies are available to determine how much or how many we have? 	
Knowledge	Skills	
 Students will know numbers that make 10 will help solve problems. numbers can be decomposed into simpler terms. the inverse relationship between addition and subtraction. solutions can be found by forming equivalent but easier or known sums. 	 Students will be able to fluently add within 20 using mental strategies. fluently subtract within 20 using mental strategies. 	
Standards for Mathematical Practice		

MP2. Reason abstractly and quantitatively.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Lessons 1.1, 1.2, 1.3, 1.4, 1.5, 1.7, 1.8, 1.9, 1.10, 1.11, 1.12, 1.13, 1.14, 1.15, 1.16, 1.17, 1.18, 2.1, 2.2, 2.6, 3.1, 3.2, 3.4, 4.6, 4.13, 5.3, 5.4, 5.5, 5.9, 5.10

Assessment		
Formative Assessment	Summative Assessment	
Minute Math	Unit Tests	
Fluency Checks	Quick Quizzes	
Do Now	• Benchmarks (beginning, middle, end of year)	
Homework		
Puzzled Penguin		
Math Talk		
Exit Slips		
• IXL and other online tools		

Operations and Algebraic Thinking C. Work with equal groups of objects to gain foundations for multiplication.

2.OA.C.3 Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2s; write an equation to express an even number as a sum of two equal addends.

2.OA.C.4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.

Understandings	Essential Questions
 Students will understand a total number of objects can be found in a rectangular array by finding the sum of equal addends. odd numbers cannot be paired and even numbers can be paired. even numbers can be counted using skip counting by 2s. 	• Why would one need to pair things?
Knowledge	Skills
 Students will know odd numbers cannot be paired completely and even numbers can. that when counting by 2s, even numbers will finish the group off 	 Students will be able to determine whether a group of objects (up to 20) has an odd or even number of members use addition to find the total number of objects in a rectangular array (with up to 5 rows and 5 columns). write an equation expressing the total of a rectangular array as a sum of equal addends.

Standards for Mathematical Practice

MP2. Reason abstractly and quantitatively.

MP3. Construct viable arguments and critique the reasoning of others.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Lessons 1.6, 1.7, 1.21, 7.1, 7.6

Assessment		
Formative Assessment	Summative Assessment	
Minute Math	Unit Tests	
Fluency Checks	Quick Quizzes	
Do Now	• Benchmarks (beginning, middle, end of year)	
Homework		
Puzzled Penguin		
Math Talk		
Exit Slips		
• IXL and other online tools		

Numbers and Operations in Base Ten A. Understand place value.

2.NBT.A.1 Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases: a. 100 can be thought of as a bundle of ten tens — called a "hundred." b. The numbers 100, 200, 300, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).

2.NBT.A.2 Count within 1000; skip-count by 5s, 10s, and 100s.

2.NBT.A.3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.

2.NBT.A.4 Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and < symbols to record the results of comparisons.

Understandings	Essential Questions
 Students will understand the location of digits in a number determines the value of the number. to compare two numbers, one must compare the digits in each place, starting with the largest place 	• Why is place value important?
Knowledge	Skills
 Students will know the three digits in a three-digit number represent the amount of hundreds, tens and ones, respectively. the numbers 100, 200, 300, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones). 	 Students will be able to identify one hundred as a bundle of ten tens and ten as a bundle of ten ones. count within 1000. skip-count by 5s, 10s, and 100s. read numbers to 1000. write numbers to 1000 using base-ten numerals, number names, and expanded form. compare three digit numbers using <, =, and >.

Standards for Mathematical Practice

MP2. Reason abstractly and quantitatively.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Lessons 1.6, 2.1, 2.2, 2.3, 2.4, 2.5, 2.12, 2.15, 3.6, 4.7, 5.2, 5.10, 6.1, 6.2, 6.3, 6.4, 6.15

Assessment		
Formative Assessment	Summative Assessment	
Minute Math	Unit Tests	
Fluency Checks	Quick Quizzes	
Do Now	• Benchmarks (beginning, middle, end of year)	
Homework		
Puzzled Penguin		
Math Talk		
Exit Slips		
• IXL and other online tools		

Numbers and Operations in Base Ten B. Use place value understanding and properties of operations to add and subtract.

2.NBT.B.5 With accuracy and efficiency add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.

2.NBT.B.6 Add up to four two-digit numbers using strategies based on place value and properties of operations.

2.NBT.B.7 Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.

2.NBT.B.8 Mentally add 10 or 100 to a given number 100–900, and mentally subtract 10 or 100 from a given number 100–900.

2.NBT.B.9 Explain why addition and subtraction strategies work, using place value and the properties of operations.

Understandings	Essential Questions
 Students will understand concrete models, drawings, strategies based on place value, properties of operations, and/or the relationship between addition and subtraction can help one solve problems. when adding 10 or 100, one must add one to the tens digit or one to the hundreds-digit and not change the ones-digit. when subtracting 10 or 100, one must subtract one from the tens-digit or one from the hundreds-digit and not change the ones-digit. 	• How does place value help one find the answers to addition and subtraction problems?
Knowledge	Skills
 Students will know properties of operations to add and subtract. the values of the digits in a three-digit number. sometimes it is necessary to compose or decompose tens or hundreds. 	 Students will be able to fluently add and subtract within 100 add up to four two-digit numbers, using strategies using place value and properties of operations. add and subtract within 1000 mentally add 10 or 100 to a given number 100900. mentally subtract 10 or 100 from a given number 100-900. explain why addition and subtraction strategies work, using place value and the properties of operations.

Standards for Mathematical Practice

MP2. Reason abstractly and quantitatively.

MP3. Construct viable arguments and critique the reasoning of others.

MP4. Model with mathematics.

MP5. Use appropriate tools strategically.

MP7. Look for and make use of structure.

MP8. Look for and express regularity in repeated reasoning.

Resources

Math Expressions, 2018: Lessons 1.1, 1.3, 1.7, 1.16, 2.2, 2.4, 2.6, 2.7, 2.8, 2.9, 2.10, 2.11, 2.13, 2.14, 2.15, 3.9, 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.8, 4.9, 4.10, 4.11, 4.12, 4.13, 4.14, 4.15, 4.16, 4.17, 4.18, 4.19, 4.20, 4.21, 4.22, 4.23 5.2, 5.5, 5.7, 6.2, 6.3, 6.5, 6.6, 6.7, 6.8, 6.9, 6.10, 6.11, 6.12, 6.13, 6.14, 6.15, 7.4, 7.5

Assessment		
Formative Assessment	Summative Assessment	
Minute Math	Unit Tests	
Fluency Checks	Quick Quizzes	
Do Now	• Benchmarks (beginning, middle, end of year)	
Homework		
Puzzled Penguin		
Math Talk		
Exit Slips		
IXL and other online tools		

Measurement

A. Measure and estimate lengths in standard units.

2.M.A.1 Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.

2.M.A.2 Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen.

2.M.A.3 Estimate lengths using units of inches, feet, centimeters, and meters.

2.M.A.4 Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.

terms of a standard length unit.		
Understandings		Essential Questions
 Students will understand the difference between non-standard an measurement. measurement tools vary in the size of th them; this variation will affect the choid Knowledge Students will know appropriate tools must be used in order to properly measure an object. the approximate length of an inch, foot, centimeter, and meter. 	he unit on ce of tools. Students wil select ar measure measure describe two diff chosen) estimate meters.	 Why do we measure objects? How do we measure objects? Why do we need standard units of measurement? Skills Il be able to n appropriate tool to measure an object. e the length of an object. e the length of an object with two different tools. e how the measurements of one object differ when using ferent tools (relate the measurement to the size of the unit b. e lengths using units of inches, feet, centimeters, and e to determine how much longer one object is than , expressing the length difference in terms of a standard
Standard	ds for Mat	hematical Practice
MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critic MP5. Use appropriate tools strategically. MP6. Attend to precision. MP7. Look for and make use of structure.		ing of others.
	Reso	urces
• Math Expressions, 2018: Lessons 3.1, 3	3.2, 3.3, 3.4, 3	3.6, 3.7, 3.8, 3.9, 4.23, 7.1
		sment

Assessment			
Formative Assessment	Summative Assessment		
Minute Math	Unit Tests		
Fluency Checks	Quick Quizzes		
Do Now	• Benchmarks (beginning, middle, end of year)		
Homework			
Puzzled Penguin			
Math Talk			
Exit Slips			
• IXL and other online tools			

Measurement B. Relate addition and subtraction to length.

2.M.B.5 Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

2.M.B.6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers 0, 1, 2, ..., and represent whole-number sums and differences within 100 on a number line diagram.

Understandings	Essential Questions		
 Students will understand addition and subtraction can be used to solve word problems involving lengths that are given in the same units. whole numbers can be represented as the lengths from 0 to the number located on an equally-spaced number line. whole number sums and differences can be represented on a number line. 	 How are the locations of numbers on a number line related to length? How can addition and subtraction be used to find lengths? 		
Knowledge	Skills		
 Students will know drawings (such as drawings of rulers) can be used to solve problems involving length. equations with an unknown can be used to solve problems involving length 	 Students will be able to add within 100 to solve word problems involving length. subtract within 100 to solve word problems involving length. represent whole numbers on a number line as length from 0. represent whole numbers sums and differences with 100 on a number-line diagram 		
Standards for N	Iathematical Practice		
MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP4. Model with mathematics. MP5. Use appropriate tools strategically. Resources • Math Expressions, 2018: Lessons 4.23, 7.3, 7.4, 7.5			
As	sessment		
Formative Assessment Minute Math Fluency Checks Do Now Homework Puzzled Penguin Math Talk Exit Slips IXL and other online tools	Summative Assessment Unit Tests Quick Quizzes Benchmarks (beginning, middle, end of year)		

Measurement C. Work with time and money.

2.M.C.7 Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m.

2.M.C.8 Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies, using \$ and ¢ symbols appropriately. Example: If you have 2 dimes and 3 pennies, how many cents do you have?

Understandings	Essential Questions	
Students will understand	Essential Questions	
• when time passes, the hour hand and the minute	• How do the positions of the hands on an analog clock	
hand move at different rates.	indicate the time?	
• different coins have different values, not related	• How do the numbers on a digital clock indicate the	
to the size of the coin.	time?	
	• How do we determine how much money is needed and	
	how money one has?	
Knowledge	Skills	
Students will know	Students will be able to	
• between the hour hand and the minute hand.	• tell and write time to the nearest five minutes using	
• on an analog clock, on the hour, the hour hand	a.m. and p.m., on an analog clock.	
is pointing exactly to the number that	• tell and write time to the nearest five minutes using	
represents the hour; on the half-hour, the hour	a.m. and p.m., on a digital clock.	
hand is pointing exactly half-way between two numbers.	• solve word problems involving dollar bills, quarters,	
 on a digital clock, the digits to the left of the 	dimes, nickels and pennies using \$ and ¢ symbols appropriately.	
colon represent the hour and the digits to the	appropriatery.	
right of the colon represent the minutes.		
• the value of a dollar bill, quarter, dime, nickel		
and penny.		
Standards for Mathematical Practice		
MP1. Make sense of problems and persevere in solvi	ng them.	
MP2. Reason abstractly and quantitatively.		
MP4. Model with mathematics.		
MP5. Use appropriate tools strategically.		
MP6. Attend to precision.		
Re	esources	
• Math Expressions, 2018: Lessons 2.11, 2.12, 2.13	5, 4.1, 4.2, 4.10, 4.15, 5.1, 5.2, 6.1	
As	sessment	
Formative Assessment	Summative Assessment	
Minute Math	• Unit Tests	
Fluency Checks	Quick Quizzes	
• Do Now	• Benchmarks (beginning, middle, end of year)	
Homework		
Puzzled Penguin		
• Math Talk		
Exit Slips		
• IXL and other online tools		

Data Literacy A. Understand concepts of data Understand concepts of data. **2.DL.A.1** Understand that people collect data to answer questions. Understand that data can vary. 2.DL.A.2 Identify what could count as data (e.g., visuals, sounds, numbers). **Essential Questions Understandings** Students will understand... What is data? • there are many ways to identify data. How is data represented? • that data answers questions. • How does collecting data help us answer questions? • what counts as data. How can representing data help us to interpret it and • • draw conclusions? Knowledge Skills Students will know . . . Students will be able to . . . that data is information or facts that are identify what counts as data collected recognize information that can be collected (Numbers, • that data can be collected in different forms words, pictures, etc.) such as numbers, words, or pictures identify sources of data (observations, surveys, etc.) • that people collect data to answer questions or • demonstrate an awaremess that data can be used to learn more about a topic answer questions or solve problems **Standards for Mathematical Practice** MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP5. Use appropriate tools strategically. Resources • Math Expressions, 2018: Lessons 2.3, 3.8, 3.9, 5.8, 5.10 Assessment Formative Assessment Summative Assessment Minute Math Unit Tests • Fluency Checks **Ouick Ouizzes** Do Now Benchmarks (beginning, middle, end of year) Homework **Puzzled Penguin** • Math Talk • Exit Slips IXL and other online tools

Data Literacy B. Represent and interpret data.

2.DL.B.3 Generate measurement data by measuring lengths of several objects to the nearest whole unit, or by making repeated measurements of the same object. Show the measurements by making a line plot, where the horizontal scale is marked off in whole-number units.

2.DL.B.4 Draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. Solve simple put-together, take-apart, and compare problems using information presented in a bar graph.

graph. 🗳	Essential Questions
Understandings Students will understand	Essential Questions
• there are many ways to analyze data.	• How can representing data help us to interpret it and draw conclusions?
Knowledge	Skills
Students will know	Students will be able to
 the difference between a picture graph and a bar graph. how to make a line plot. 	 generate measurement data by measuring lengths of several objects to the nearest whole unit generate measurement data by making repeated measurements of the same object. show measurements by making a line plot, where the horizontal scale is marked off in whole-number units. organize data with up to four categories. represent data with up to four categories using a picture graph. represent data with up to four categories using a bar graph. solve simple put-together, take-apart, and compare problems using a bar graph
Standards for N	Iathematical Practice
MP1. Make sense of problems and persevere in solving	
MP2. Reason abstractly and quantitatively.	
MP4. Model with mathematics.	
MP5. Use appropriate tools strategically.	
MP6. Attend to precision.	
MP8. Look for and express regularity in repeated reas	soning.
	esources
• Math Expressions, 2018: Lessons 3.6, 3.7, 3.8, 5.	3, 5.4, 5.5, 5.6, 5.7, 5.8, 5.9, 5.10
As	sessment
Formative Assessment	Summative Assessment
Minute Math	• Unit Tests
Fluency Checks	Quick Quizzes
Do Now	• Benchmarks (beginning, middle, end of year)
Homework	
Puzzled Penguin	
Math Talk	
Exit Slips	
• IXL and other online tools	

Geometry A. Reason with shapes and their attributes.

2.G.A.1 Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces.1 Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.

2.G.A.2 Partition a rectangle into rows and columns of same-size squares and count to find the total number of them.

2.G.A.3 Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape. For example, students partition a rectangle (i.e., the whole) into three equal shares, identify each of the shares as a 'third' and describe the rectangle as three 'thirds'.

Underst		unira an	Essential Questions
Students will understand	anungs		Essential Questions
 shares of a whole must always 	be equal.		Why do we need to identify shapes?
 decomposing into more equal 	-	s.	Why would we partition shapes?
 equal shares of identical whole 			why would we putition shapes.
Knowledge			Skills
 Students will know the characteristics of triangles, guadrilatorpla 	Students will be able torecognize shapes havi	ng specifi	
pentagons, hexagons, and cubes.	 partition a rectangle into rows and columns of the same-size squares. count the squares in a partitioned rectangle to find the total number. 		
• the word half, third, and fourth refers, respectively, to			
having 2, 3, and 4equal	 partition rectangles into two, three, or four equal shares. 		
parts.	• appropriately use the words halves, thirds, fourths and quarters and the phrases half of, a third of, a fourth of, and quarter of.		
	• describe the whole as	two halve	s, three thirds, or four fourths.
	• identify equal shares of same shape.	of identica	l wholes even though they do not have the
	Standards for Mather	natical F	Practice
MP2. Reason abstractly and quant	itatively.		
MP4. Model with mathematics.			
MP6. Attend to precision.			
MP7. Look for and make use of st	ructure.		
MP8. Look for and express regula	rity in repeated reasoning.		
· · · · · · · · · · · · · · · · · · ·	Resource	ces	
• Math Expressions, 2018: Less	ons 3.2, 3.3, 3.4, 3.5, 3.9, 5	.2, 7.1, 7.2	2, 7.4, 7.6
	Assessm	ent	
Formative Assessment	Sur	nmative A	Assessment
• Minute Math			Tests
Fluency Checks			k Quizzes
• Do Now		• Benc	hmarks (beginning, middle, end of year)
Homework			
Puzzled Penguin			
• Math Talk			
Exit Slips			
• IXL and other online tools	5		

Career Readiness, Life Literacies, and Key Skills

Career Readiness, Life Literacies, and Key Skills

Rapid advancements in technology and subsequent changes in the economy have created opportunities for individuals to compete and connect on a global scale. In this increasingly diverse and complex world, the successful entrepreneur or employee must not only possess the requisite education for specific industry pathways but also employability skills necessary to collaborate with others and manage Resources effectively in order to establish and maintain stability and independence. This document outlines concepts and skills necessary for New Jersey's students to thrive in an ever-changing world. Intended for integration throughout all K–12 academic and technical content areas, the New Jersey Student Learning Standards- Career Readiness, Life Literacies, and Key Skills (NJSLS-CLKS) provides the framework for students to learn the concepts, skills, and practices essential to the successful navigation of career exploration and preparation, personal finances and digital literacy.

Mission

Career readiness, life literacies, and key skills education provides students with the necessary skills to make informed career and financial decisions, engage as responsible community members in a digital society, and to successfully meet the challenges and opportunities in an interconnected global economy.

Vision

An education in career readiness, life literacies, and key skills fosters a population that:

•Continually self-reflects and seeks to improve the essential life and career practices that lead to success;

•Uses effective communication and collaboration skills and Resources to interact with a global society;

•Possesses financial literacy and responsibility at home and in the broader community;

•Plans, executes, and alters career goals in response to changing societal and economic conditions; and •Seeks to attain skill and content mastery to achieve success in a chosen career path.

Career Readiness, Life Literacies, and Key Skills

- 9.1.2. FI.1: Differentiate the various forms of money and how they are used (e.g., coins, bills, checks, debit and credit cards).
- 9.1.2.FP.2: Differentiate between financial wants and needs.
- **9.1.2.FP.3:** Identify the factors that influence people to spend or save (e.g., commercials, family, culture, society).
- 9.1.2.PB.2: Explain why an individual would choose to save money.
- **9.4.2.CI.1**: Demonstrate openness to new ideas and perspectives (e.g., 1.1.2.CR1a, 2.1.2.EH.1, 6.1.2.CivicsCM.2).
- 9.4.2.CI.2: Demonstrate originality and inventiveness in work (e.g., 1.3A.2CR1a).
- **9.4.2.CT.1:** Gather information about an issue, such as climate change, and collaboratively brainstorm ways to solve the problem (e.g., K-2-ETS1-1, 6.3.2.GeoGI.2).
- 9.4.2.CT.2: Identify possible approaches and Resources to execute a plan (e.g., 1.2.2.CR1b, 8.2.2.ED.3).
- 9.4.2.CT.3: Use a variety of types of thinking to solve problems (e.g., inductive, deductive).
- **9.4.2.DC.3:** Explain how to be safe online and follow safe practices when using the internet (e.g., 8.1.2.NI.3, 8.1.2.NI.4).
- 9.4.2.DC.6: Identify respectful and responsible ways to communicate in digital environments.
- 9.4.2.IML.2: Represent data in a visual format to tell a story about the data (e.g., 2.MD.D.10)

Computer Science and Design Thinking

Computer Science and Design Thinking

New approaches necessary for solving the critical challenges that we face as a society will require harnessing the power of technology and computing. Rapidly changing technologies and the proliferation of digital information have permeated and radically transformed learning, working, and everyday life. To be well-educated, global-minded individuals in a computing-intensive world, students must have a clear understanding of the concepts and practices of computer science. As education systems adapt to a vision of students who are not just computer users but also computationally literate creators who are proficient in the concepts and practices of computer science and design thinking, engaging students in computational thinking and human-centered approaches to design through the study of computer science and technology serves to prepare students to ethically produce and critically consume technology.

Mission

Computer science and design thinking education prepares students to succeed in today's knowledge-based economy by providing equitable and expanded access to high-quality, standards-based computer science and technological design education.

Vision

All students have equitable access to a rigorous computer science and design thinking education. Students will benefit from opportunities to engage in high-quality technology programs that foster their ability to: • develop and apply computational and design thinking to address real-world problems and design creative solutions;

• engage as collaborators, innovators, and entrepreneurs on a clear pathway to success through postsecondary education and careers;

• navigate the dynamic digital landscape to become healthy, productive, 21st century global-minded individuals; and

• participate in an inclusive and diverse computing culture that appreciates and incorporates perspectives from people of different genders, ethnicities, and abilities.

COMPUTER SCIENCE AND DESIGN THINKING

- **8.1.2.CS.1:** Select and operate computing devices that perform a variety of tasks accurately and quickly based on user needs and preferences.
- **8.1.2.AP.1:** Model daily processes by creating and following algorithms to complete tasks.
- **8.1.2.AP.4:** Break down a task into a sequence of steps.
- **8.1.2.AP.5:** Describe a program's sequence of events, goals, and expected outcomes.
- **8.1.2.AP.6:** Debug errors in an algorithm or program that includes sequences and simple loops.
- 8.1.2.DA.1: Collect and present data, including climate change, in various visual formats.
- **8.1.2.DA.3:** Identify and describe patterns in data visualizations.
- **8.1.2.DA.4:** Make predictions based on data using charts or graphs.
- **8.2.2.ED.1:** Communicate the function of a product or device.
- **8.2.2.ITH.4:** Identify how various tools reduce work and improve daily tasks.
- **8.2.2.NT.2:** Brainstorm how to build a product, improve a designed product, fix a product that has stopped working, or solve a simple problem.

Differentiation Strategies

Students with Disabilities/ Students at Risk of School Failure

(For students with disabilities, appropriate accommodations, instructional adaptations, and/or modifications should be determined by the IEP or 504 team)

Modifications for Classroom

- Pair visual prompts with verbal presentations
- Ask students to restate information, directions, and assignments.
- Give repetition and practice exercises
- Model skills/techniques to be mastered
- Give extended time to complete class work
- Provide copy of class notes
- Determine if preferential seating would be beneficial
- Provide access to a computer
- Provide copies of textbooks for home
- Provide access to books on tape/CD/digital media, as available and appropriate
- Assign a peer helper in the class setting
- Provide oral reminders and check student work during independent work time
- Assist student with long- and short-term planning of assignments
- Encourage student to proofread assignments and tests
- Provide regular parent/school communication

Modifications for Homework and Assignments

- Provide extended time to complete assignments
- Break down assignments
- Provide the student with clearly stated (written) expectations and grading criteria for assignments
- Implement RAFT activities as they pertain to the types/modes of communication (role, audience, format, topic)

Modifications for Assessments

- Provide extended time on classroom tests and quizzes
- Provide alternate setting as needed
- Restate, reread, and clarify directions/questions
- Distribute study guide for classroom tests
- Establish procedures for accommodations /modifications for assessments

Differentiation Strategies

Gifted and Talented

(content, process, product and learning environment)

- Allow students to pursue independent projects based on their individual interests
- Provide enrichment activities that include more advanced material
- Allow team-teaching opportunities and collaboration
- Set individual goals
- Conduct research and provide presentation of appropriate topics
- Design surveys to generate and analyze data to be used in discussion.
- Use Higher-Level Questioning Techniques
- Provide assessments at a higher level of thinking

English Language Learners

Modifications for Classroom

- Pair visual prompts with verbal presentations
- Provide repetition and practice
- Model skills/techniques to be mastered

Modifications for Homework/Assignments

- Provide Native Language Translation (peer, online assistive technology, translation device, bilingual dictionary)
- Provide extended time for assignment completion as needed
- Highlight key vocabulary
- Use graphic organizers

Third Grade

Interdisciplinary Connections

Mathematics is a unified body of knowledge whose concepts build upon each other. Connecting mathematical concepts includes linking ideas to related ideas learned previously.

Major emphasis should be given to ideas and concepts across mathematical content areas that help students see that mathematics is a web of closely connected ideas. Students need to connect their mathematical learning to appropriate real-world contexts. They need to create interest and maintain the interest after the novelty of the work has worn off.

Mathematics is the language of science and is greatly utilized in industry and business. It gives us the power to solve difficult realworld problems, but also helps us to understand how the universe operates.

Every mathematics teacher needs to make students unafraid of the subject by convincing the students of the usefulness of learning mathematics in their daily lives and for higher studies. The world today, which leans more and more heavily on Science and Technology, demands more from mathematics. Tomorrow's world will, no doubt, make still greater demands from mathematics.

Interdisciplinary Connections for Grade 3

Literature:

~"The Doorbell Rang" by Pat Hutchins (**R.I.3.2**)

- Introduce the lesson by reading *The Doorbell Rang*.
- Follow the lesson in the Supplemental Section. The lesson provided can cover up to 3 days, but modify as needed for time and student needs.

~"A Remainder of One" by Elinor Princzes (**R.I.3.2**)

- Introduce the lesson by reading *A Remainder of One*.
- Follow the lesson in the Supplemental Section.

~"How Big is a Foot?" by Rolf Myller (R.I.3.1)

- Introduce the lesson by reading *How Big is a Foot?* There is a you tube video of the story as well.
- Follow the lesson in the Supplemental Section.

Social Studies:

~Bar Graphs (6.1.5.GeoPP.4)

- Students will interview their classmates about their nationalities.
- Compile the data collected, organize the data and create bar graphs displaying their results.
- Use the worksheet in the Supplemental Section as a guide

Climate Change for Grade 3

With the adoption of the 2020 New Jersey Student Learning Standards (NJSLS), New Jersey became the first state in the nation to include climate change across content areas. The goal of inclusion of climate change education implementation is to foster generations of New Jersey students that can analyze, question, interpret, to think independently, and bring critical deduction to fulfill, and to lead in jobs created by burgeoning industries of the future green economy.

- 3.OA.A.3: Students may solve multiplication and division word problems involving measurement quantities related to glacier retreat.
- 3.M.C.6 : Climate Change Example: Students may solve real world problems about glacier retreat that involve perimeters of polygons.
 - o Students will solve word problems involving glacier retreat.
 - Students will be provided with 2 pictures of the same glacier one present day and one from its past. Students will measure the perimeter of both glaciers and compare its size.

New Jersey Student Learning Standards (NJSLS)

In Grade 3, instructional time should focus on four critical areas: (1) developing understanding of multiplication and division and strategies for multiplication and division within 100; (2) developing understanding of fractions, especially unit fractions (fractions with numerator 1); (3) developing understanding of the structure of rectangular arrays and of area; and (4) describing and analyzing two-dimensional shapes.

(1) Students develop an understanding of the meanings of multiplication and division of whole numbers through activities and problems involving equal-sized groups, arrays, and area models; multiplication is finding an unknown product, and division is finding an unknown factor in these situations. For equal-sized group situations, division can require finding the unknown number of groups or the unknown group size. Students use properties of operations to calculate products of whole numbers, using increasingly sophisticated strategies based on these properties to solve multiplication and division problems involving single-digit factors. By comparing a variety of solution strategies, students learn the relationship between multiplication and division.

(2) Students develop an understanding of fractions, beginning with unit fractions. Students view fractions in general as being built out of unit fractions, and they use fractions along with visual fraction models to represent parts of a whole. Students understand that the size of a fractional part is relative to the size of the whole. For example, 1/2 of the paint in a small bucket could be less paint than 1/3 of the paint in a larger bucket, but 1/3 of a ribbon is longer than 1/5 of the same ribbon because when the ribbon is divided into 3 equal parts, the parts are longer than when the ribbon is divided into 5 equal parts. Students are able to use fractions to represent numbers equal to, less than, and greater than one. They solve problems that involve comparing fractions by using visual fraction models and strategies based on noticing equal numerators or denominators.

(3) Students recognize area as an attribute of two-dimensional regions. They measure the area of a shape by finding the total number of same size units of area required to cover the shape without gaps or overlaps, a square with sides of unit length being the standard unit for measuring area. Students understand that rectangular arrays can be decomposed into identical rows or into identical columns. By decomposing rectangles into rectangular arrays of squares, students connect area to multiplication, and justify using multiplication to determine the area of a rectangle.

(4) Students describe, analyze, and compare properties of two-dimensional shapes. They compare and classify shapes by their sides and angles, and connect these with definitions of shapes. Students also relate their fraction work to geometry by expressing the area of part of a shape as a unit fraction of the whole.

3.OA.A.1. Interpret products of whole numbers, e.g., interpret 5×7 as the total number of objects in 5 groups of 7 objects each. *For example, describe and/or represent a context in which a total number of objects can be expressed as* 5×7 .

3.OA.A.2. Interpret whole-number quotients of whole numbers, e.g., interpret $56 \div 8$ as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. *For example, describe and/or represent a context in which a number of shares or a number of groups can be expressed as* $56 \div 8$.

3.OA.A.3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.¹

3.OA.A.4. Determine the unknown whole number in a multiplication or division equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = \div 3$, $6 \times 6 = ?$

Understandings		Essential Questions	
 Students will understand the total number of objects, when grouped, can be found most efficiently by multiplication. there are two different interpretations to a division problem. when two out of three numbers are known in an equation, there is exactly one number, represented by the unknown, which will make the statement true. 		• How are multiplication and division related?	
Knowledge		Skills	
 Students will know the product of a x b is "a" groups of "b" things. the quotient of c ÷ d can be interpreted as the number of objects when "c" things are partitioned equally into "d" shares or it can be interpreted as the number of groups when "c" things are partitioned into equal shares of "d" things. 	 Students will be able to interpret products of whole numbers. interpret whole-number quotients of whole numbers. by using multiplication and division in drawings and equations, solve word problems within 100. The word problems will involve equal groups, arrays, and measurement quantities. determine the unknown whole number in a multiplication or division equation relating three whole numbers. 		
Standards for	· Mathema	itical Practice	
MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively.	others. MP4. Model	uct viable arguments and critique the reasoning of with mathematics. for and express regularity in repeated reasoning.	
	Resources	\cdot	
• Math Expressions, 2018: Unit 1, Unit 2, Unit 6, Unit			
A	Assessmen	t	
Formative Assessment Quick Check Quiz Puzzled Penguin Exit Slips White Board Checks]	tive Assessment Unit Assessment Mid-Unit Quiz Unit Projects	
Homework			

3.OA.B.5. Apply properties of operations as strategies to multiply and divide.² *Examples:* If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known. (Commutative property of multiplication.) $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$. (Associative property of multiplication.) Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (Distributive property.)

3.OA.B.6. Understand division as an unknown-factor problem. For example, find $32 \div 8$ by finding the number that makes 32 when multiplied by 8.

Understandings	Essential Questions
 Students will understand multiplication and division are inverse operations. using properties can make problems easier. 	 How can one use properties as strategies to solve problems? How can one use multiplication to help solve division problems?
Knowledge	Skills
 Students will know a x b = b x a (a x b) x c = a x (b x c) a x (b + c) = (a x b) + (a x c) how to solve unknown-factor problems. 	 Students will be able to apply properties (commutative, associative, and distributive) of operations as strategies to multiply and divide. find the answer to a division problem by solving the related unknown-factor problem.
Standards for M	athematical Practice
MP1. Make sense of problems and persevere in solving MP2. Reason abstractly and quantitatively. MP4. Model with mathematics.	them.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Unit 1, Unit 2

Assessment		
Formative Assessment	Summative Assessment	
Quick Check Quiz	Unit Assessment	
Puzzled Penguin	Mid-Unit Quiz	
Exit Slips	Unit Projects	
White Board Check		
Homework		

3.OA.C.7. With accuracy and efficiency, multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g. knowing that $8 \ge 40$, one knows $40 \div 5 = 8$) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers.

By the end of Grade 3, know from memory all products of two one-digit numbers.

² Students need not use formal terms for these properties.

Understandings	Essential Questions
Students will understand	
 there is an inverse relationship between 	• How can one use the relationship between
multiplication and division.	multiplication and division to find products and
1	quotients?
	quotients:
Knowledge	Skills
Students will know	Students will be able to
• strategies to multiply and divide.	• fluently multiply within 100, using properties of
	operations or the relationship between multiplication
	and division.
	• fluently divide within 100, using properties of operations or the relationship between multiplication
	and division.
Standards for N	Aathematical Practice
MP1. Make sense of problems and persevere in solvi	ng them.
MP2. Reason abstractly and quantitatively.	
MP4. Model with mathematics.	
MP8. Look for and express regularity in repeated rea	soning.
J	Resources
• Math Expressions, 2018: Unit 1, Unit 2	
As	sessment
Formative Assessment	Summative Assessment
Quick Check Quiz	Unit Assessment
Puzzled Penguin	Mid-Unit Quiz
Exit Slips	Unit Projects
White Board Check	
Homework	

3.OA.D.8. Solve two-step word problems, including problems involving money, using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.³

3.OA.D.9. Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations. *For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.*

³ This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order.

	particular order.		
Understandings	5	Essential Questions	
 Students will understand there are strategies to find patterns in a sequence of numbers. equations can model real-world problems. 		• How can patterns be used to solve problems?	
Knowledge		Skills	
Knowledge Status Students will know Students will be able to how to round a number. represent word problems using equations with a letter standing for the unknown quantity. properties of operations. solve two-step word problems using the four operations. assess the reasonableness of answers using mental computation and estimation strategies including rounding. identify arithmetic patterns (including patterns in the addition or multiplication tables), and explain them using properties of operations. For example, observe that four times a number is always even and explain why four times a number can be decomposed into two equal addends. MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics.			
MP8. Look for and express regula			
	Re	sources	
Math Expressions, 2018: Unit 1, Unit 2, Unit 6			
	As	ssessment	
Formative Assessment Quick Check Quiz Puzzled Penguin Exit Slips White Board Check Homework		Summative Assessment Unit Assessment Mid-Unit Quiz Unit Projects	

Numbers and Operations in Base Ten

3.NBT.A.1. Use place value understanding to round whole numbers to the nearest 10 or 100.

3.NBT.A.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.

3.NBT.A.3. Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., 9×80 , 5×60) using strategies based on place value and properties of operations.

 $\overline{^{1}}$ A range of algorithms may be used.

¹ A range of algorithms may be used.	
Understandings	Essential Questions
 Students will understand the place that a digit is located assigns a value to that digit. products that involve multiples of 10 can be found by multiplying the non-zero digits of the two numbers and then multiplying by 10. 	• Why is place value important?
Knowledge	Skills
 the procedure needed to round a whole number. properties of operations. strategies involving place-value, properties of operations, and inverse operations. multiples of 10 in the range 10 – 90 process 	
R	esources
Math Expressions, 2018: Unit 3, Unit 4, Unit 6	
	ssessment
Formative Assessment Quick Check Quiz Puzzled Penguin Exit Slips White Board Check Homework	Summative Assessment Unit Assessment Mid-Unit Quiz Unit Projects

Numbers and Operations - Fractions

3.NF.A.1. Understand a fraction 1/b as the quantity formed by 1 part when *a* whole is partitioned into *b* equal parts; understand a fraction a/b as the quantity formed by a parts of size 1/b. For example: If a rectangle (i.e. the whole) is partitioned into 3 equal parts, each part is 1/3. Two of those parts would be 2/3.

3.NF.A.2. Understand a fraction as a number on the number line; represent fractions on a number line diagram.

- a. Represent a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into *b* equal parts. Recognize that each part has size 1/b and that the endpoint of the part based at 0 locates the number 1/b on the number line. For example, partition the number line from 0 to 1 into 3 equal parts, represent 1/3 on the number line and show that each part has a size of 1/3
- b. Represent a fraction a/b on a number line diagram by marking off a lengths 1/b from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line.

3.NF.A.3. Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.

- a. Understand two fractions as equivalent (equal) if they are the same size. Understand two fractions as equivalent if they are located at the same point on a number line.
- b. Recognize and generate simple equivalent fractions, e.g., 1/2 = 2/4, 4/6 = 2/3). Explain why the fractions are equivalent with the support of visual models.
- c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. Examples: Express 3 in the form 3 = 3/1; recognize that 6/1 = 6; locate 4/4 and 1 at the same point on a number line diagram.
- d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions with the support of a visual fraction model.

¹ Grade 3 expectations in this domain are limited to fractions with denominators 2, 2	3, 4, 6	, 8.
--	---------	------

Understandings	Essential Questions
 Students will understand other numbers exist in addition to whole numbers. the number one can be broken down into fractional parts that are also numbers. 	• Why do we need fractions?
Knowledge	Skills
 a fraction 1/b is the quantity formed by 1 part when a whole is partitioned into b equal parts; when b gets larger, more parts are formed and each part gets smaller. a fraction a/b is the quantity formed by a parts of size 1/b. a fraction is a number on the number line. two fractions are equivalent (equal) if they represent the same amount of the whole. two fractions are equivalent (equal) if they represent the same point on the number line. comparing fractions is valid only when the two 	 Students will be able to represent fractions on a number line diagram. represent a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size 1/b and that the endpoint of the part based at 0 locates the number 1/b on the number line. represent a fraction a/b on a number line diagram by defining the interval from 0 to 1 as the whole, partition it into b equal parts and mark off a, lengths 1/b, from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line. explain equivalence of fractions in special cases.

	 generate simple equivalent fractions. explain why fractions are equivalent, e.g., using a visual fraction model. express whole numbers as fractions. recognize fractions that are equivalent to whole numbers. compare two fractions with the same numerator or the same denominator by reasoning about their size. compare fractions using <, =, or > . justify fraction comparisons, e.g., using a visual fraction model. 			
Standards for Mathematical Practice				
MP1. Make sense of problems and persevere in solving them.				
MP2. Reason abstractly and quantitatively.				
MP3. Construct viable arguments and critique the reasoning of others.				
MP4. Model with mathematics.				
MP5. Use appropriate tools strategically.				
MP6. Attend to precision.				
Resources				
• Math Expressions, 2018: Unit 4, Unit 5				
Assessment				
Formative Assessment	Summative Assessment			
Quick Check Quiz	Unit Assessment			
Puzzled Penguin	Mid-Unit Quiz			
i ullioù i onguin				
Exit Slips	Unit Projects			
e e	Unit Projects			

Measurement

A. Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.

3.M.A.1. Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.

3.M.A.2. Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l). Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem.

Clarification: "Measure and estimate liquid volumes and masses" excludes compound units such as cm³ and finding the geometric volume of a container. "Multiplying to solve one-step word problems" excludes multiplicative comparison problems (problems involving "times as much"; See Glossary, Tables 2a-2d)).

Understand	lings	Essential Questions	
Understandings Students will understand		Why does one need to measure?	
 measurement involves units that must match in order to add 		5	
or subtract them.		• How does one measure riquids:	
		• How does one measure mass?	
Knowled	ge	Skills	
Students will know	Students will be able to .		
• time intervals involve a start	• tell and write time to the nearest minute.		
time and an end time.	• measure time intervals in minutes.		
• how to add or subtract on a	• solve word problems involving addition and subtraction of time intervals in		
number line.	minutes, e.g., by representing the problem on a number line diagram.		
	• measure liquid volumes .		
	• estimate liquid volumes.		
	• measure masses of objects using standard units of grams (g), kilograms		
	(kg), and liters (l).		
	• estimate masses of objects using standard units of grams (g), kilograms		
	(kg), and liters (l).		
		ly, or divide to solve one-step word problems involving	
	masses or volumes that are given in the same units, e.g., by using drawings		
(such as a beaker with a measurement scale) to represent the problem.			
	Standards for Mather	matical Practice	
MP1. Make sense of problems and p	e		
MP3. Construct viable arguments ar	nd critique the reasoning of	f others.	
MP4. Model with mathematics.			
MP5. Use appropriate tools strategic	cally.		
MP8. Look for and express regularit	ty in repeated reasoning.		
Resources			
• Math Expressions, 2018: Unit	4, Unit 7		
Assessment			
Formative Assessment		Summative Assessment	
Quick Check Quiz		Unit Assessment	
Puzzled Penguin		Mid-Unit Quiz	
Exit Slips		Unit Projects	
White Board Check		·	
Homework			

Measurement				
B. Geometric measurement: Understand concepts of area and relate area to multiplication and to addition.				
3.M.B.3. Recognize area as an attribute of plane figures and understand concepts of area measurement.a. A square with side length 1 unit, called "a unit square," is said to have "one square unit" of area, and can be used to				
	measure area. b. A plane figure which can be covered without gaps or overlaps by <i>n</i> unit squares is said to have an area of <i>n</i> square units.			
3.M.B.4 . Measure areas by counting unit	squares (square cm, squa	are m, square in, square ft, and non-standard units).		
 3.M.B.5. Relate area to the operations of multiplication and addition. a. Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths. b. Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning. c. Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths <i>a</i> and <i>b</i> + <i>c</i> is the sum of <i>a</i> × <i>b</i> and <i>a</i> × <i>c</i>. Use area models to represent the distributive property in mathematical reasoning. d. Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world problems. 				
Understandings:		Essential Questions		
 Students will understand area measurement involves covering a surface. area is measured in square units. that area is related to the operations of multiplication and division. 		Why do we need to measure the area of a surface?How do we find areas of irregular shapes?		
Knowledge	Skills			
 Students will know area is an attribute of plane figures. a square with side length 1 unit, called "a unit square" is said to have "one square unit" of area. a unit square can be used to measure area. a plane figure which can be covered without gaps or overlaps by <i>n</i> unit squares is said to have an area of <i>n</i> square units. area is additive. 	 Students will be able to measure areas by counting unit squares (square cm, square m, square in, square ft., and improvised units). find the area of a rectangle with whole-number side lengths by tiling it show that the area of a rectangle found by tiling is the same as would be found by multiplying the side lengths. multiply side lengths to find areas of rectangles with whole number side lengths in the context of solving real-world and mathematical problems. represent whole-number products as rectangular areas in mathematical reasoning. use tiling in a concrete case that the area of a rectangle with whole-number side lengths <i>a</i> and <i>b</i>+<i>c</i> is the sum of <i>a</i> x <i>b</i> and <i>a</i> x <i>c</i>. use area models to represent the distributive property in mathematical reasoning. find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts. apply this technique to solve real-world problems. 			
Standards for Mathematical Practice				
MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP4. Model with mathematics. MP8. Look for and express regularity in repeated reasoning. Resources				
Math Expressions, 2018: Unit 1, Unit 2				
Assessment				
Formative Assessment Quick Check Quiz Puzzled Penguin Exit Slips White Board Check Homework		Summative Assessment Unit Assessment Mid-Unit Quiz Unit Projects		
Measurement and Data

C. Geometric measurement: Recognize perimeter as an attribute of plane figures and distinguish between area measurements.

3.M.C.6. Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

Students will understand • What types of problems involve perimeter? • What types of problems involve perimeter? • What types of problems involve area? • If ind an unknown side length of a polygon given the side lengths. • find an unknown side length of a polygon. • exhibit rectangles with the same area but different areas. • exhibit rectangles with the same area but different areas. • solve real-world and mathematical problems involving perimeters. • Studards for Mathematical Practice MP1. Make sense of problems and persevere in solving them. MP2.	Understandings	Essential Questions	
measure. • What types of problems involve area? Knowledge Skills Students will know • the difference between area and perimeter. • rectangles with the same area do not necessarily have the same perimeter and vice versa. • find the perimeter of a polygon given the side lengths. • and unknown side length of a polygon. • exhibit rectangles with the same perimeter but different areas. • exhibit rectangles with the same perimeter but different perimeters. • solve real-world and mathematical problems involving perimeters of polygons. MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP6. Attend to precision. Resources • Math Expressions, 2018: Unit 5 • Supplemental Lessons: Binder pages	0		
measure. • What types of problems involve area? Knowledge Skills Students will know • the difference between area and perimeter. • rectangles with the same area do not necessarily have the same perimeter and vice versa. • find the perimeter of a polygon given the side lengths. • what types of problems involve area? • find the perimeter of a polygon given the side lengths. • rectangles with the same area do not necessarily have the same perimeter and vice versa. • find an unknown side length of a polygon. • exhibit rectangles with the same perimeter but different areas. • schibit rectangles with the same area but different perimeters. • solve real-world and mathematical problems involving perimeters of polygons. • solve real-world and mathematical problems involving perimeters of polygons. MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP6. Attend to precision. Resources • Math Expressions, 2018: Unit 5 • Supplemental Lessons: Binder pages	• perimeter is a linear measure and area is a square	• What types of problems involve perimeter?	
Knowledge Skills Students will know Students will know • the difference between area and perimeter. Students will be able to • rectangles with the same area do not necessarily have the same perimeter and vice versa. • find the perimeter of a polygon given the side lengths. • find an unknown side length of a polygon. • exhibit rectangles with the same perimeter but different areas. • exhibit rectangles with the same area but different areas. • exhibit rectangles with the same area but different perimeters. • solve real-world and mathematical problems involving perimeters of polygons. • solve real-world and mathematical problems involving perimeters of polygons. MP1. Make sense of problems and persevere in solving them. • Standards for Mathematical Practice MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP6. Attend to precision. • Math Expressions, 2018: Unit 5 • Supplemental Lessons: Binder pages	measure.		
 Students will know the difference between area and perimeter. rectangles with the same area do not necessarily have the same perimeter and vice versa. find an unknown side length of a polygon. exhibit rectangles with the same perimeter but different areas. exhibit rectangles with the same area but different perimeters. solve real-world and mathematical problems involving perimeters of polygons. MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP4. Model with mathematics. MP6. Attend to precision. Resources Math Expressions, 2018: Unit 5 Supplemental Lessons: Binder pages	Knowledge		
 MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP6. Attend to precision. Resources Math Expressions, 2018: Unit 5 Supplemental Lessons: Binder pages Assessment	 Students will know the difference between area and perimeter. rectangles with the same area do not necessarily 	 Students will be able to find the perimeter of a polygon given the side lengths. find an unknown side length of a polygon. exhibit rectangles with the same perimeter but different areas. exhibit rectangles with the same area but different perimeters. solve real-world and mathematical problems 	
MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP6. Attend to precision. • Math Expressions, 2018: Unit 5 • Supplemental Lessons: Binder pages Assessment	MP1. Make sense of problems and persevere in solving them.		
MP4. Model with mathematics. MP6. Attend to precision. • Math Expressions, 2018: Unit 5 • Supplemental Lessons: Binder pages Assessment		ning of others	
MP6. Attend to precision. Resources Math Expressions, 2018: Unit 5 Supplemental Lessons: Binder pages Assessment	e 1		
Resources • Math Expressions, 2018: Unit 5 • Supplemental Lessons: Binder pages Assessment	MP6. Attend to precision.		
Supplemental Lessons: Binder pages Assessment			
	•		
	Assessment		
Formative Assessment Summative Assessment	Formative Assessment	Summative Assessment	
Quick Check Quiz Unit Assessment	Quick Check Quiz	Unit Assessment	
Puzzled Penguin Mid-Unit Quiz	Puzzled Penguin	Mid-Unit Quiz	
Exit Slips Unit Projects	*	Unit Projects	
White Board Check	White Board Check		
Homework	Homework		

Data Literacy

A. Understand data-based questions and data collections 3.DL.A.1 Develop data-based questions and decide what data will answer the question. (e.g. "What size show does a 3rd grader wear?", "How many books does a 3rd grader read?")

3.DL.A.2 Collect student-centered data (e.g. collect data on students' favorite ice cream flavor) or use existing data to answer the data-based questions.

Understandings	Essential Questions
Students will understand • How is data collected?	
• What a data-based question is	• What is done with data once it is?
How to collect appropriate data	what is done with data once it is.
Knowledge	Skills
Students will know	Students will be able to
• The difference between a data-based question and a	Collect appropriate data
non-data-based question.	• Determine if data collected will answer statistical questions
Standards for Mat	hematical Practice
MP2. Reason abstractly and quantitatively. MP4. Model with mathematics	
 MP5. Use appropriate tools strategically Reso Math Expressions, 2018: Unit 1, Unit 4 	urces
Math Expressions, 2018: Unit 1, Unit 4	urces
Math Expressions, 2018: Unit 1, Unit 4	
Math Expressions, 2018: Unit 1, Unit 4 Asses	sment
Math Expressions, 2018: Unit 1, Unit 4 Asses Formative Assessment	sment Summative Assessment
Math Expressions, 2018: Unit 1, Unit 4 Asses Formative Assessment Quick Check Quiz	sment Summative Assessment Unit Assessment
Math Expressions, 2018: Unit 1, Unit 4 Asses Formative Assessment Quick Check Quiz Puzzled Penguin	sment Summative Assessment Unit Assessment Mid-Unit Quiz

Data Literacy B. Represent and interpret data

3.DL.B.3 Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve oneand two-step "how many more" and "how many less" problems using information presented in scaled bar graphs. *For example, draw a bar graph in which each square in a bar graph might represent 5 pets.*

3.DL.B.4. Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units— whole numbers, halves, or quarters.

Understandings	Essential Questions
 Students will understand different scales are needed to represent various 	 How can representing data help us to interpret it and draw conclusions? How can one determine the best representation to display data?
Knowledge	Skills
 Students will know the characteristics of picture graphs. the characteristics of bar graphs. the characteristics of a line plot. 	 Students will be able to draw a scaled picture graph to represent a data set with several categories. draw a scaled bar graph to represent a data set with several categories. solve one- and two-step "how many more" and "how many less" problems using information presented in scaled bar graphs (<i>e.g.</i>, <i>one square = 5 pets</i>). generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. use a line plot to show measurement data found with a ruler, where the horizontal scale is marked off in appropriate units – whole numbers, halves, or quarters.
Standards	for Mathematical Practice
MP1. Make sense of problems and persevere in so MP3. Construct viable arguments and critique the MP4. Model with mathematics. MP5. Use appropriate tools strategically.	reasoning of others.
Math Expressions, 2018: Unit 4	Resources
• Whath Expressions, 2010. Only	
	Assessment
Formative Assessment Quick Check Quiz Puzzled Penguin Exit Slips White Board Check Homework	Summative Assessment Unit Assessment Mid-Unit Quiz Unit Projects

Geometry

3.G.A.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

3.G.A2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as 1/4 of the area of the shape.*

Understandings	Essential Questions	
 Students will understand shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). 	• What characteristics define a polygon?	
Knowledge	Skills	
 Students will know shapes in different categories may share attributes (e.g., rhombuses and rectangles both have four sides). shared attributes can define a larger category (e.g., rhombuses and rectangles are part of the category called quadrilaterals. 	 Students will be able to recognize that rhombuses, rectangles, and squares are examples of quadrilaterals. draw examples of quadrilaterals that do not belong to any of these subcategories. partition shapes into parts with equal areas. express area of a part of a shape as a unit fraction of the whole. (<i>For example, partition a shape into 4 parts with equal area, and describe the area of each part as 1/4 of the area of the whole shape.</i>) 	
Standards for Mathematical Practice		
MP1. Make sense of problems and persevere in solvMP3. Construct viable arguments and critique the reMP4. Model with mathematicsMP7. Look for and make use of structure.MP8. Look for and express regularity in repeated res	easoning of others.	
R	esources	
Math Expressions, 2018: Unit 4, Unit 7		
Α	ssessment	
Formative Assessment Quick Check Quiz Puzzled Penguin Exit Slips White Board Check Homework	Summative Assessment Unit Assessment Mid-Unit Quiz Unit Projects	

Career Readiness, Life Literacies, and Key Skills

Career Readiness, Life Literacies, and Key Skills

Rapid advancements in technology and subsequent changes in the economy have created opportunities for individuals to compete and connect on a global scale. In this increasingly diverse and complex world, the successful entrepreneur or employee must not only possess the requisite education for specific industry pathways but also employability skills necessary to collaborate with others and manage resources effectively in order to establish and maintain stability and independence. This document outlines concepts and skills necessary for New Jersey's students to thrive in an ever-changing world. Intended for integration throughout all K–12 academic and technical content areas, the New Jersey Student Learning Standards- Career Readiness, Life Literacies, and Key Skills (NJSLS-CLKS) provides the framework for students to learn the concepts, skills, and practices essential to the successful navigation of career exploration and preparation, personal finances and digital literacy.

Mission

Career readiness, life literacies, and key skills education provides students with the necessary skills to make informed career and financial decisions, engage as responsible community members in a digital society, and to successfully meet the challenges and opportunities in an interconnected global economy.

Vision

An education in career readiness, life literacies, and key skills fosters a population that:

•Continually self-reflects and seeks to improve the essential life and career practices that lead to success;

•Uses effective communication and collaboration skills and resources to interact with a global society;

•Possesses financial literacy and responsibility at home and in the broader community;

•Plans, executes, and alters career goals in response to changing societal and economic conditions; and •Seeks to attain skill and content mastery to achieve success in a chosen career path.

Career Readiness, Life Literacies, and Key Skills Standards

- 9.4.5.CI.3: Participate in a brainstorming session with individuals with diverse perspectives to expand one's thinking about a topic of curiosity.
- 9.4.5.CT.1: Identify and gather relevant data that will aid in the problem-solving process.
- 9.4.5.CT.3: Describe how digital tools and technology may be used to solve problems.
- 9.4.5.CT.4: Apply critical thinking and problem-solving strategies to different types of problems such as personal, academic, community and global.
- 9.4.5.IML.3: Represent the same data in multiple visual formats in order to tell a story about the data.

Computer Science and Design Thinking

Computer Science and Design Thinking

New approaches necessary for solving the critical challenges that we face as a society will require harnessing the power of technology and computing. Rapidly changing technologies and the proliferation of digital information have permeated and radically transformed learning, working, and everyday life. To be well-educated, global-minded individuals in a computing-intensive world, students must have a clear understanding of the concepts and practices of computer science. As education systems adapt to a vision of students who are not just computer users but also computationally literate creators who are proficient in the concepts and practices of computer science and design thinking, engaging students in computational thinking and human-centered approaches to design through the study of computer science and technology serves to prepare students to ethically produce and critically consume technology.

Mission

Computer science and design thinking education prepares students to succeed in today's knowledge-based economy by providing equitable and expanded access to high-quality, standards-based computer science and technological design education.

Vision

All students have equitable access to a rigorous computer science and design thinking education. Students will benefit from opportunities to engage in high-quality technology programs that foster their ability to: • develop and apply computational and design thinking to address real-world problems and design creative solutions;

• engage as collaborators, innovators, and entrepreneurs on a clear pathway to success through postsecondary education and careers;

• navigate the dynamic digital landscape to become healthy, productive, 21st century global-minded individuals; and

• participate in an inclusive and diverse computing culture that appreciates and incorporates perspectives from people of different genders, ethnicities, and abilities.

Computer Science and Design Thinking Standards

- **8.1.5.IC.1:** Identify computing technologies that have impacted how individuals live and work and describe the factors that influenced the changes.
- **8.1.5.IC.2:** Identify possible ways to improve the accessibility and usability of computing technologies to address the diverse needs and wants of users.
- **8.1.5.DA.1:** Collect, organize, and display data in order to highlight relationships or support a claim.
- **8.1.5.DA.3:** Organize and present collected data visually to communicate insights gained from different views of the data.
- **8.1.5.AP.1:** Compare and refine multiple algorithms for the same task and determine which is the most appropriate.
- **8.1.5.AP.4:** Break down problems into smaller, manageable sub-problems to facilitate program development.
- **8.1.5.AP.5:** Modify, remix, or incorporate pieces of existing programs into one's own work to add additional features or create a new program.
- **8.2.5.ED.2:** Collaborate with peers to collect information, brainstorm to solve a problem, and evaluate all possible solutions to provide the best results with supporting sketches or models.
- **8.2.5.ITH.4:** Describe a technology/tool that has made the way people live easier or has led to a new business or career.

Grade 4

Interdisciplinary Connections

Mathematics is a unified body of knowledge whose concepts build upon each other. Connecting mathematical concepts includes linking ideas to related ideas learned previously.

Major emphasis should be given to ideas and concepts across mathematical content areas that help students see that mathematics is a web of closely connected ideas. Students need to connect their mathematical learning to appropriate real-world contexts. They need to create interest and maintain the interest after the novelty of the work has worn off.

Mathematics is the language of science and is greatly utilized in industry and business. It gives us the power to solve difficult real-world problems, but also helps us to understand how the universe operates.

Every mathematics teacher needs to make students unafraid of the subject by convincing the students of the usefulness of learning mathematics in their daily lives and for higher studies. The world today, which leans more and more heavily on Science and Technology, demands more from mathematics. Tomorrow's world will, no doubt, make still greater demands from mathematics.

Interdisciplinary Connections for Grade 4

Literacy: (RL.4.1, RI.4.1, RI.4.4)

~ The Beautiful Oops

- Read The Beautiful Oops by Barney Saltzberg.
- Discuss the story with students. Are mistakes okay to make? Why?
- Have students talk about a time when they made a mistake, but it turned out to be better than expected.
- ~ Grandfather Tang's Story
 - Introduce lesson by reading *Grandfather Tang's Story* by Ann Tompert.
 - Follow the attached lesson in the Supplemental Section.
- ~ Great Estimations
 - Introduce lesson by reading Great Estimations by Bruce Goldstone
 - Follow attached lesson in the Supplemental Section

~ Zachary Zormer Book

- Introduce lesson by reading Zachary Zormer by Joanne Reisberg
- Discuss the book as you read.
- ~Vocabulary Poster Project
 - See the attached document in the Supplemental Section for directions and rubric.

Climate Change for Grade 4

With the adoption of the 2020 New Jersey Student Learning Standards (NJSLS), New Jersey became the first state in the nation to include climate change across content areas. The goal of inclusion of climate change education implementation is to foster generations of New Jersey students that can analyze, question, interpret, to think independently, and bring critical deduction to fulfill, and to lead in jobs created by burgeoning industries of the future green economy.

- **4.OA.A.3** Students may, knowing that energy and fuels are derived from natural resources and that their uses affect the climate, use the four operations to solve multi-step word problems posed with whole numbers, having whole-number answers and that are based on energy, fuels, and natural resources.
 - Students will solve word problems related to fossil fuels, energy usage and the consumption of natural resources.
- **4.DL.B.5** Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Solve problems involving addition and subtraction of fractions by using information presented in line plots. *For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection.*

- **4.DL.B.5** Students may, knowing that energy and fuels are derived from natural resources and that their uses affect the climate, make a line plot to display a data set of measurements in fractions of a unit.
- Students, being provided historical climate data, will create line plot showing global temperature, as well as temperature for a specific location.

New Jersey Student Learning Standards (NJSLS)

In Grade 4, instructional time should focus on three critical areas: (1) developing understanding and fluency with multi-digit multiplication, and developing understanding of dividing to find quotients involving multi-digit dividends; (2) developing an understanding of fraction equivalence, addition and subtraction of fractions with like denominators, and multiplication of fractions by whole numbers; (3) understanding that geometric figures can be analyzed and classified based on their properties, such as having parallel sides, perpendicular sides, particular angle measures, and symmetry.

(1) Students generalize their understanding of place value to 1,000,000, understanding the relative sizes of numbers in each place. They apply their understanding of models for multiplication (equal-sized groups, arrays, area models), place value, and properties of operations, in particular the distributive property, as they develop, discuss, and use efficient, accurate, and generalizable methods to compute products of multi-digit whole numbers. Depending on the numbers and the context, they select and accurately apply appropriate methods to estimate or mentally calculate products. They develop fluency with efficient procedures for multiplying whole numbers; understand and explain why the procedures work based on place value and properties of operations; and use them to solve problems. Students apply their understanding of models for division, place value, properties of operations, and the relationship of division to multiplication as they develop, discuss, and use efficient, accurate, and generalizable procedures to find quotients involving multi-digit dividends. They select and accurately apply appropriate methods to estimate and mentally calculate quotients, and interpret remainders based upon the context.

(2) Students develop understanding of fraction equivalence and operations with fractions. They recognize that two different fractions can be equal (e.g., 15/9 = 5/3), and they develop methods for generating and recognizing equivalent fractions. Students extend previous understandings about how fractions are built from unit fractions, composing fractions from unit fractions, decomposing fractions into unit fractions, and using the meaning of fractions and the meaning of multiplication to multiply a fraction by a whole number.
(3) Students describe, analyze, compare, and classify two-dimensional shapes. Through building, drawing, and analyzing two-dimensional shapes, students deepen their understanding of properties of two-dimensional objects and the use of them to solve problems involving symmetry.

Operations & Algebraic Thinking A. Use the four operations with whole numbers to solve problems.

4.OA.A.1 Interpret a multiplication equation as a comparison, e.g., interpret $35 = 5 \times 7$ as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.

4.OA.A.2 Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.¹

4.OA.A.3 Solve multi-step word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

Understandings		Essential Questions
 Students will understand multiplication involving whole numbers (gr the answer become larger than either numb when solving word problems, remainders n Knowledge 	ber. nust be interpreted	and division in the answer? Skills
 Students will know sometimes one needs to multiply or divide numbers to find an answer. 	 as a statemen Represent ver equations. Multiply to so by using draw represent the Divide to solv using drawing represent the Distinguish n Solve multi-s number answ remainders m Represent wo unknown qua Assess the reat 	altiplication equation as a comparison, e.g., interpret 35 = 5 x 7 t that 35 is 5 times as many as 7 and 7 times as many as 5. -bal statements of multiplicative comparisons as multiplication olve word problems involving multiplicative comparison, e.g., vings and equations with a symbol for the unknown number to problem. ve word problems involving multiplicative comparison, e.g., by gs and equations with a symbol for the unknown number to problem. nultiplicative comparison from additive comparison. tep word problems posed with whole numbers and having whole ers using the four operations, including problems in which ust be interpreted. rd problems using equations with a letter standing for the
Standards for Mathematical Practice		
MP2. Reason abstractly and quantitatively.MP3.MP3. Construct viable arguments and critique the reasoningMP3.		IP4. Model with mathematics.IP5. Use appropriate tools strategically.IP7. Look for and make use of structure.IP8. Look for and express regularity in repeated
reas Resources		easoning. S

• Math Expressions, 2018: Unit 1, Unit 2, Unit 3, Unit 4

Assessment		
Formative Assessment	Summative Assessment	
Diagnostic Checks	Performance Task	
Puzzled Penguin	Unit Assessment	
Exit Slips	Mid-Unit Quiz	
Quick Quiz		
Fluency Check		

Operations & Algebraic Thinking B. Gain familiarity with factors and multiples

4.OA.B.4 Find all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1–100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1–100 is prime or composite.

Understanding	Essential Questions			
 Students will understand factors of a number are less than or equal to the number. multiples of a number are greater than or equal to the number. the determination of prime or composite is unrelated to the size of the number. 	 Why do we need factors and multiples? Why do we need to distinguish a number as being prime or composite? How does finding factors or multiples of a number help us to solve problems? 			
Knowledge	Skills			
 Students will know a factor is one of 2 or more numbers that form a product when multiplied together . a multiple is a number which is a product of some specified number and another number. a prime number is a number that has only two factors, 1 and itself. a composite number is a number that has more than 2 factors. a whole number is a multiple of each of its factors. 	 Students will be able to Find all factor pairs for a whole number in the range 1 – 100. Determine whether a given whole number in the range 1 – 100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1 – 100 is prime or composite. 			
Standards for Mathematical Practice				
MP1. Make sense of problems and persevere in solving them.MP2. Reason abstractly and quantitatively.MP6. Attend to precision.MP7. Look for and make use of structure.MP8. Look for and express regularity in repeated reasoning.				
Resources				
• Math Expressions, 2018: Unit 4				
As	sessment			
Formative Assessment Diagnostic Checks Puzzled Penguin Exit Slips	Summative Assessment Performance Task Unit Assessment Mid-Unit Quiz			

Quick Quiz Fluency Check

Operations & Algebraic Thinking C. Generate and analyze patterns

4.OA.C.5 Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. For example, given the rule "Add 3" and the starting number *l*, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.

Understanding	Essential Questions	
Students will understand		
• patterns have units that repeat over	• How does recognizing a pattern help one to solve problems?	
and over.the unit in a pattern must be	• Why does one need to look for patterns?	
identified.		
Knowledge	Skills	
Students will know	Students will be able to	
• pattern types, e.g., ABABAB	• Generate a pattern that follows a given rule.	
• patterns can be made from numbers,	• Identify apparent features of the pattern that were not explicit	
shapes, letters, etc.	in the rule itself.	
Standards for Mathematical Practice		
MP1. Make sense of problems and persevere in solving them.		
MP2. Reason abstractly and quantitatively.		
MP6. Attend to precision.		
MP7. Look for and make use of structure.		
MP8. Look for and express regularity in r	epeated reasoning.	
	Resources	
• Math Expressions, 2018: Unit 4		
Assessment		
Formative Assessment	Summative Assessment	
Diagnostic Checks	Performance Task	
Puzzled Penguin	Unit Assessment	
Exit Slips	Mid-Unit Quiz	
Quick Quiz		
Fluency Check		

Numbers and Operations in Base Ten¹ A. Generalize place value understanding for multi-digit whole numbers.

4.NBT.A.1 Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. For example, recognize that $700 \div 70 = 10$ by applying concepts of place value and division.

4.NBT.A.2 Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form. Compare two multi-digit numbers based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.

4.NBT.A.3 Use place value understanding to round multi-digit whole numbers to any place.

¹Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000

Understanding	Essential Questions
 Students will understand place value is used to round numbers. place value can be used to compare and order numbers. 	• What does knowing place value help us to do?
Knowledge	Skills
 Students will know how a base-ten numeral is related to the numeral name and the expanded form. that in a multi-digit whole number, a digit in one place represents ten times what it represents to its right. 	 Students will be able to read multi-digit whole numbers using base-ten numerals, numeral names, and expanded form. write multi-digit whole numbers using base-ten numerals, numeral names, and expanded form. compare two multi-digit numbers based on meanings of the digits in each place, using <, =, and > symbols. use place-value understanding to round multi-digit whole numbers to any place.
Standards for Mathematical Practice	
MP1. Make sense of problems and persevere in solving them.MP2. Reason abstractly and quantitatively.MP3. Construct viable arguments and critique th reasoning of others.	MP4. Model with mathematics.MP5. Use appropriate tools strategically.MP6. Attend to precision.MP7. Look for and make use of structure.
	Resources

• Math Expressions, 2018: Unit 1, Unit 2

Assessment		
Formative Assessment Diagnostic Checks Puzzled Penguin Exit Slips Quick Quiz Fluency Check	Summative Assessment Performance Task Unit Assessment Mid-Unit Quiz	

Numbers and Operations in Base Ten¹

B. Use place value understanding and properties of operations to perform multi-digit arithmetic.

4.NBT.B.4 With accuracy and efficiency, add and subtract multi-digit whole numbers using the standard algorithm.

4.NBT.B.5 Multiply a whole number of up to four digits by a one-digit whole number, and multiply two twodigit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

4.NBT.B.6 Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

¹Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000

Understanding		Essential Questions	
 Students will understand the standard algorithm is one way to get the answer to an addition or subtraction problem. one should use an alternate algorithm to check the answer to a problem. place value helps to understand the appropriate size of an answer. 		 How are strategies useful in solving computation problems? Why does it help to know inverse relationships? 	
Knowledge		Ski	lls
 Students will know addition and subtraction are inverse operations. multiplication and division are inverse operations. 	 Students will be able to fluently add multi-digit whole num fluently subtract multi-digit whole : multiply a whole number of up to fe multiply two two-digit numbers. find whole-number quotients an dividends and one-digit divisors. 		bers using the standard algorithm. numbers using the standard algorithm. our digits by a one-digit whole number. d remainders with up to four-digit by using equations, rectangular arrays,
Standards for Mathematical Pr		ractice	
MP1. Make sense of problems a solving them.MP2. Reason abstractly and qua MP3. Construct viable argument the reasoning of others.	antitatively.	MP4. Model with ma MP5. Use appropriate MP6. Attend to precis MP7. Look for and m	e tools strategically. sion.
Resources			
• Math Expressions, 2018: Unit 1, Unit 2, Unit 3, Unit 4			
Assessment			
Formative Assessment Diagnostic Checks Puzzled Penguin Exit Slips Quick Quiz Fluency Check		Unit As	essment nance Task ssessment nit Quiz

Number & Operations - Fractions¹ A. Extend understanding of fraction equivalence and ordering

4.NF.A.1 Explain why a fraction a/b is equivalent to a fraction $(n \times a)/(n \times b)$ by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

4.NF.A.2 Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as 1/2. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model.

¹ Grade 4 expectations in this domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, 100.

Understanding		Essential Questions	
Students will understand			
 equivalent fractions represent the same amount of a whole. 		• Why does one need to use fractions?	
	on that	• Why does one need to find equivalent fractions?	
• fraction comparisons are only valid wh refer to the same whole.	len they		
 in order to find the fraction equivalent 	to one		
half, the numerator must be the denomination			
divided by 2; or the denominator must			
times the numerator.	002		
Knowledge		Skills	
Students will know		Students will be able to	
• the same number must multiply the	• iden	tify equivalent fractions.	
numerator and denominator in order	• gen	erate equivalent fractions.	
for fractions to be equivalent.	• exp	lain fractions that are equivalent through visual models.	
· ····································		pare two fractions using a benchmark fraction.	
compare the methods aching a		pare two fractions using common numerators or	
		ominators.	
greater than; and "=" means equal to.			
Standards for Mathematical Practice			
MP1. Make sense of problems and persevere in solving them.		ring them.	
MP2. Reason abstractly and quantitatively.			
MP4. Model with mathematics.			
MP5. Use appropriate tools strategically.			
MP7. Look for and make use of structure.			
Resources			
Math Expressions, 2018: Unit 6, Unit 7			
Assessment			
Formative Assessment		Summative Assessment	
Diagnostic Checks		Performance Task	
Puzzled Penguin		Unit Assessment	
Exit Slips		Mid-Unit Quiz	
Quick Quiz			
Fluency Check			

Number & Operations - Fractions¹ B. Build fractions from unit fractions by applying and extending previous understanding of operations on whole numbers.

4.NF.B.3 Understand a fraction a/b with a > 1 as a sum of fractions 1/b.

- a. Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.
- b. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. *Examples:* 3/8 = 1/8 + 1/8 + 1/8; 3/8 = 1/8 + 2/8; 21/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8.
- c. Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction.
- d. Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.

4.NF.B.4 Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.

- a. Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to represent 5/4 as the product $5 \times (1/4)$, recording the conclusion by the equation $5/4 = 5 \times (1/4)$.
- b. Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as 6/5. (In general, $n \times (a/b) = (n \times a)/b$.)
- c. Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. *For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?*

¹ Grade 4 expectations in this domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, 100.

Understanding		Essential Questions
 Students will understand a fraction (with a numerator greater than 1) i of unit fractions, e.g. 3/7 = 1/7 + 1/7 + 1/7. addition and subtraction of fractions is joining separating parts referring to the same whole. a fraction <i>a/b</i> is a multiple of 1/<i>b</i>. a multiple of a/b is a multiple of 1/b. 	ng and	 How operations are allowed with fractions? When would one need to add, subtract, multiply, or divide a fraction?
Knowledge		Skills
 Students will know fractions must have common denominators in order to be added or subtracted. when adding or subtracting fractions with like denominators, one must add or subtract the numerators and keep the denominator the same. mixed numbers are multiples of fractions. 	 decomp than one justify d add mix subtract solve w subtract having l multiply 	Il be able to ose a fraction into the sum of fractions in more e way. lecompositions. ted numbers with like denominators. ord problems involving addition and tion of fractions referring to the same whole and like denominators. y a fraction by a whole number. ord problems involving multiplication of a

fraction by a whole number.

Standards for Mathematical Practice			
MP1. Make sense of problems and persever	MP1. Make sense of problems and persevere in solving them.		
MP2. Reason abstractly and quantitatively.			
MP4. Model with mathematics.			
MP5. Use appropriate tools strategically.			
MP7. Look for and make use of structure.			
	Resources		
• Math Expressions, 2018: Unit 6			
	Assessment		
Formative Assessment Summative Assessment			
Diagnostic Checks	Performance Task		
Puzzled Penguin	Unit Assessment		
Exit Slips	Mid-Unit Quiz		
Quick Quiz			
Fluency Check			

Number & Operations - Fractions¹ C. Understand decimal notation for fractions, and compare decimal fractions.

4.NF.C.5 Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and $100.^2$ For example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100.

4.NF.C.6 Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.

4.NF.C./7 Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual model.

¹ Grade 4 expectations in this domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, 100. ² Students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators in

general. But addition and subtraction with unlike denominators in general is not a requirement at this grade.

Essential Questions		
Essential Questions d. • Why does one need to change a fraction to a decimal? 10 or 100 can • When is it easier to use the decimal form of a fraction? • When is it easier to use the decimal form of a fraction? • Why would decimal forms of a fraction need to be compared? Students will be able to • find an fraction with a denominator of 100 for a fraction with a denominator of 10. • add two fractions with respective denominators 10 and 100. • write fractions with denominators 10 or 100 in decimal form. • compare two decimals to hundredths by reasoning about their size.		
two decimals using the symbols >, =, or <, and justify the ons. Mathematical Practice		
MP1. Make sense of problems and persevere in solving them.MP2. Reason abstractly and quantitatively.MP4. Model with mathematics.MP5. Use appropriate tools strategically.MP7. Look for and make use of structure.		
Resources		
• Math Expressions, 2018: Unit 7		
Assessment		
Summative Assessment Performance Task Unit Assessment Mid-Unit Quiz		

Measurement

A. Solve problems involving measurement and conversion of measurement from a larger unit to a smaller unit.

4.M.A.1 Know relative sizes of measurement units within one system of units including km, m , cm, mm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a two-column table. For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36), ...

4.M.A.2 Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.

4.M.A.3 Apply the area and perimeter formulas for rectangles in real world and mathematical problems. *For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor.*

Understandings	Essential Questions
 Students will understand the size of the unit used to measure has an effect on the number of units in the answer. area and perimeter measure different things therefore the types of label on the answers are different. the region covered by square units in an array is the same as the area of the rectangle. 	 What can be measured? Why does one need to measure things?
Knowledge	Skills
 Students will know relative sizes of measurement units within one system of units including km, m, cm, mm; kg, g; lb, oz.; l, ml; hr, min, sec. the larger the unit used to measure, the smaller the number of units in the answer and vice versa. area of a rectangle is equal to the length x the width (A = l x w) 	 Students will be able to express measurements in a larger unit in terms of a smaller unit. record measurement equivalents in a two-column table. find the area of a rectangle using the formula. find the perimeter of a rectangle using the formula.
Standards for Mathematical Practice	
MP1. Make sense of problems and persevere in solving them.MP2. Reason abstractly and quantitatively.MP4. Model with mathematics.MP5. Use appropriate tools strategically.MP7. Look for and make use of structure.	
Resources	
• Math Expressions, 2018: Unit 1, Unit 2, Unit 4, Unit 5, Unit 6, Unit 7	

Assessment		
Formative Assessment Summative Assessment		
Diagnostic Checks	Performance Task	
Puzzled Penguin	Unit Assessment	
Exit Slips	Mid-Unit Quiz	
Quick Quiz		
Fluency Check		

Measurement

B. Geometric measurement: Understand concepts of angle and measure angles.

4.M.B.4 Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle measurement:

- a. An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through 1/360 of a circle is called a "one-degree angle," and can be used to measure angles.
- b. An angle that turns through n one-degree angles is said to have an angle measure of n degrees.

4.M.B.5 Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure.

4.M.B.6 Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure.

Understanding		Essential Questions	
Students will understand		• Why would one need to measure an	
• the measure of an angle is the measure of the turn.		angle?	
Knowledge		Skills	
 Students will know that an angle is formed wherever two rays share a common endpoint. angle measure is additive. an angle decomposed into non-overlapping parts is the sum of the measure of each parts. an angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. an angle that turns through 1/360 of a circle is called a "one-degree angle," and can be used to measure angles. an angle that turns through <i>n</i> one-degree angles is said to have an angle measure of <i>n</i> degrees. 		 Students will be able to measure angles in whole-number degrees using a protractor. sketch angles of specified measure. solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems. 	
MP1. Make sense of problems and persevere in solving	Standards for Mathematical Practice MP1 Make sense of problems and persevere in solving them		
MP3. Construct viable arguments and critique the reas	-		
MP5. Use appropriate tools strategically.			
MP7. Look for and make use of structure.			
R	esources		
• Math Expressions, 2018: Unit 8			
Assessment			
Formative Assessment	Summativ	ve Assessment	
Diagnostic Checks	Perfo	formance Task	
Puzzled Penguin	Unit	t Assessment	
Exit Slips	Mid-	-Unit Quiz	
Quick Quiz			
Fluency Check			

Data Literacy A. Organize data and understand visualizations¹

4.DL.A.1 Create data-based questions, generate ideas based on the questions, and then refine the questions.

4.DL.A.2 Develop strategies to collect various types of data and organize data digitally.

4.DL.A.3 Understand that subsets of data can be selected and analyzed for a particular purpose.

4.DL.A.4 Analyze visualizations of a single data set, share explanations and draw conclusions that the data supports.

Analysis of data and visualizations at this grade excludes ratio, rate, proportion and percentages. These concepts are introduced in Grade 6.

Understanding	Essential Questions		
Students will understand			
Data is essential to answer questions	• How is a data-based question written?		
• That data can be broken down and analyzed	• How is data collected?		
	• Why is data collected?		
Knowledge	Skills		
Students will know	Students will be able to		
• That data can be broken down	Analyze data		
• That data can be used to draw conclusions	Share and draw conclusions about data		
• That data can be analyzed and presented.			
Standards for M	athematical Practice		
MP2. Reason abstractly and quantitatively.			
MP3. Construct viable arguments and critique the reasoning of others.			
	MP4. Model with mathematics		
MP5. Use appropriate tools strategically			
Res	ources		
Math Expressions, 2018: Unit 5, Unit 6, U nit 7			
Asso	essment		
Formative Assessment	Summative Assessment		
Diagnostic Checks	Performance Task		
Puzzled Penguin	Unit Assessment		
Exit Slips	Mid-Unit Quiz		
Quick Quiz			
Fluency Check			

Data Literacy B. Represent and interpret data

4.DL.B.5 Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Solve problems involving addition and subtraction of fractions by using information presented in line plots. *For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection.*

Understanding	Essential Questions	
 Students will understand a line plot is a visual display of data used to help see trends in the data. 	When would a line plot be used?Why does one need to display data graphically?	
Knowledge	Skills	
 Students will know the scale of a line plot must be equally spaced as in a number line. the scale of a line plot can contain fractions. 	 Students will be able to make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). solve problems involving addition and subtraction of fractions by using information presented in line plots. 	
Standards for M	athematical Practice	
MP1. Make sense of problems and persevere in solving them.MP2. Reason abstractly and quantitatively.MP4. Model with mathematics.MP5. Use appropriate tools strategically.MP7. Look for and make use of structure.		
	sources	
• Math Expressions, 2018: Unit 5, Unit 6, Unit 7		
Assessment		
Formative Assessment Diagnostic Checks Puzzled Penguin Exit Slips Quick Quiz Fluency Check	Summative Assessment Performance Task Unit Assessment Mid-Unit Quiz	

Geometry

A. Draw and identify lines and angles, and classify shapes by properties of their lines and angles.

4.G.A.1 Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures.

4.G.A.2 Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.

4.G.A.3 Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry.

Understanding	Essential Questions	
 Students will understand characteristics of a figure enables one to identify it by a name. 	 Why does one need to classify shapes? Why does one need to identify lines of symmetry? 	
Knowledge	Skills	
 Students will know a right triangle is a category of triangles. a line of symmetry is such that the figure can be folded along the line into matching parts. 	 Students will be able to draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. identify these in two-dimensional figures. classify two-dimensional figures based on properties of parallel and perpendicular lines and sizes of angles. identify right triangles. identify line-symmetric figures. draw lines of symmetry. 	
Standard	s for Mathematical Practice	
MP1. Make sense of problems and persevere in solving them.MP3. Construct viable arguments and critique the reasoning of others.MP5. Use appropriate tools strategically.MP7. Look for and make use of structure.		
	Resources	
Math Expressions, 2018: Unit 8		
Assessment		
Formative Assessment Quick Quiz Fluency Check Diagnostic Checks Puzzled Penguin Exit Slips	Summative Assessment Performance Task Unit Assessment Mid-Unit Quiz	

Career Readiness, Life Literacies, and Key Skills

Career Readiness, Life Literacies, and Key Skills

Rapid advancements in technology and subsequent changes in the economy have created opportunities for individuals to compete and connect on a global scale. In this increasingly diverse and complex world, the successful entrepreneur or employee must not only possess the requisite education for specific industry pathways but also employability skills necessary to collaborate with others and manage resources effectively in order to establish and maintain stability and independence. This document outlines concepts and skills necessary for New Jersey's students to thrive in an ever-changing world. Intended for integration throughout all K–12 academic and technical content areas, the New Jersey Student Learning Standards- Career Readiness, Life Literacies, and Key Skills (NJSLS-CLKS) provides the framework for students to learn the concepts, skills, and practices essential to the successful navigation of career exploration and preparation, personal finances and digital literacy.

Mission

Career readiness, life literacies, and key skills education provides students with the necessary skills to make informed career and financial decisions, engage as responsible community members in a digital society, and to successfully meet the challenges and opportunities in an interconnected global economy.

Vision

An education in career readiness, life literacies, and key skills fosters a population that:

•Continually self-reflects and seeks to improve the essential life and career practices that lead to success;

•Uses effective communication and collaboration skills and resources to interact with a global society;

•Possesses financial literacy and responsibility at home and in the broader community;

•Plans, executes, and alters career goals in response to changing societal and economic conditions; and •Seeks to attain skill and content mastery to achieve success in a chosen career path.

Career Readiness, Life Literacies, and Key Skills Standards

- 9.4.5.CI.3: Participate in a brainstorming session with individuals with diverse perspectives to expand one's thinking about a topic of curiosity.
- 9.4.5.CT.1: Identify and gather relevant data that will aid in the problem-solving process.
- 9.4.5.CT.3: Describe how digital tools and technology may be used to solve problems.
- 9.4.5.CT.4: Apply critical thinking and problem-solving strategies to different types of problems such as personal, academic, community and global.
- 9.4.5.IML.3: Represent the same data in multiple visual formats in order to tell a story about the data.

Computer Science and Design Thinking

Computer Science and Design Thinking

New approaches necessary for solving the critical challenges that we face as a society will require harnessing the power of technology and computing. Rapidly changing technologies and the proliferation of digital information have permeated and radically transformed learning, working, and everyday life. To be well-educated, global-minded individuals in a computing-intensive world, students must have a clear understanding of the concepts and practices of computer science. As education systems adapt to a vision of students who are not just computer users but also computationally literate creators who are proficient in the concepts and practices of computer science and design thinking, engaging students in computational thinking and human-centered approaches to design through the study of computer science and technology serves to prepare students to ethically produce and critically consume technology.

Mission

Computer science and design thinking education prepares students to succeed in today's knowledge-based economy by providing equitable and expanded access to high-quality, standards-based computer science and technological design education.

Vision

All students have equitable access to a rigorous computer science and design thinking education. Students will benefit from opportunities to engage in high-quality technology programs that foster their ability to: • develop and apply computational and design thinking to address real-world problems and design creative solutions;

• engage as collaborators, innovators, and entrepreneurs on a clear pathway to success through postsecondary education and careers;

• navigate the dynamic digital landscape to become healthy, productive, 21st century global-minded individuals; and

• participate in an inclusive and diverse computing culture that appreciates and incorporates perspectives from people of different genders, ethnicities, and abilities.

Computer Science and Design Thinking Standards

- **8.1.5.IC.1:** Identify computing technologies that have impacted how individuals live and work and describe the factors that influenced the changes.
- **8.1.5.IC.2:** Identify possible ways to improve the accessibility and usability of computing technologies to address the diverse needs and wants of users.
- **8.1.5.DA.1:** Collect, organize, and display data in order to highlight relationships or support a claim.
- **8.1.5.DA.3:** Organize and present collected data visually to communicate insights gained from different views of the data.
- **8.1.5.AP.1:** Compare and refine multiple algorithms for the same task and determine which is the most appropriate.
- **8.1.5.AP.4:** Break down problems into smaller, manageable sub-problems to facilitate program development.
- **8.1.5.AP.5:** Modify, remix, or incorporate pieces of existing programs into one's own work to add additional features or create a new program.
- **8.2.5.ED.2:** Collaborate with peers to collect information, brainstorm to solve a problem, and evaluate all possible solutions to provide the best results with supporting sketches or models.
- **8.2.5.ITH.4:** Describe a technology/tool that has made the way people live easier or has led to a new business or career.

Fifth Grade

Interdisciplinary Connections

Mathematics is a unified body of knowledge whose concepts build upon each other. Connecting mathematical concepts includes linking ideas to related ideas learned previously.

Major emphasis should be given to ideas and concepts across mathematical content areas that help students see that mathematics is a web of closely connected ideas. Students need to connect their mathematical learning to appropriate real-world contexts. They need to create interest and maintain the interest after the novelty of the work has worn off.

Mathematics is the language of science and is greatly utilized in industry and business. It gives us the power to solve difficult realworld problems, but also helps us to understand how the universe operates.

Every mathematics teacher needs to make students unafraid of the subject by convincing the students of the usefulness of learning mathematics in their daily lives and for higher studies. The world today, which leans more and more heavily on Science and Technology, demands more from mathematics. Tomorrow's world will, no doubt, make still greater demands from mathematics.

Interdisciplinary Connections for Grade 5

See Me in Space-A Walk through the Solar System

<u>SUBJECT AREA: Science (5-ESSI-1)</u>

A practice in scientific notation, measurement, and scale distances, this lesson plan integrates mathematics into the science curriculum. Students will apply knowledge of the properties, movements, and locations of objects in our solar system. We hope that our students will be able to recognize and elaborate on each of the planets and be able to transfer knowledge from one curricular area to the next.

http://www.learnnc.org/lp/pages/3091

Myahsteward.weebly.com

Be the Author of Your Own Problem!

SUBJECT AREA: ELA- Writing, Reading (W.5.2.D)

Students will become authors of their own division word problems. Before writing students will brainstorm ideas and wording for their word problems. Word problems can be centered around a grade level related theme. (read-aloud book, science unit, ss unit, season etc). Students will need to write a division word problem that includes a remainder in the quotient. The final result should include: word problem, number sentence, illustration, solution, and an explanations of what they did with the remainder and why.

5th Grade Shape Sorter

SUBJECT AREA: Math, Science, ELA-Writing and Presenting (NJSLA.SL4, NJSLA.SL5)

Students will work in small groups to design a machine that sorts triangles and quadrilaterals. They are required to draw, describe and present their machines. Their drawing is a detailed diagram that explains how their machine sorts the shapes. The written response is a description of what happens with two different shapes as they travel through the machine. Presentations are an overview of their machine, where both teacher and classmates can ask questions.

Google Doc- directions

Interdisciplinary Connections (continued)

Fairytale Word Problems

1

SUBJECT AREA: ELA- Writing, (W.5.3)

This lesson is a hands-on math lesson that is meant to stimulate critical thinking as well as reinforce vocabulary that is necessary to be able to create and solve word problems both on paper and on the computer. Students will be able to generate and utilize a list of math vocabulary words by identifying which operations they reflect and by using them when they create their own word problems incorporating fairytales as their LA focus. Students will be able to work cooperatively with a partner to participate in creating their own word problem and showing the work for a class book. They will first sketch out this page and then be asked to input it using Google Slides. The students will then need to present their word problems to the class via slideshow on Google Slides. Google Docs- directions & rubric

Climate Change for Grade 5

With the adoption of the 2020 New Jersey Student Learning Standards (NJSLS), New Jersey became the first state in the nation to include climate change across content areas. The goal of inclusion of climate change education implementation is to foster generations of New Jersey students that can analyze, question, interpret, to think independently, and bring critical deduction to fulfill, and to lead in jobs created by burgeoning industries of the future green economy.

- **5.G.A.2** Represent real world and mathematical problems by graphing points in the first quadrant of the coordinate plane, and interpret coordinate values of points in the context of the situation.
- **5.DL.A.3** Collect and clean data to be analyzable (e.g., make sure each entry is formatted correctly, deal with missing or incomplete data.)
- **5.DL.A.4** Using appropriate visualizations (i.e. double line plot, double bar graph), analyze data across samples.
 - Students will work through the lesson "What do these numbers mean?". As they work through, they will graph the data they find during the course of the lesson. They will also answer questions about the data they collected.

New Jersey Student Learning Standards (NJSLS)

In Grade 5, instructional time should focus on three critical areas: (1) developing fluency with addition and subtraction of fractions, and developing understanding of the multiplication of fractions and of division of fractions in limited cases (unit fractions divided by whole numbers and whole numbers divided by unit fractions); (2) extending division to 2-digit divisors, integrating decimal fractions into the place value system and developing understanding of operations with decimals to hundredths, and developing fluency with whole number and decimal operations; and (3) developing understanding of volume.

(1) Students apply their understanding of fractions and fraction models to represent the addition and subtraction of fractions with unlike denominators as equivalent calculations with like denominators. They develop fluency in calculating sums and differences of fractions, and make reasonable estimates of them. Students also use the meaning of fractions, of multiplication and division, and the relationship between multiplication and division to understand and explain why the procedures for multiplying and dividing fractions make sense. (Note: this is limited to the case of dividing unit fractions by whole numbers and whole numbers by unit fractions.)

(2) Students develop understanding of why division procedures work based on the meaning of base-ten numerals and properties of operations. They finalize fluency with multi-digit addition, subtraction, multiplication, and division. They apply their understandings of models for decimals, decimal notation, and properties of operations to add and subtract decimals to hundredths. They develop fluency in these computations, and make reasonable estimates of their results. Students use the relationship between decimals and fractions, as well as the relationship between finite decimals and whole numbers (i.e., a finite decimal multiplied by an appropriate power of 10 is a whole number), to understand and explain why the procedures for multiplying and dividing finite decimals make sense. They compute products and quotients of decimals to hundredths efficiently and accurately.

(3) Students recognize volume as an attribute of three-dimensional space. They understand that volume can be measured by finding the total number of same-size units of volume required to fill the space without gaps or overlaps. They understand that a 1-unit by 1-unit by 1-unit cube is the standard unit for measuring volume. They select appropriate units, strategies, and tools for solving problems that involve estimating and measuring volume. They decompose three-dimensional shapes and find volumes of right rectangular prisms by viewing them as decomposed into layers of arrays of cubes. They measure necessary attributes of shapes in order to determine volumes to solve real world and mathematical problems.

Operations and Algebraic Thinking A. Write and interpret numerical expressions.

5.OA.A.1 Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.

5.OA.A.2 Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and 7, then multiply by 2" as $2 \times (8 + 7)$. Recognize that $3 \times (18932 + 921)$ is three times as large as 18932 + 921, without having to calculate the indicated sum or product.

Understandings	Essential Questions
Students will understand	
• the order of operations affects the value of the	
answer.	• Why is there an order to follow to compute answers?
Knowledge	Skills
Students will know	Students will be able to
• the order of operations is as follows:	• use the order of operations to find answers to
• parentheses	expressions.
• exponents	• write simple expressions that record calculations with
• multiplication and division, left to right	numbers.
• addition and subtraction, left to right.	• interpret numerical expressions without evaluating
	them.
Standards for Ma	athematical Practice
MP2. Reason abstractly and quantitatively.	
MP3. Construct viable arguments and critique the reas	oning of others.
MP6. Attend to precision.	C C C C C C C C C C C C C C C C C C C
	sources
• Math Expressions, 2018: Unit 7	
Ass	essment
Formative Assessment	Summative Assessment
Fluency Check	End of Unit Assessment
Puzzled Penguin	Quick Quiz
Homework	Unit Project
Check for understanding	Performance Assessment
Exit ticket	
Strategy Check	
$\mathbf{D}_{\mathbf{r}}$	1

Personal Math Trainer

Operations and Algebraic Thinking B. Analyze patterns and relationships

5.OA.B.3 Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane. For example, given the rule "Add 3" and the starting number 0, and given the rule "Add 6" and the starting number 0, generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so.

Understandings	Essential Questions	
 Students will understand patterns can be put together to generate new patterns. 	• How are the coordinate points related to patterns?	
Knowledge	Skills	
Students will know	Students will be able to	
• that to determine if there is a pattern present in a set	• generate patterns from other patterns.	
of numbers, one can look for constant change between the variables.	• graph ordered pairs generated by the pattern on a coordinate plane.	
Standards for Ma	thematical Practice	
MP6. Attend to precision. Resources • Math Expressions, 2018: Unit 7		
A.c.c.		
Assessment Summative Assessment		
Formative Assessment	End of Unit Assessment	
Fluency Check Puzzled Penguin	Quick Quiz	
Homework	Unit Project	
Check for understanding	Performance Assessment	
Exit ticket		
Strategy Check		

Numbers and Operations in Base Ten A. Understand the place value systems

5.NBT.A.1 Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.

5.NBT.2 Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.

5.NBT.A.3 Read, write, and compare decimals to thousandths.

Personal Math Trainer

- a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$.
- b. Compare two decimals to thousandths based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.

5.NBT.A.4 Use place value understanding to round decimals to any place.

Understandings	Essential Questions	
 Students will understand each place in the place-value system has a limit to the var which can be placed there. the same relationship exists between any two adjacent place-value system. placement of a number into a place in the place-value sy a significant effect on its value. 	 value system affect the value of the number? How is place value used to round numbers? 	
Knowledge	Skills	
 Students will know when the value in a place exceeds the limit, it must chan in a multi-digit number, a digit in one place represents 1 much as it represents in the place to its right and 1/10 of represents in the place to its left. place-value understanding is needed to round decimals t place. the place to examine in order to round numbers, includin decimals. 	0 times as using base-ten numerals, number names, and expanded form. • compare two decimals to thousandths. • o any • use >, =, and < symbols to record the results of comparisons.	
MP1. Make sense of problems and persevere in solving them.MP2. Reason abstractly and quantitatively.MP3. Construct viable arguments and critique the reasoning of others.MP6. Attend to precision.		
Resources		
Math Expressions, 2018: Unit 2, Unit 4, Unit 5		
	ssment	
Formative Assessment Fluency Check Puzzled Penguin Homework Check for understanding Exit ticket Strategy Check	End of Unit Assessment Quick Quiz Unit Project	

Numbers and Operations in Base 10 B. Perform operations with multi-digit whole numbers and with decimals to hundreds.

5.NBT.B.5 With accuracy and efficiency, multiply multi-digit whole numbers using the standard algorithm.

5.NBT.B.6 Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

5.NBT.B.7 Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Students will understandrectangles have an area that represents the product of	• How are products and quotients related?
the two dimensions. Knowledge	Skills
 Students will know multi-digit computation is just an extension of single- digit computations. 	 Students will be able to fluently multiply multi-digit whole numbers using the standard algorithm. find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors. illustrate and explain calculations by using equations, rectangular arrays, and/or area models. add, subtract, multiply, and divide decimals to hundredths.

Standards for Mathematical Practice

MP2. Reason abstractly and quantitatively.

MP3. Construct viable arguments and critique the reasoning of others.

MP6. Attend to precision.

MP8. Look for and express regularity in repeated reasoning.

Resources

• Math Expressions, 2018: Unit 2, Unit 4, Unit 5, Unit 6

Assessment		
Formative Assessment Fluency Check Puzzled Penguin Homework Check for understanding Exit ticket Strategy Check Personal Math Trainer	Summative Assessment End of Unit Assessment Quick Quiz Unit Project Performance Assessment	

Number and Operations – Fractions A. Use equivalent fractions as a strategy to add and subtract fractions.

5.NF.A.1 Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, 2/3 + 5/4 = 8/12 + 15/12 = 23/12. (In general, a/b + c/d = (ad + bc)/bd.)

5.NF.A.2 Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers. *For example, recognize an incorrect result* 2/5 + 1/2 = 3/7, *by observing that* 3/7 < 1/2.

Understandings	Essential Questions	
 Students will understand fractions must have common denominators in order to be added or subtracted. 	• When would one use addition or subtraction of fractions?	
Knowledge	Skills	
 Students will know that a common denominator is a common multiple of the two denominators (usually the least common one). that when adding fractions, the common denominators do not get added together, only the numerators do. 	 Students will be able to add and subtract fractions with unlike denominators (including mixed numbers). solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators. use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers. 	
Standards for Mathematical Practice		
MP1. Make sense of problems and persevere in solving them.MP2. Reason abstractly and quantitatively.MP3. Construct viable arguments and critique the reasoning of others.MP4. Model with mathematics.MP6. Attend to precision.		
Resources		
• Math Expressions, 2018: Unit 1, Unit 3, Unit 6		
Assessment		

Assessment		
Formative Assessment Fluency Check Puzzled Penguin Homework Check for understanding Exit ticket Strategy Check Personal Math Trainer	Summative Assessment End of Unit Assessment Quick Quiz Unit Project Performance Assessment	

Numbers and Operations – Fractions

B. Apply and extend previous understandings of multiplication and division to multiply and divide fractions.

5.NF.B.3 Interpret a fraction as division of the numerator by the denominator (i.e. $a/b = a \div b$). Solve word problems involving division of whole numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret 3/4 as the result of dividing 3 by 4, noting that 3/4 multiplied by 4 equals 3, and that when 3 wholes are shared equally among 4 people each person has a share of size 3/4. If 9 people want to share a 50-pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie?

5.NF.B.4 Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction.

- a. Interpret the product $(a/b) \times q$ as a parts of a partition of q into b equal parts; equivalently, as the result of a sequence of operations $a \times q \div b$. For example, use a visual fraction model to show $(2/3) \times 4 = 8/3$, and create a story context for this equation. Do the same with $(2/3) \times (4/5) = 8/15$. (In general, $(a/b) \times (c/d) = ac/bd$.)
- b. Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.

5.NF.B.5 Interpret multiplication as scaling (resizing), by:

- a. Comparing the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication.
- b. Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case); explaining why multiplying a given number by a fraction less than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence $a/b = (n \times a)/(n \times b)$ to the effect of multiplying a/b by 1.

5.NF.B.6 Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem.

5.NF.B.7 Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions.¹

- a. Interpret division of a unit fraction by a non-zero whole number, and compute such quotients. For example, create a story context for $(1/3) \div 4$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $(1/3) \div 4 = 1/12$ because $(1/12) \times 4 = 1/3$.
- b. Interpret division of a whole number by a unit fraction, and compute such quotients. For example, create a story context for $4 \div (1/5)$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $4 \div (1/5) = 20$ because $20 \times (1/5) = 4$.
- c. Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem. For example, how much chocolate will each person get if 3 people share 1/2 lb of chocolate equally? How many 1/3-cup servings are in 2 cups of raisins?

¹ Students able to multiply fractions in general can develop strategies to divide fractions in general, by reasoning about the relationship between multiplication and division. But division of a fraction by a fraction is not a requirement at this grade.

Understandings	Essential Questions
 Students will understand a fraction is division of the numerator by the denominator (a/b = a ÷ b). when multiplying by a fraction less than one, the product will be smaller than the first factor. when multiplying by a fraction greater than one, the product will be larger than the first factor. 	 What does it mean to divide by a fraction? Why would one need to divide by a fraction?

Knowledge	Skills
 Students will know the relative size of the answer based on the sizes of the factors. 	 Students will be able to solve word problems involving division of whole numbers. multiply a fraction or whole number by a fraction. find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths. show that the area from tiles is the same as would be found by multiplying the side lengths. multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas. solve real world problems involving multiplication of fractions and mixed numbers. divide unit fractions by whole numbers and whole numbers by unit fractions. interpret division of a unit fraction by a non-zero whole number. interpret division of a whole number by a unit fractions by non-zero whole numbers and division of unit fractions by unit fractions.
Standards	for Mathematical Practice

MP1. Make sense of problems and persevere in solving them.

MP2. Reason abstractly and quantitatively.

MP3. Construct viable arguments and critique the reasoning of others.

MP4. Model with mathematics.

MP6. Attend to precision.

Resources

• Math Expressions, 2018: Unit 3, Unit 6

Assessment		
Formative Assessment Fluency Check Puzzled Penguin Homework Check for understanding Exit ticket Strategy Check Personal Math Trainer	Summative Assessment End of Unit Assessment Quick Quiz Unit Project Performance Assessment	

Measurement A. Convert like measurement units within a given measurement system.

5.M.A.1 Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.

Understandings	Essential Questions	
 Students will understand measurement units vary in the customary system differently than in the metric system. 	• Why would one need to convert measurements from one unit to another?	
• understanding place value helps one to understand the metric system.	• How does one know whether the new answer should be a bigger or smaller number of units?	
Knowledge	Skills	
 Students will know every step in the metric system involves a power of 10, e.g. 10 cm = 1 decimeter, 10 mm = 1 cm, etc.) customary equivalents. 	 Students will be able to convert among different-sized standard measurement units within a given measurement system. solve real-world problems involving conversions. 	
Standards for N	Iathematical Practice	
MP3. Construct viable arguments and critique the re-	easoning of others.	
MP5. Use appropriate tools strategically.	-	
MP6. Attend to precision.		
MP7. Look for and make use of structure.		
R	esources	
Math Expressions, 2018: Unit 8		
Assessment Assessment Summative Assessment		
Formative Assessment	End of Unit Assessment	
Fluency Check Puzzled Penguin	Quick Quiz	
Homework	Unit Project	
Check for understanding	Performance Assessment	
Exit ticket		
Strategy Check		
Personal Math Trainer		

Measurement & Data

B. Geometric measurement: Understand concepts of volume and relate volume to multiplication and to addition

5.M.B.2 Recognize volume as an attribute of solid figures and understand concepts of volume measurement.

- a. A cube with side length 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to measure volume.
- b. A solid figure which can be packed without gaps or overlaps using n unit cubes is said to have a volume of n cubic units.

5.M.B.3 Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and non-standard units.

5.M.B.4 Relate volume to the operations of multiplication and addition and solve real world and mathematical problems involving volume.

- a. Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplying the height by the area of the base. Represent threefold whole-number products as volumes, e.g., to represent the associative property of multiplication.
- b. Apply the formulas $V = l \times w \times h$ and $V = B \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real world and mathematical problems.
- c. Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real world problems.

Understandings		Essential Question
Students will understand		
• volume is an attribute of solid figures.		• For what types of items can we
• the concept of volume measurement involves filling up space.		measure volume?
• volume is related to the operations of multiplication and addition.		
• volume is additive.	-	
Knowledge		Skills
Students will know	Students will be able to	
• a cube with side length 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to	ft, and improvised units.	nting unit cubes, using cubic cm, cubic in, cubic
measure volume.		
• a solid figure which can be packed	• apply the formulas $V = l \times w \times h$ and $V = b \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge	
without gaps or overlaps using <i>n</i> unit		solving real world and mathematical problems.
cubes is said to have a volume of <i>n</i>	 find volumes of solid figures composed of two non-overlapping right 	
cubic units.		ding the volumes of the non-overlapping parts.
Standards for Mathematical Practice		
MP3. Construct viable arguments and critiqu	e the reasoning of others.	
MP5. Use appropriate tools strategically.		
MP6. Attend to precision.	MP6. Attend to precision.	
MP7. Look for and make use of structure.		
Resources		
• Math Expressions, 2018: Unit 8		
	Assessment	
	Sum	mative Assessment
Formative Assessment		End of Unit Assessment
Fluency Check		Quick Quiz
Puzzled Penguin Homework		Unit Project
Check for understanding		Performance Assessment
Exit ticket		
Strategy Check		
Personal Math Trainer		
Data Literacy A. Understand and analyze data visualizations¹

- **5.DL.A.1** Understand how different visualizations can highlight different aspects of data. Ask questions and interpret data visualizations to describe and analyze patterns
- **5.DL.A.2** Develop strategies to collect, organize and represent data of various types and from various sources. Communicate results digitally through a data visual (e.g. chart, storyboard, video presentations)
- **5.DL.A.3** Collect and clean data to be analyzable (e.g., make sure each entry is formatted correctly, deal with missing or incomplete data.)
- **5.DL.A.4** Using appropriate visualizations (i.e. double line plot, double bar graph), analyze data across samples.

¹ Analysis of data and visualizations at this grade excludes ratio, rate, proportion and percentages. These concepts are introduced in Grade 6

Understandings	Essential Questions
Students will understand	
How to communicate data	• Why collect data?
How to analyze data appropriately	• How should data be represented?
Knowledge	Skills
Students will know	Students will be able to
How to ask questions	Collect Data
How to interpret data	Organize data into a readable form
	• Create appropriate representations of the data
Standards for Mathematical Practice	

MP2. Reason abstractly and quantitatively.

MP3. Construct viable arguments and critique the reasoning of others.

- MP4. Model with mathematics
- MP5. Use appropriate tools strategically

Resources

• Math Expressions, 2018: Unit 8

Assessment		
Formative Assessment Fluency Check Puzzled Penguin Homework Check for understanding Exit ticket Strategy Check Personal Math Trainer	Summative Assessment End of Unit Assessment Quick Quiz Unit Project Performance Assessment	

Data Literacy B. Represent and interpret data.

5.DL.B.2 Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Use operations on fractions for this grade to solve problems involving information presented in line plots. *For example, given different measurements of liquid in identical beakers, find the amount of liquid each beaker would contain if the total amount in all the beakers were redistributed equally.*

Understandings			
	Essential Questions		
 Students will understand data entries do not have to be only whole numbers. the scale on a line plot must be evenly spaced. 	• What types of data can be graphed on a line plot with a fractional scale?		
Knowledge	Skills		
 Students will know there will still be a whole number of pieces of data even though there is a fractional scale. 	 Students will be able to make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). use operations on fractions for this grade to solve problems involving information presented in line plots. 		
Standards for N	Aathematical Practice		
MP3. Construct viable arguments and critique the MP5. Use appropriate tools strategically.MP6. Attend to precision.MP7. Look for and make use of structure.	6		
Resources			
• Math Expressions, 2018: Unit 8			
	ssessment Summative Assessment		

Geometry

A. Graph points on the coordinate plane to solve real-world and mathematical problems.

5.G.A.1 Use a pair of perpendicular number lines, called axes, to define a coordinate system, with the intersection of the lines (the origin) arranged to coincide with the 0 on each line and a given point in the plane located by using an ordered pair of numbers, called its coordinates. Understand that the first number indicates how far to travel from the origin in the direction of one axis, and the second number indicates how far to travel in the direction of the second axis, with the convention that the names of the two axes and the coordinates correspond (e.g., *x*-axis and *x*-coordinate, *y*-axis and *y*-coordinate).

5.G.A.2 Represent real world and mathematical problems by graphing points in the first quadrant of the coordinate plane, and interpret coordinate values of points in the context of the situation.

Understandings	Essential Questions	
 Students will understand the first number in an ordered pair indicates how far travel from the origin in the direction of one axis, ar the second number indicates how far to travel in the direction of the second axis. 	nd plane?	
Knowledge	Skills	
Students will know	Students will be able to	
 a pair of perpendicular number lines, called axes, define a coordinate system, with the intersection of lines (the origin) arranged to coincide with the 0 on each line. a given point in the plane is located by using an ordered pair of numbers, called its coordinates. the names of the two axes and the coordinates correspond (e.g., <i>x</i>-axis and <i>x</i>-coordinate, <i>y</i>-axis and coordinate). 	problems by graphing points in the first quadrant of the coordinate plane.	
Standards for Mathematical Practice		
MP2. Reason abstractly and quantitatively.		
MP3. Construct viable arguments and critique the reason	ning of others	
MP6. Attend to precision.		
Resou	urces	
• Math Expressions, 2018: Unit 7		
Assessment		
Formative Assessment	Summative Assessment	
Fluency Check	End of Unit Assessment	
Puzzled Penguin	Quick Quiz	
Homework	Unit Project	
Check for understanding	Performance Assessment	
Exit ticket		
Strategy Check		
Personal Math Trainer		

Geometry

B. Classify two dimensional figures into categories based on their properties.

5.G.B.3 Understand that attributes belonging to a category of two-dimensional figures also belong to all subcategories of that category. For example, all rectangles have four right angles and squares are rectangles, so all squares have four right angles.

5.G.B.4 Classify two-dimensional figures in a hierarchy based on properties.

Understandings	Essential Questions	
 Students will understand attributes belonging to a category of two- dimensional figures also belong to all subcategories of that category. 	 How does one classify two-dimensional figures? Why would one need to classify a two-dimensional figure? 	
Knowledge	Skills	
Students will knowthe characteristics of figures.	 Students will be able to classify two-dimensional figures in a hierarchy based on properties. 	
Standards for	Mathematical Practice	
MP3. Construct viable arguments and critique the MP5. Use appropriate tools strategically. MP6. Attend to precision. MP7. Look for and make use of structure.		
	Resources	
• Math Expressions, 2018: Unit 8		
	Assessment	
Formative AssessmentSFluency CheckPuzzled PenguinHomeworkCheck for understandingExit ticketStrategy CheckPersonal Math Trainer	Summative Assessment End of Unit Assessment Quick Quiz Unit Project Performance Assessment	

Career Readiness, Life Literacies, and Key Skills

Career Readiness, Life Literacies, and Key Skills

Rapid advancements in technology and subsequent changes in the economy have created opportunities for individuals to compete and connect on a global scale. In this increasingly diverse and complex world, the successful entrepreneur or employee must not only possess the requisite education for specific industry pathways but also employability skills necessary to collaborate with others and manage resources effectively in order to establish and maintain stability and independence. This document outlines concepts and skills necessary for New Jersey's students to thrive in an ever-changing world. Intended for integration throughout all K–12 academic and technical content areas, the New Jersey Student Learning Standards- Career Readiness, Life Literacies, and Key Skills (NJSLS-CLKS) provides the framework for students to learn the concepts, skills, and practices essential to the successful navigation of career exploration and preparation, personal finances and digital literacy.

Mission

Career readiness, life literacies, and key skills education provides students with the necessary skills to make informed career and financial decisions, engage as responsible community members in a digital society, and to successfully meet the challenges and opportunities in an interconnected global economy.

Vision

An education in career readiness, life literacies, and key skills fosters a population that:

•Continually self-reflects and seeks to improve the essential life and career practices that lead to success;

•Uses effective communication and collaboration skills and resources to interact with a global society;

•Possesses financial literacy and responsibility at home and in the broader community;

•Plans, executes, and alters career goals in response to changing societal and economic conditions; and •Seeks to attain skill and content mastery to achieve success in a chosen career path.

Career Readiness, Life Literacies, and Key Skills Standards

- 9.4.5.CI.3: Participate in a brainstorming session with individuals with diverse perspectives to expand one's thinking about a topic of curiosity.
- 9.4.5.CT.1: Identify and gather relevant data that will aid in the problem-solving process.
- 9.4.5.CT.3: Describe how digital tools and technology may be used to solve problems.
- 9.4.5.CT.4: Apply critical thinking and problem-solving strategies to different types of problems such as personal, academic, community and global.
- 9.4.5.IML.3: Represent the same data in multiple visual formats in order to tell a story about the data.

Computer Science and Design Thinking

Computer Science and Design Thinking

New approaches necessary for solving the critical challenges that we face as a society will require harnessing the power of technology and computing. Rapidly changing technologies and the proliferation of digital information have permeated and radically transformed learning, working, and everyday life. To be well-educated, global-minded individuals in a computing-intensive world, students must have a clear understanding of the concepts and practices of computer science. As education systems adapt to a vision of students who are not just computer users but also computationally literate creators who are proficient in the concepts and practices of computer science and design thinking, engaging students in computational thinking and human-centered approaches to design through the study of computer science and technology serves to prepare students to ethically produce and critically consume technology.

Mission

Computer science and design thinking education prepares students to succeed in today's knowledge-based economy by providing equitable and expanded access to high-quality, standards-based computer science and technological design education.

Vision

All students have equitable access to a rigorous computer science and design thinking education. Students will benefit from opportunities to engage in high-quality technology programs that foster their ability to:

• develop and apply computational and design thinking to address real-world problems and design creative solutions;

• engage as collaborators, innovators, and entrepreneurs on a clear pathway to success through postsecondary education and careers;

• navigate the dynamic digital landscape to become healthy, productive, 21st century global-minded individuals; and

• participate in an inclusive and diverse computing culture that appreciates and incorporates perspectives from people of different genders, ethnicities, and abilities.

Computer Science and Design Thinking Standards

- **8.1.5.IC.1:** Identify computing technologies that have impacted how individuals live and work and describe the factors that influenced the changes.
- **8.1.5.IC.2:** Identify possible ways to improve the accessibility and usability of computing technologies to address the diverse needs and wants of users.
- **8.1.5.DA.1:** Collect, organize, and display data in order to highlight relationships or support a claim.
- **8.1.5.DA.3:** Organize and present collected data visually to communicate insights gained from different views of the data.
- **8.1.5.AP.1:** Compare and refine multiple algorithms for the same task and determine which is the most appropriate.
- 8.1.5.AP.4: Break down problems into smaller, manageable sub-problems to facilitate program development.
- **8.1.5.AP.5:** Modify, remix, or incorporate pieces of existing programs into one's own work to add additional features or create a new program.
- **8.2.5.ED.2:** Collaborate with peers to collect information, brainstorm to solve a problem, and evaluate all possible solutions to provide the best results with supporting sketches or models.
- **8.2.5.ITH.4:** Describe a technology/tool that has made the way people live easier or has led to a new business or career.

Sixth Grade

Interdisciplinary Connections

Mathematics is a unified body of knowledge whose concepts build upon each other. Connecting mathematical concepts includes linking ideas to related ideas learned previously.

Major emphasis should be given to ideas and concepts across mathematical content areas that help students see that mathematics is a web of closely connected ideas. Students need to connect their mathematical learning to appropriate real-world contexts. They need to create interest and maintain the interest after the novelty of the work has worn off.

Mathematics is the language of science and is greatly utilized in industry and business. It gives us the power to solve difficult real-world problems, but also helps us to understand how the universe operates.

Every mathematics teacher needs to make students unafraid of the subject by convincing the students of the usefulness of learning mathematics in their daily lives and for higher studies. The world today, which leans more and more heavily on Science and Technology, demands more from mathematics. Tomorrow's world will, no doubt, make still greater demands from mathematics.

Interdisciplinary Connections for Grade 6

Big Ideas, 2022:7.1-7.7, 8.6

Language Arts/Science - (MS ETS 1-1), (NJSLSA.W2)

- Design an Aquarium Unit Project Science (MS LS 1-1)
 - Microscope lens Covering and Surrounding Resource Ace Question 93

Climate Change for Grade 6

With the adoption of the 2020 New Jersey Student Learning Standards (NJSLS), New Jersey became the first state in the nation to include climate change across content areas. The goal of inclusion of climate change education implementation is to foster generations of New Jersey students that can analyze, question, interpret, to think independently, and bring critical deduction to fulfill, and to lead in jobs created by burgeoning industries of the future green economy.

- **6.EE.C.9** Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables and relate these to the equation.
 - Students will take food production data and create equations based on the data. They will then take their equations and graph them. Students will then answer questions based on their equation and graphs.

New Jersey Student Learning Standards (NJSLS)

In Grade 6, instructional time should focus on four critical areas: (1) connecting ratio and rate to whole number multiplication and division and using concepts of ratio and rate to solve problems; (2) completing understanding of division of fractions and extending the notion of number to the system of rational numbers, which includes negative numbers; (3) writing, interpreting, and using expressions and equations; and (4) developing understanding of statistical thinking.

(1) Students use reasoning about multiplication and division to solve ratio and rate problems about quantities. By viewing equivalent ratios and rates as deriving from, and extending, pairs of rows (or columns) in the multiplication table, and by analyzing simple drawings that indicate the relative size of quantities, students connect their understanding of multiplication and division with ratios and rates. Thus students expand the scope of problems for which they can use multiplication and division to solve problems, and they connect ratios and fractions. Students solve a wide variety of problems involving ratios and rates.

(2) Students use the meaning of fractions, the meanings of multiplication and division, and the relationship between multiplication and division to understand and explain why the procedures for dividing fractions make sense. Students use these operations to solve problems. Students extend their previous understandings of number and the ordering of numbers to the full system of rational numbers, which includes negative rational numbers, and in particular negative integers. They reason about the order and absolute value of rational numbers and about the location of points in all four quadrants of the coordinate plane.

(3) Students understand the use of variables in mathematical expressions. They write expressions and equations that correspond to given situations, evaluate expressions, and use expressions and formulas to solve problems. Students understand that expressions in different forms can be equivalent, and they use the properties of operations to rewrite expressions in equivalent forms. Students know that the solutions of an equation are the values of the variables that make the equation true. Students use properties of operations and the idea of maintaining the equality of both sides of an equation to solve simple one-step equations. Students construct and analyze tables, such as tables of quantities that are in equivalent ratios, and they use equations (such as 3x = y) to describe relationships between quantities.

(4) Building on and reinforcing their understanding of number, students begin to develop their ability to think statistically. Students recognize that a data distribution may not have a definite center and that different ways to measure center yield different values. The median measures center in the sense that it is roughly the middle value. The mean measures center in the sense that it is the value that each data point would take on if the total of the data values were redistributed equally, and also in the sense that it is a balance point. Students recognize that a measure of variability (interquartile range or mean absolute deviation) can also be useful for summarizing data because two very different sets of data can have the same mean and median yet be distinguished by their variability. Students learn to describe and summarize numerical data sets, identifying clusters, peaks, gaps, and symmetry, considering the context in which the data were collected.

Students in Grade 6 also build on their work with area in elementary school by reasoning about relationships among shapes to determine area, surface area, and volume. They find areas of right triangles, other triangles, and special quadrilaterals by decomposing these shapes, rearranging or removing pieces, and relating the shapes to rectangles. Using these methods, students discuss, develop, and justify formulas for areas of triangles and parallelograms. Students find areas of polygons and surface areas of prisms and pyramids by decomposing them into pieces whose area they can determine. They reason about right rectangular prisms with fractional side lengths to extend formulas for the volume of a right rectangular prism to fractional side lengths. They prepare for work on scale drawings and constructions in Grade 7 by drawing polygons in the coordinate plane.

Ratios and Proportional Relationships

A. Understand ratio concepts and use ratio reasoning to solve problems.

6.RP.A.1 Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. *For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes."*

6.RP.A.2 Understand the concept of a unit rate a/b associated with a ratio a:b with $b \neq 0$, and use rate language in the context of a ratio relationship. For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is 3/4 cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger."¹

6.RP.A.3 Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.

- a. Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.
- b. Solve unit rate problems including those involving unit pricing and constant speed. *For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed?*
- c. Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means 30/100 times the quantity); solve problems involving finding the whole, given a part and the percent.
- d. Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing quantities.

¹ Expectations for unit rates in this grade are limited to non-complex fractions.

Understandings	Essential Questions
 Students will understand that Ratios compare two values. unit rates are <i>a/b</i> given that the ratio is <i>a:b</i>, such that <i>b ≠ 0</i>. 	 Why does one need to compare numbers? When does one need to use ratios to compare numbers? How can one compare and contrast numbers?
Knowledge	Skills
 Students will know ratio language (the ratio of <i>a:b</i> means that there is <i>a</i> of something for every <i>b</i> of a corresponding item). <i>a/b</i> is the same as <i>a:b</i> or <i>a to b</i>. how to relate a percent of a quantity to a rate per 100. 	 Students will be able to use ratio language to describe a ratio relationship between two quantities. use rate language in the context of a ratio relationship. use ratio and rate reasoning to solve real-world and mathematical problems. make a table of equivalent ratios relating quantities with whole-number measurements. solve unit rate problems including those involving unit pricing and constant rate. find a percent of a quantity as a rate per 100 and solve problems involving finding the whole, given a part or the percent. use ratio reasoning to convert measurement units. manipulate and transform units appropriately when multiplying or dividing quantities.

Standards for Mathematical Practice MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP3. Construct viable arguments and critique the reasoning of others. MP4. Model with mathematics. MP7. Look for and make use of structure. MP8. Look for and express regularity in repeated reasoning. Resources Big Ideas, 2022:1.5, 3.1-3.6, 4.1, 4.2, 4.4, 7.1, 7.7 • Assessment Formative Summative Binder Quiz Check-up Exit Slips Partner Quiz Do Now Unit Assessments Homework Unit Projects

The Number System

A. Apply and extend previous understandings of multiplication and division to divide fractions by fractions.

6.NS.A.1 Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. For example, create a story context for $(2/3) \div (3/4)$ and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that $(2/3) \div (3/4) = 8/9$ because 3/4 of 8/9 is 2/3. (In general, $(a/b) \div (c/d) = ad/bc$.) How much chocolate will each person get if 3 people share 1/2 lb of chocolate equally? How many 3/4-cup servings are in 2/3 of a cup of yogurt? How wide is a rectangular strip of land with length 3/4 mi and area 1/2 square mi?

Understandings	Essential Questions	
Understandings		
Students will understand that		
• the size of a factor impacts the size of the	• What is represented by division of a fraction by a fraction?	
answer with respect to the other factor.		
• division by a rational number may result in a	• What type of visual models can be used to represent division of fractions?	
quotient whose value is bigger than, equal to, or smaller than the value of the dividend.	 How are division and multiplication of a fraction by a 	
or smaller than the value of the dividend.	fraction related?	
Knowledge	Skills	
Students will know	Students will be able to	
• multiplication with fractions represents part	• compute quotients of fractions.	
of a part.	• interpret quotients of fractions.	
• division of a fraction by a proper fraction	• create a story context for division.	
creates a larger answer.	• solve word problems involving division of fractions.	
• multiplication of a fraction by a proper		
fraction creates a smaller answer.		
Standards for 1	Mathematical Practice	
MP1. Make sense of problems and persevere in solving	them.	
MP2. Reason abstractly and quantitatively.		
MP4. Model with mathematics		
MP7. Look for and make use of structure.		
MP8. Look for and express regularity in repeated reaso		
I	Resources	
Big Ideas, 2022: 2.1, 2.2, 2.3		
	ssessment	
Formative	Summative	
Binder Quiz	Check-up	
Exit Slips	Partner Quiz	
Do Now	Unit Assessments	
Homework	Unit Projects	

The Number System

B. Compute fluently with multi-digit numbers and find common factors and multiples.

6.NS.B.2 With accuracy and efficiency, divide multi-digit numbers using the standard algorithm.

6.NS.B.3 With accuracy and efficiency, add, subtract, multiply and divide multi-digit decimals using the standard algorithm for each operation.

6.NS. B.4 Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1-100 with a common factor as a multiple of a sum of two whole numbers with no common factor. *For example, express* 36 + 8 as 4 (9 + 2).

Understandings	Essential Questions	
 Students will understand that the proper operations and procedures must be determined in order to solve problems. factors of a (whole) number are always less than or to the number itself. multiples of a (whole) number are always greater th equal to the number itself. Knowledge Students will know the standard algorithm for division of multidigit numbers the standard algorithms for addition, subtraction, multiplication, and division of multi-digit decimals the definition of a factor. the process of finding a factor. 	 Why would one need to find common factors and multiples? In what situation would one want to use the distributive property add two whole numbers? What type(s) of problems require using multi-digit decimal operations? Students will be able to fluently divide using the standard algorithm. fluently add multi-digit decimals using the standard algorithm. fluently subtract multi-digit decimals using the standard algorithm. fluently multiply multi-digit decimals using the standard algorithm. fluently divide multi-digit decimals using the standard algorithm. 	
 the definition of a multiple. the process of finding a multiple. how to find the prime factorization of a number. how to factor out a number from the sum of two whole numbers 	 find the least common multiple of two whole numbers less than or equa to 12. use the distributive property to express a sum of two whole numbers 1-100 with a common factor as a multiple of the sum of two whole number with no common factor. <i>For example, express 36 + 8 as 4(9 + 2).</i> 	
Standard	Is for Mathematical Practice	
MP1. Make sense of problems and persevere in solvingMP2. Reason abstractly and quantitatively.MP4. Model with mathematicsMP5. Use appropriate tools strategically.MP7. Look for and make use of structure.MP8. Look for and express regularity in repeated reason		
	Resources	
• Big Ideas, 2022: 1.3, 1.4, 1.5, 2.4-2.7, 5.5		
Assessment		
Formative	Summative	
Binder Quiz	Check-up	
Exit Slips	Partner Quiz	
Do Now	Unit Assessments	
Homework	Unit Projects	

The Number System

C. Apply and extend previous understandings of numbers to the system of rational numbers.

6.NS. C.5 Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.

6.NS. C.6 Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.

- a. Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., -(-3) = 3, and that 0 is its own opposite.
- b. Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.
- c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.

6.NS. C.7 Understand ordering and absolute value of rational numbers.

- a. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. For example, interpret -3 > -7 as a statement that -3 is located to the right of -7 on a number line oriented from left to right.
- b. Write, interpret, and explain statements of order for rational numbers in real-world contexts. For example, write $-3 \circ C > -7 \circ C$ to express the fact that $-3 \circ C$ is warmer than $-7 \circ C$.
- c. Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. For example, for an account balance of -30 dollars, write |-30| = 30 to describe the size of the debt in dollars.
- d. Distinguish comparisons of absolute value from statements about order. *For example, recognize that an account balance less than –30 dollars represents a debt greater than 30 dollars.*

6.NS. C.8 Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.

Understandings	Essential Questions
 Students will understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge). a rational number is a point on the number line. rational numbers on the number line are oriented from left to right rational numbers have an order that exists related to their location on a number line. the absolute value of a rational number is its distance from 0 on the number line. the distance from a point on the coordinate system to the origin (0,0) is related to the absolute value of its x- and y- coordinates . 	 What are some rational numbers around us? What are some non-rational numbers around us? How can ordering of rational numbers help to make sense of the world around us? When is the absolute value of a rational number used in real life?

Knowledge	Skills		
 Knowledge Students will know opposite signs of numbers indicate locations on opposite sides of 0 on the number line. the opposite of the opposite of a number is the number itself, e.g., -(-3) = 3, and that 0 is its own opposite. signs of numbers in ordered pairs indicate locations in quadrants of the coordinate plane. that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes. how to find the absolute value of a rational number. 	 Students will be able to use positive and negative numbers to represent quantities in real-world contexts. explain the meaning of 0 in situations using positive and negative numbers. extend number-line diagrams and coordinate axes to represent points on the line and in the plane with negative number coordinates. find and position integers and other rational numbers on a horizontal or vertical number line diagram. find and position pairs of integers and other rational numbers on a coordinate plane. interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. <i>For example, interpret -3 > -7 as a statement that -3 is located to the right of -7 on a number line oriented from left to right.</i> write, interpret, and explain statements of order for rational numbers in real- 		
MP2. Reason abstractly and quantitative	find distances between points with the same first coordinate or the same second coordinate, using coordinates and absolute value. Standards for Mathematical Practice Make sense of problems and persevere in solving them. Reason abstractly and quantitatively.		
MP4. Model with mathematics. MP5. Use appropriate tools strategically			
The second appropriate tools strategically	Resources		
• Big Ideas, 2022: 4.1-4.3, 8.1-8.8			
	Assessment		
Formative Binder Quiz Exit Slips Do Now Homework	Summative Check-up Partner Quiz Unit Assessments Unit Projects		

Expressions and Equations

A. Apply and extend previous understandings of arithmetic to algebraic expressions.

6.EE. A.1 Write and evaluate numerical expressions involving whole-number exponents.

6.EE.A.2 Write, read, and evaluate expressions in which letters stand for numbers.

- a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation "Subtract y from 5" as 5 y.
- b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression 2 (8 + 7) as a product of two factors; view (8 + 7) as both a single entity and a sum of two terms.
- c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in realworld problems. Perform arithmetic operations, including those involving whole-number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas $V = s^3$ and $A = 6 s^2$ to find the volume and surface area of a cube with sides of length s = 1/2.

6.EE.A.3 Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression 3(2 + x) to produce the equivalent expression 6 + 3x; apply the distributive property to the expression 24x + 18y to produce the equivalent expression 6(4x + 3y); apply properties of operations to y + y + y to produce the equivalent expression 3y.

6.EE.A.4 Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions y + y + y and 3y are equivalent because they name the same number regardless of which number y stands for.

Understandin	ngs	Essential Questions
 Students will understand that algebraic expressions have letters tha arithmetic expressions have only num numbers can be substituted in place or expressions algebraic expressions can be equivale area, perimeter, or volume formulas area that verbal sentences or expressions can be expressions 	nbers and no letters. of letters in algebraic ent to each other are algebraic expressions	 How are mathematical expressions in which letters stand for numbers useful in real life? What is the purpose of identifying equivalent expressions? What is the difference between an algebraic expression and an arithmetic expression?
Knowledge		Skills
 Students will know the definition of sum, term, product, factor, quotient, coefficient. how to identify two algebraic expressions that are equivalent . to apply the conventional order of operations when no parentheses are given. how to apply the distributive property. 	 evaluate numerical expressions in white expressions in white read expressions in white evaluate expressions in white evaluate expressions that remumbers. identify parts of an expression at search evaluate expressions at search form formulas used including those involving there are no parentheses apply the properties of o two expressions are equipated at the evaluation of the eva	 ons involving whole-number exponents. essions involving whole-number exponents. ch letters stand for numbers. ch letters stand for numbers. which letters stand for numbers. cord operations with numbers and with letters standing for ession using mathematical terms (sum, term, product, factor, ew one or more parts of an expression as a single entity. pecific values of their variables. Include expressions that d in real world problems. Perform arithmetic operations, g whole-number exponents, in the conventional order when to specify a particular order (Order of Operations). perations to generate equivalent expressions. Identify when ivalent (i.e., when the two expressions name the same tich value is substituted into them).

Standards for Mathematical Practice		
MP1. Make sense of problems and persevere in solving them.		
MP2. Reason abstractly and quantitatively.		
MP5. Use appropriate tools strategically.		
MP6. Attend to precision.		
MP8. Look for and express regularity in repeated reasoning.		
Resources		
• Big Ideas, 2022: 1.1-1.5, 5.1-5.5, 6.1-6.4, 7.1-7.7, 8.7, 8.8		
Assess	ment	
Formative	Summative	
Binder Quiz	Check-up	
Exit Slips	Partner Quiz	
Do Now	Unit Assessments	
Homework	Unit Projects	

Expressions and Equations

B. Reason about and solve one-variable equations and inequalities.

6.EE. B.5 Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.

6.EE. B.6 Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.

6.EE. B.7 Solve real-world and mathematical problems by writing and solving equations of the form x + p = q and px = q for cases in which *p*, *q* and *x* are all nonnegative rational numbers.

6.EE. B.8 Write an inequality of the form x > c or x < c to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form x > c or x < c have infinitely many solutions; represent solutions of such inequalities on number line diagrams.

Understandings		Essential Questions		
5		20000000		
 Students will understand that solving an equation or inequality will find the value(s) that will make the statement true. a variable can represent an unknown number. a variable can represent any number in a specified set. 		 What is the difference between an equation and an inequality? What does it mean when a number does not satisfy an equation or inequality? 		
Knowledge		Skills		
 Students will know that a random number may not make an equation or inequality true. that a variable in an equation or inequality represents an unknown number. inequalities of the form x > c or x < c have infinitely many solutions. that solutions of inequalities of form x>c or x < c an be represented as intervals on the number line. that while inequalities may have infinitely many solutions, equations have a finite number of solutions. 	 Students will be able to use substitution to determine whether a given number in a specified set will make an equation or inequality true. use variables to represent numbers solve real-world and mathematical problems by writing and solving equations of the form x + p = q for cases in which p, q and x are all nonnegative rational numbers. solve real-world and mathematical problems by writing and solving equations of the form px = q for cases in which p, q and x are all nonnegative rational numbers. write inequality of the form x > c or x < c to represent a constraint or condition in a real-world or mathematical problem. recognize that inequalities of the form x > c or x < c have infinitely many solutions represent solutions of inequalities on number line diagrams 			
Standar	ds for Mathe	ematical Practice		
MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP4. Model with mathematics. MP5. Use appropriate tools strategically.				
	Resour	ces		
• Big Ideas, 2022: 6.1-6.4, 7.1-7.3, 8.7, 8.8				
Assessment				
Formative Binder Quiz Exit Slips Do Now Homework		Summative Check-up Partner Quiz Unit Assessments Unit Projects		

Expressions and Equations

6.EE. C.9 Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation d = 65t to represent the relationship between distance and time.

Understandings		Essential Questions		
 Students will understand that quantities can change in relation to one another and the relationship can be expressed as an equation relating the two. the value of one quantity determines the value of the second quantity. two quantities may or may not be related. 		 How is a relationship represented in tables? How is a relationship represented in graphs? How is a relationship represented in an equation? How can one tell that there is a relationship between two quantities? Why is it useful to write an equation to express one quantity in terms of another quantity? 		
Knowledge	Skills			
 Students will know the meaning of a dependent variable. the meaning of an independent variable. when two quantities are related to each other. 	 Students will be able to use variables to represent two quantities in a realworld problem that change in relationship to one another. write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. use the equation of a relationship between two dependent and independent and independent variables to predict ordered pairs that are not displaced in a given graph or table 			
Standar	ds for Math	nematical Practice		
MP1. Make sense of problems and persevere in solving them. MP2. Reason abstractly and quantitatively. MP4. Model with mathematics. MP5. Use appropriate tools strategically. Resources				
• Big Ideas, 2022: 6.4				
Assessment				
Formative Binder Quiz Exit Slips Do Now Homework		Summative Check-up Partner Quiz Unit Assessments Unit Projects		

Geometry

A. Solve real-world and mathematical problems involving area, surface area and volume.

6.G. A.1 Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real world and mathematical problems.

6.G. A.2. Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas V = l w h and V = b h to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.

6.G. A.3. Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.

6.G.A.4. Represent three-dimensional figures (e.g. pyramid, triangular prism, rectangular prism) using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.

Understandings	Essential Questions		
Students will understand that			
 triangles and rectangles can be used to find areas of other polyge a 2-D net of a 3-D figure can be used to find the surface area of figure surface area is related to "wrapping" or "covering" of a surface square units, i.e. squares with side length of one unit volume is related to "filling" of space with cubic units, i.e. cubes with edges of one-unit length 	 f the How are areas of polygons found? How are volume and surface area of a right rectangular prism found? Why are volumes represented in cubic units? 		
Knowledge	Skills		
 Students will know that areas of triangles, including right triangles, and rectangles be used to find areas of other polygons, when the other polygon are decomposed into triangles or composed into rectangles that the volume of a right rectangular prism is the number of un cubes it contains (of the appropriate unit fraction edge length) the total area of a net of a 3-D figure is the surface area of figure 	 find the area of other triangles. find the area of special quadrilaterals. find the areas of polygons by composing them into rectangles or decomposing them into triangles represent three-dimensional figures using nets to find the surface area of a 3-D figure by finding the total area of its 2-D net 		
Standards for Math	nematical Practice		
MP1. Make sense of problems and persevere in solving them.MP4. Model with mathematics.MP5. Use appropriate tools strategically.MP6. Attend to precision.MP7. Look for and make use of structure.			
Resou	irces		
• Big Ideas, 2022:7.1-7.7, 8.6			
Assessment			
Formative Binder Quiz Exit Slips Do Now Homework	Summative Check-up Partner Quiz Unit Assessments Unit Projects		

Statistics and Probability

6.SP. A.1. Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. *For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages.*

6.SP. A.2. Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.

6.SP. A.3. Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.

Understandings	Essential Questions		
 Students will understand that statistical questions anticipate variability a set of data has a distribution center and spread are two related but different ways of describing a set of data 	 What is a statistical question? What is a distribution? What is the difference between the center and the spread of a numerical set? How are data sets described? 		
Knowledge	Skills		
 Students will know that a set of data can be described by its center, spread, and overall shape how to find the center of a numerical data set the center summarizes a data set with a single number the spread is a measure of variation of all values in a data set about the center 	 Students will be able to recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages. understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape. recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure 		
Standar	of variation describes how its values vary with a single number. 'ds for Mathematical Practice		
MP1. Make sense of problems and persevere in sMP4. Model with mathematics.MP5. Use appropriate tools strategically.MP6. Attend to precision.MP7. Look for and make use of structure.MP8. Look for and express regularity in repeated			
	Resources		
• Big Ideas, 2022: 9.1-9.5, 10.1, 10.3-10.5			
	Assessment		
Formative Binder Quiz Exit Slips Do Now Homework	Summative Check-up Partner Quiz Unit Assessments Unit Projects		

Statistics and Probability

B. Summarize and describe distributions

6.SP. B.4. Display numerical data in plots on a number line, including dot plots, histograms, and box plots.

6.SP. B.5. Summarize numerical data sets in relation to their context, such as by:

- a. Reporting the number of observations.
- b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.
- c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.
- d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.

Understandings		Essential Questions		
Students will understand that numerical data can be displayed in multi summaries of numerical data vary based overall patterns of numerical data can va some patters in numerical data can have Knowledge Students will know	on their contexts. ary. striking deviations. Students will be able to	 How do measures of center and variability help us make sense of the world around us? In what contexts are the measures of center and variability preferred descriptions of the data? Why do we need multiple ways of describing numerical data? 		
 how to display numerical data using dot plots, histograms, and box plots. how to summarize numerical data in multiple ways. that the choice of measures of center and variability depends on the context. how to identify a striking deviation from the overall pattern. real life examples of patterns with, and without, striking deviations. 	 construct dot plots, histograms, and box plots. summarize numerical data by: o reporting the number of observations; o describing the nature of the attribute under investigation, including how it was measured and its units of measurement; giving quantitative measures of center (median and/or mean) o giving quantitative measures of variability (interquartile range and/or mean absolute deviation); describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered; relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered. 			
Sta	ndards for Mathema	atical Practice		
MP1. Make sense of problems and persevereMP4. Model with mathematics.MP5. Use appropriate tools strategically.MP6. Attend to precision.MP7. Look for and make use of structure.MP8. Look for and express regularity in repeated.	-			
	Resources			
•Big Ideas, 2022: 9.1-9.5, 10.1-10.5				
	Assessmen	t		
Formative Binder Quiz Exit Slips Do Now Homework		Summative Check-up Partner Quiz Unit Assessments Unit Projects		

Career Readiness, Life Literacies, and Key Skills

Career Readiness, Life Literacies, and Key Skills

Rapid advancements in technology and subsequent changes in the economy have created opportunities for individuals to compete and connect on a global scale. In this increasingly diverse and complex world, the successful entrepreneur or employee must not only possess the requisite education for specific industry pathways but also employability skills necessary to collaborate with others and manage resources effectively in order to establish and maintain stability and independence. This document outlines concepts and skills necessary for New Jersey's students to thrive in an ever-changing world. Intended for integration throughout all K–12 academic and technical content areas, the New Jersey Student Learning Standards- Career Readiness, Life Literacies, and Key Skills (NJSLS-CLKS) provides the framework for students to learn the concepts, skills, and practices essential to the successful navigation of career exploration and preparation, personal finances and digital literacy.

Mission

Career readiness, life literacies, and key skills education provides students with the necessary skills to make informed career and financial decisions, engage as responsible community members in a digital society, and to successfully meet the challenges and opportunities in an interconnected global economy.

Vision

An education in career readiness, life literacies, and key skills fosters a population that:

•Continually self-reflects and seeks to improve the essential life and career practices that lead to success; •Uses effective communication and collaboration skills and resources to interact with a global society;

•Possesses financial literacy and responsibility at home and in the broader community;

•Plans, executes, and alters career goals in response to changing societal and economic conditions; and •Seeks to attain skill and content mastery to achieve success in a chosen career path.

Standards for Career Readiness, Life Literacy and Key Skills

- **9.1.8.CDM.1:** Compare and contrast the use of credit cards and debit cards for specific purchases and the advantages and disadvantages of using each.
- **9.1.8.CDM.2:** Demonstrate an understanding of the terminology associated with different types of credit (e.g. credit cards, installment loans, mortgages, lines of credit) and compare and calculate the interest rates associated with each.
- 9.1.8. FP.7: Identify the techniques and effects of deceptive advertising.
- 9.4.8.IML.2: Identify specific examples of distortion, exaggeration, or misrepresentation of information.
- **9.4.8.IML.12:** Use relevant tools to produce, publish, and deliver information supported with evidence for an authentic audience.
- **9.4.8.TL.2:** Gather data and digitally represent information to communicate a real-world problem (e.g. MS-ESS3-4, 6.1.8.EconET.1, 6.1.8.CivicsPR.4)
- 9.4.8.TL.3: Select appropriate tools to organize and present information digitally.
- 9.4.8.TL.6:Collaborate to develop and publish work that provides perspectives on a real-world problem.

Computer Science and Design Thinking

Computer Science and Design Thinking

New approaches necessary for solving the critical challenges that we face as a society will require harnessing the power of technology and computing. Rapidly changing technologies and the proliferation of digital information have permeated and radically transformed learning, working, and everyday life. To be well-educated, global-minded individuals in a computing-intensive world, students must have a clear understanding of the concepts and practices of computer science. As education systems adapt to a vision of students who are not just computer users but also computationally literate creators who are proficient in the concepts and practices of computer science and design thinking, engaging students in computational thinking and human-centered approaches to design through the study of computer science and technology serves to prepare students to ethically produce and critically consume technology.

Mission

Computer science and design thinking education prepares students to succeed in today's knowledge-based economy by providing equitable and expanded access to high-quality, standards-based computer science and technological design education.

Vision

All students have equitable access to a rigorous computer science and design thinking education. Students will benefit from opportunities to engage in high-quality technology programs that foster their ability to: • develop and apply computational and design thinking to address real-world problems and design creative solutions;

• engage as collaborators, innovators, and entrepreneurs on a clear pathway to success through postsecondary education and careers;

• navigate the dynamic digital landscape to become healthy, productive, 21st century global-minded individuals; and

• participate in an inclusive and diverse computing culture that appreciates and incorporates perspectives from people of different genders, ethnicities, and abilities.

Standards for Computer Science and Design Thinking

- **8.1.8.DA.1:** Organize and transform data collected using computational tools to make it usable for a specific purpose.
- **8.1.8.DA.5:** Test, analyze, and refine computational models.
- **8.1.8.AP.1:** Design and illustrate algorithms that solve complex problems using flowcharts and/or pseudocode.

• **8.1.8.AP.4:** Decompose problems and sub-problems into parts to facilitate the design, implementations and review of programs.